

# Lecture 05

## References and Mutable Data



Luna received a duck. The duck is mutable (note missing limbs)

# hw02 technical notes

## Testing for expected outcome

- `assert my_function() == b`

This works for **integers**, **strings**, and **Booleans**

## What about floating point numbers?

- `assert 3.14159265 - eps < calc_pi() and`

`calc_pi() < 3.14159265 + eps`

Note: 'eps' should be some small floating point number (e.g., 1e-6)

# hw02 technical notes (con't)

## Conversions of data types and constants:

- float()
- int()
- str()
- float('inf')
- -float('inf')
- float('nan')

## Checking the Python version:

Add this to the top of your .py script

```
import sys
print(sys.version)
```

This should produce version 3.x.y

```
3.5.3 (default, Sep 27 2018, 17:25:39)
[GCC 6.3.0 20170516]
```

# Recall: Variables as Boxes

- You can picture a variable as a named "box" in memory.
- Example from an early lecture:

num1 = 100  
num2 = 120

num1

100

num2

120

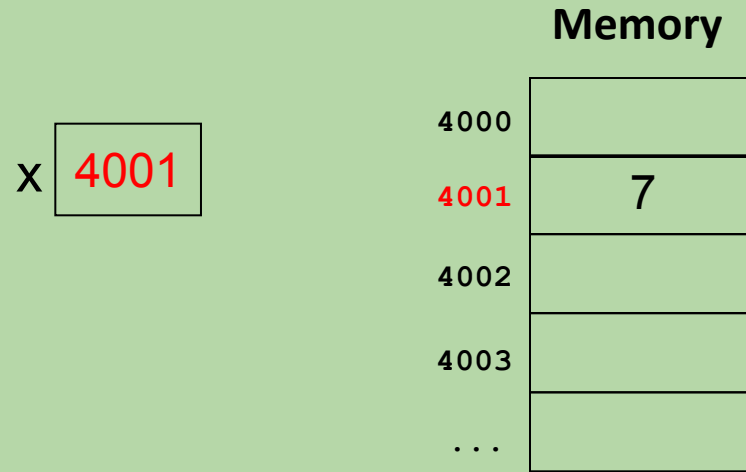
# Variables and Values

- In Python, when we assign a value to a variable, we're not actually storing the value *in* the variable.
- Rather:
  - the value is somewhere else in memory
  - the variable stores the *memory address* of the value.
- Example: `x = 7`

x 4001

| Memory |   |
|--------|---|
| 4000   |   |
| 4001   | 7 |
| 4002   |   |
| 4003   |   |
| ...    |   |

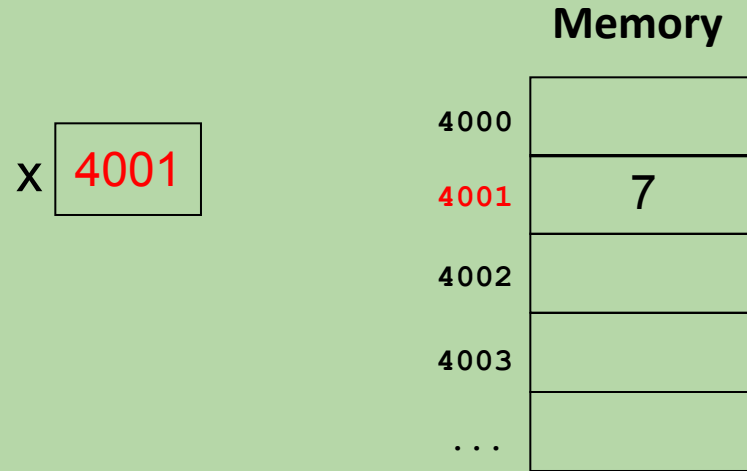
# References



We say that a variable stores a *reference* to its value.

- also known as a *pointer*

# References (cont.)

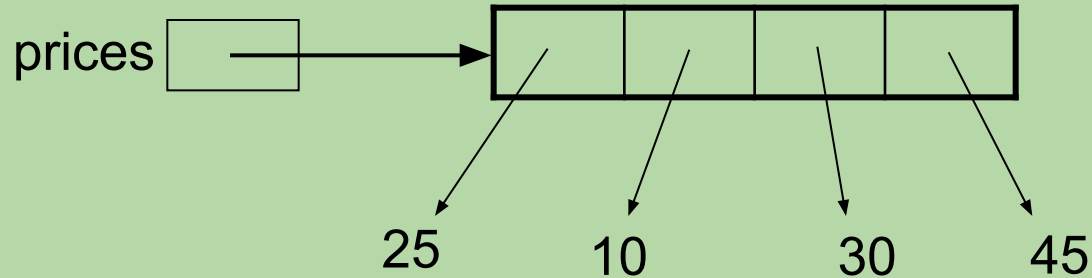


- Because we don't care about the actual memory address, we use an arrow to represent a reference:



# Lists and References

```
prices = [25, 10, 30, 45]
```



- When a variable represents a list, it stores a reference to the list.
- The list itself is a *collection* of references!
  - each element of the list is a reference to a value



# Mutable vs. Immutable Data

- In Python, strings and numbers are *immutable*.
  - their contents/components cannot be changed
- Lists are *mutable*.
  - their contents/components *can* be changed
  - example:

```
>>> prices = [25, 10, 30, 45]
>>> prices[2] = 50
>>> print(prices)
[25, 10, 50, 45]
```

# Changing a Value vs. Changing a Variable

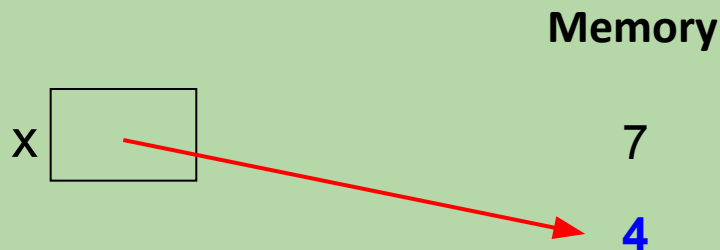
- There's no way to change an immutable value like 7.

x = 7



- However, we *can* use assignment to change the variable—making it refer to a different value:

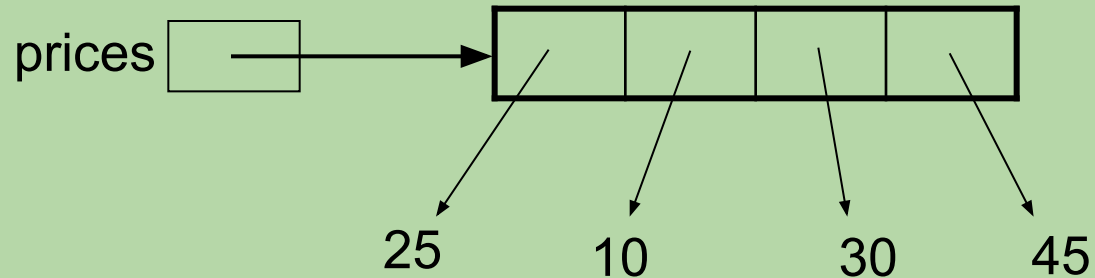
x = 4



- We're not actually changing the value 7.
- We're making the variable x refer to a different value.

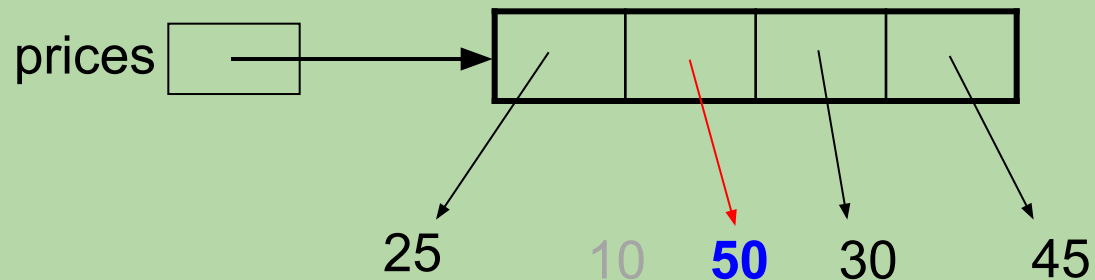
# Changing a Value vs. Changing a Variable

- Here's our original list:



- Lists are mutable, so we *can* change the value (the list) by modifying its elements:

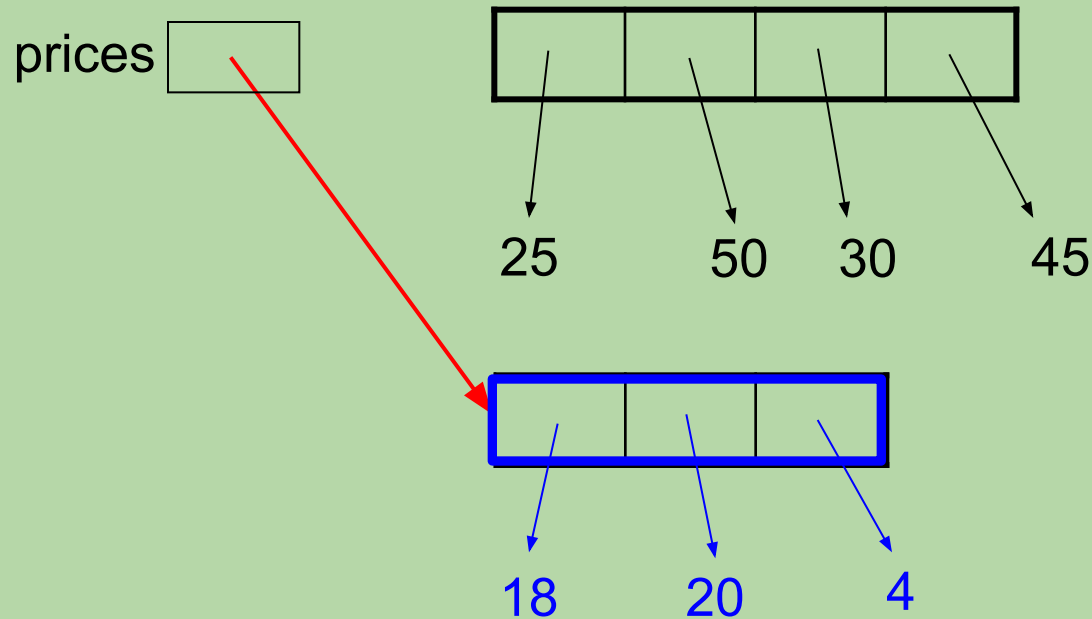
prices[1] = 50



# Changing a Value vs. Changing a Variable

- We can also change the variable—making it refer to a completely different list:

prices = [18, 20, 4]



# Simplifying Our Mental Model

- When a variable represents an **immutable** value, it's okay to picture the value as being *inside* the variable.

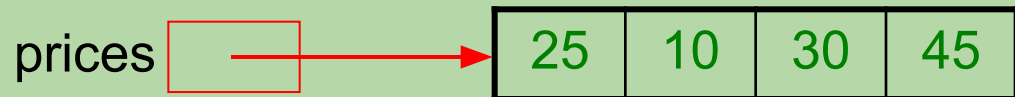
`x = 7`                      `x`

|   |
|---|
| 7 |
|---|

- a simplified picture, but good enough!

- The same thing holds for list elements that are **immutable**.

`prices = [25, 10, 30, 45]`



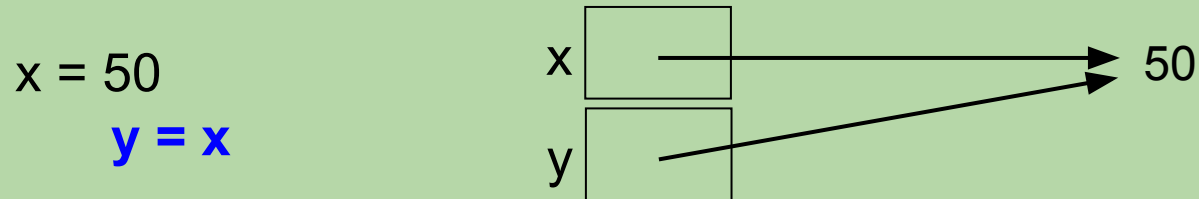
- We still need to use references for **mutable** data like lists.

# Copying Variables

- The assignment

*var2 = var1*

copies the reference of *var1* into *var2*, e.g.,



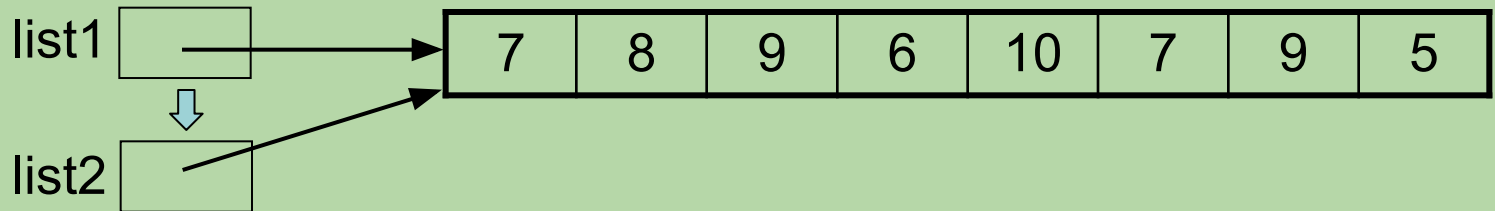
- But when the data in *var1* is **immutable** you can use the box notation, e.g.,



# Copying References

- Consider this example:

```
list1 = [7, 8, 9, 6, 10, 7, 9, 5]  
list2 = list1
```



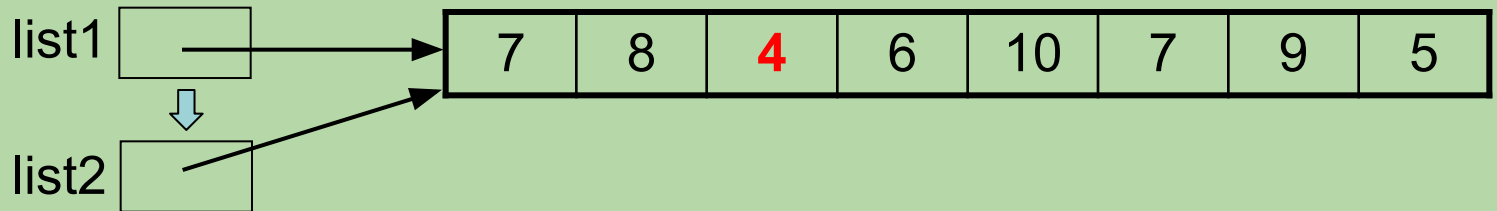
- Given the lines of code above, what will the lines below print?

```
list2[2] = 4  
print(list1[2], list2[2])
```

# Copying References

- Consider this example:

```
list1 = [7, 8, 9, 6, 10, 7, 9, 5]  
list2 = list1
```



- Given the lines of code above, what will the lines below print?

```
list2[2] = 4  
print(list1[2], list2[2])
```

4 4  
4 4

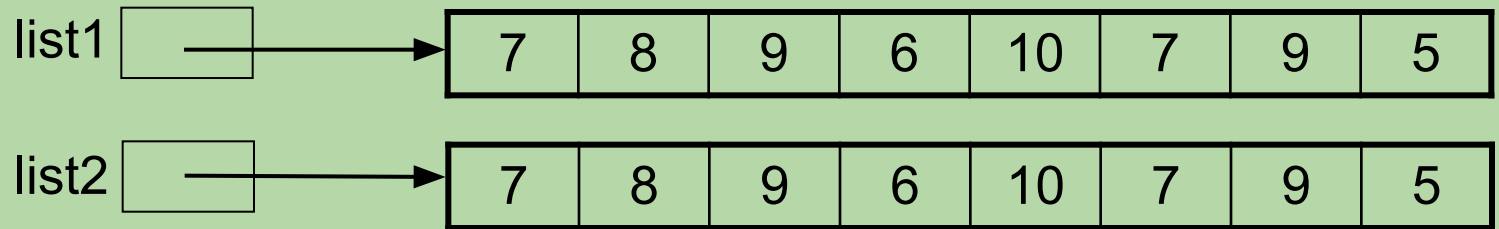
- Copying a list variable simply copies the reference.
- It doesn't copy the list itself!



# Copying a List, using slicing

- We can copy a list like slicing:

```
list1 = [7, 8, 9, 6, 10, 7, 9, 5]  
list2 = list1[:]
```



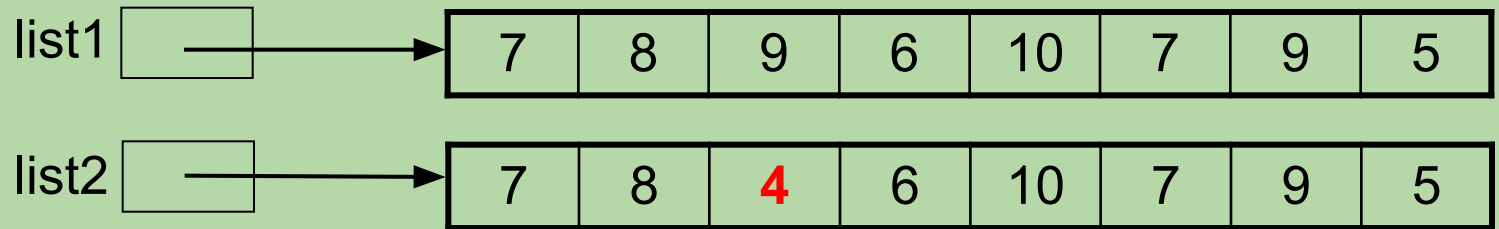
- What will this print now?

```
list2[2] = 4  
print(list1[2], list2[2])
```

# Copying a List, using slicing

- We can copy a list like this one using a full slice:

```
list1 = [7, 8, 9, 6, 10, 7, 9, 5]
list2 = list1[:]
```



- What will this print now?

```
list2[2] = 4
print(list1[2], list2[2])
```

9 4

9 4

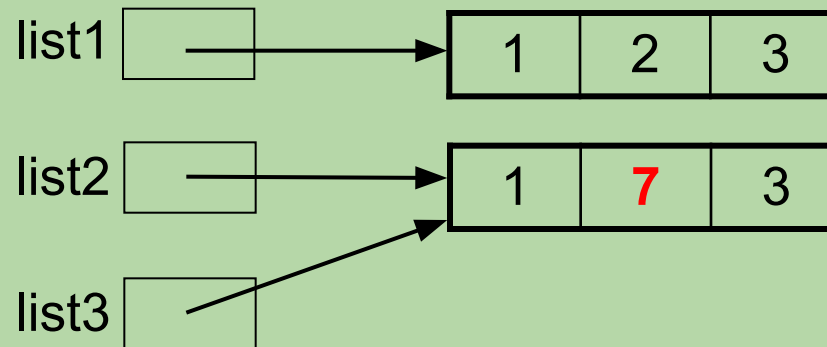
# What does this program output?

```
list1 = [1, 2, 3]
list2 = list1[:]
list3 = list2
list2[1] = 7
print(list1, list2, list3)
```

- A. [1, 2, 3] [1, 7, 3] [1, 2, 3]
- B. [1, 7, 3] [1, 7, 3] [1, 2, 3]
- C. [1, 2, 3] [1, 7, 3] [1, 7, 3]
- D. [1, 7, 3] [1, 7, 3] [1, 7, 3]

# What does this program output?

```
list1 = [1, 2, 3]
list2 = list1[:]
list3 = list2
list2[1] = 7
print(list1, list2, list3)
```



- A. [1, 2, 3] [1, 7, 3] [1, 2, 3]
- B. [1, 7, 3] [1, 7, 3] [1, 2, 3]
- C. [1, 2, 3] [1, 7, 3] [1, 7, 3]
- D. [1, 7, 3] [1, 7, 3] [1, 7, 3]

# What does this program output?

```
list1 = [1, 2, 3]
list2 = list1[:]
list3 = list2
list2[1] = 7
print(list1, list2, list3)
```

list1 

|     |
|-----|
| 128 |
|-----|

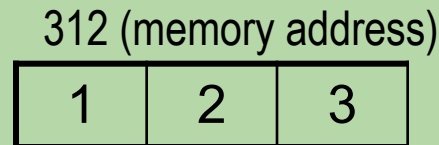
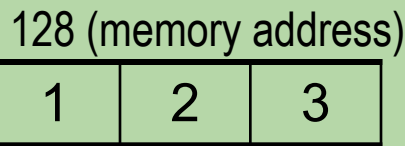
list2 

|     |
|-----|
| 312 |
|-----|



list3 

|     |
|-----|
| 312 |
|-----|



- A. [1, 2, 3] [1, 7, 3] [1, 2, 3]
- B. [1, 7, 3] [1, 7, 3] [1, 2, 3]
- C. [1, 2, 3] [1, 7, 3] [1, 7, 3]
- D. [1, 7, 3] [1, 7, 3] [1, 7, 3]

# Passing an Immutable Value to a Function

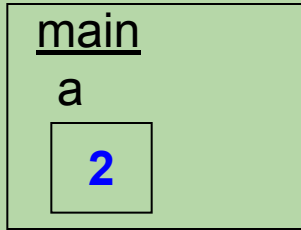
- When an immutable value (like a number or string) is passed into a function, we can think of the function as getting a copy of value (though really it gets a reference).
- If the function changes its copy of the value, that change will *not* be there when the function returns, this is because any assignment to the local variable updates it's reference and not the referenced value.
- Consider the following program:

```
def main():  
    a = 2  
    triple(a)  
    print(a)      # what will be printed?
```

```
def triple(x):  
    x = x * 3
```

# Passing an Immutable Value to a Function (cont.)

*before call to triple()*

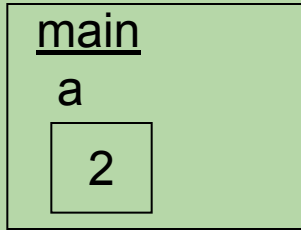


```
def triple(x):  
    x = x * 3
```

```
def main():  
    a = 2  
    triple(a)  
    print(a)
```

# Passing an Immutable Value to a Function (cont.)

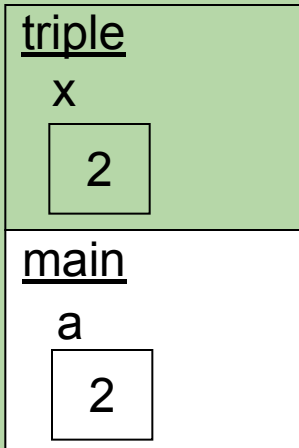
*before call to triple()*



```
def triple(x):
    x = x * 3
```

```
def main():
    a = 2
    triple(a)
    print(a)
```

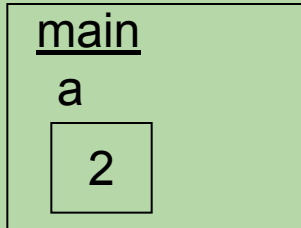
*during call to triple()*





# Passing an Immutable Value to a Function (cont.)

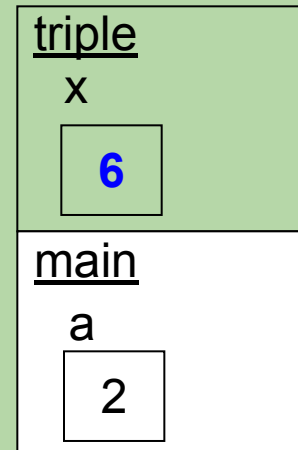
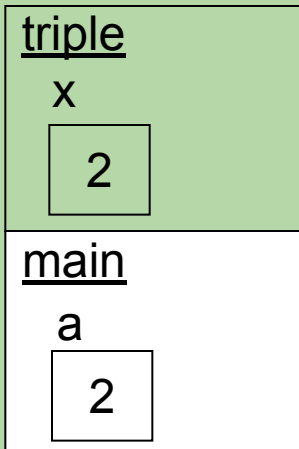
*before call to triple()*



```
def triple(x):  
    x = x * 3
```

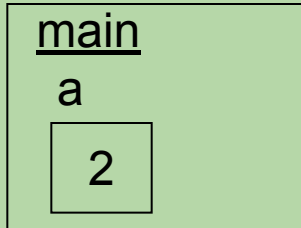
```
def main():  
    a = 2  
    triple(a)  
    print(a)
```

*during call to triple()*



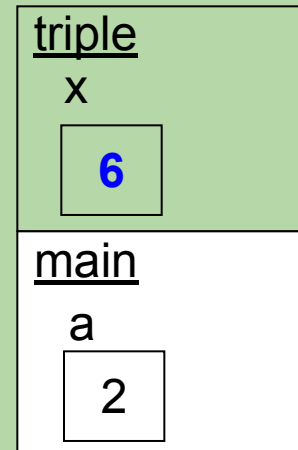
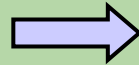
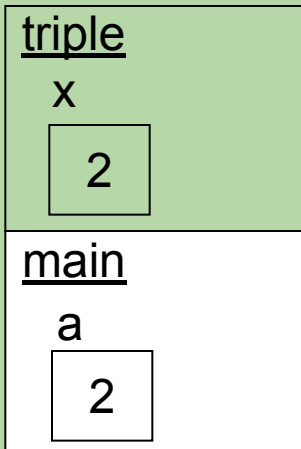
# Passing an Immutable Value to a Function (cont.)

*before call to triple()*

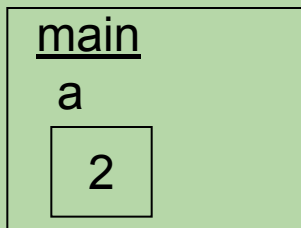


```
def main():  
    a = 2  
    triple(a)  
    print(a)    # prints 2
```

*during call to triple()*



*after call to triple()*



# Passing a List to a Function

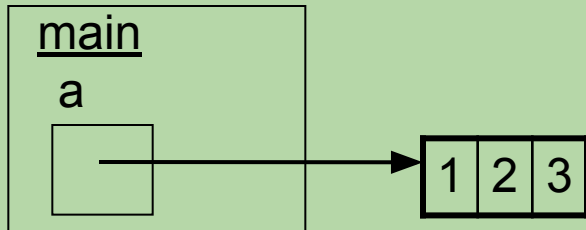
- When a list is passed into a function:
  - the function gets a copy of the *reference* to the list
  - it does *not* get a copy of the list itself
- Thus, if the function changes the components of the list, those changes will be there when the function returns.
- Consider the following program:

```
def main():  
    a = [1, 2, 3]  
    triple(a)  
    print(a)      # what will be printed?
```

```
def triple(vals):  
    for i in range(len(vals)):  
        vals[i] = vals[i] * 3
```

# Passing a List to a Function (cont.)

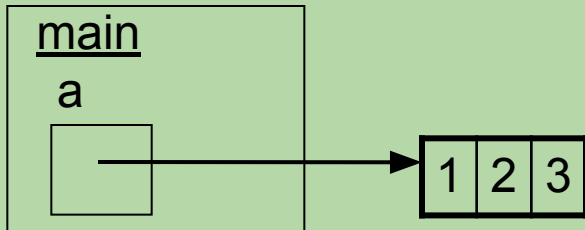
*before call to triple()*



```
def main():  
    a = [1, 2, 3]  
    triple(a)  
    print(a)
```

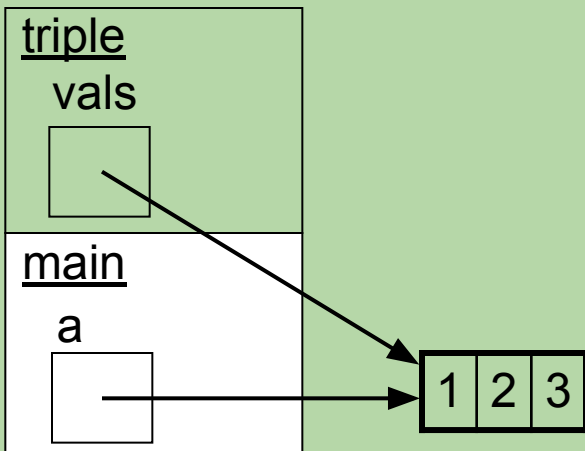
# Passing a List to a Function (cont.)

*before call to triple()*



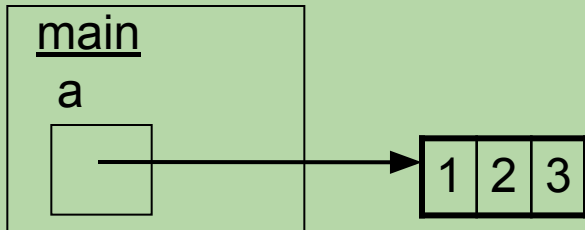
```
def main():  
    a = [1, 2, 3]  
    triple(a)  
    print(a)
```

*during call to triple()*



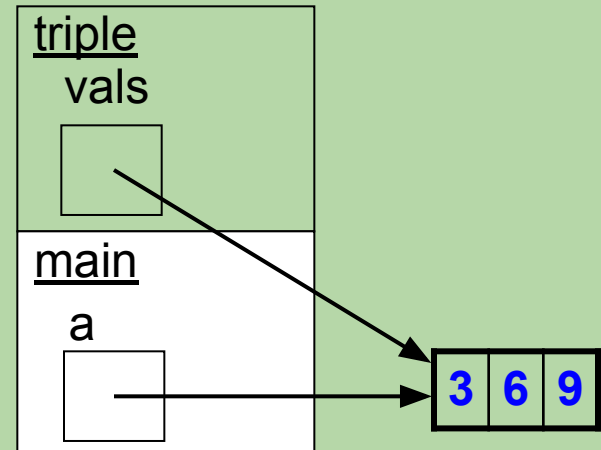
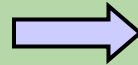
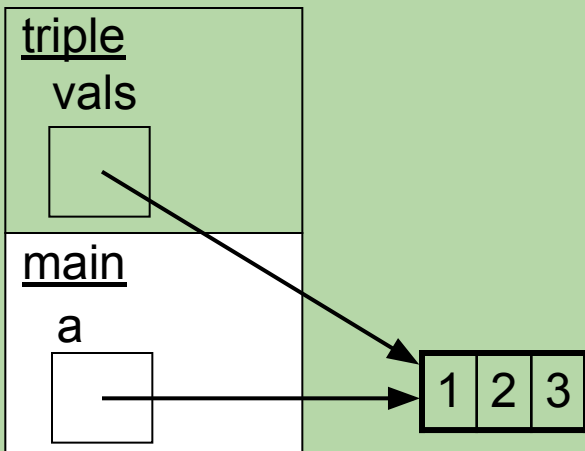
# Passing a List to a Function (cont.)

*before call to triple()*



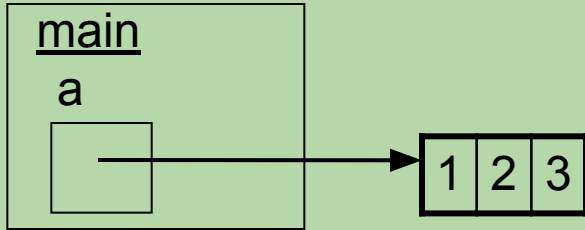
```
def triple(vals) :  
    for i in range(len(vals)):  
        vals[i] = vals[i] * 3
```

*during call to triple()*



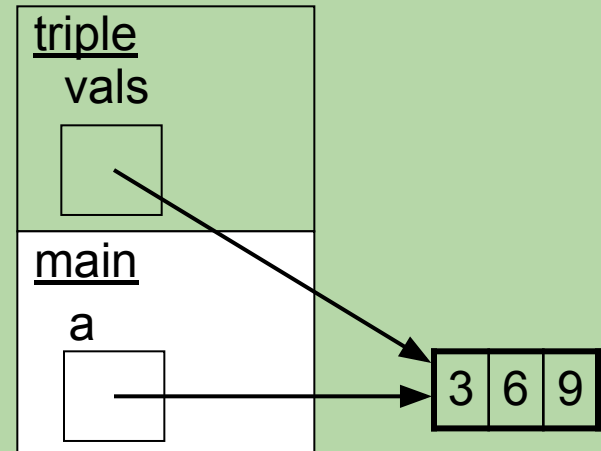
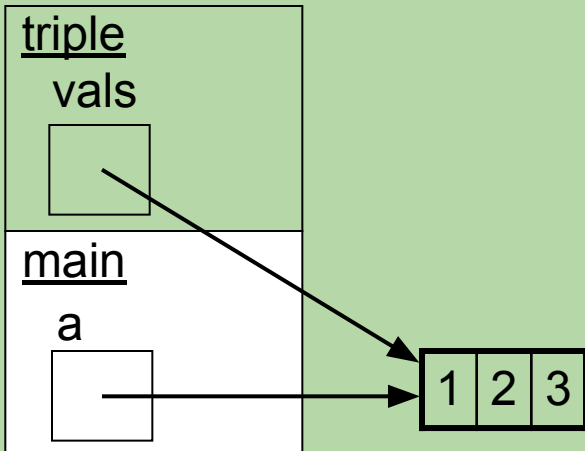
# Passing a List to a Function (cont.)

*before call to triple()*

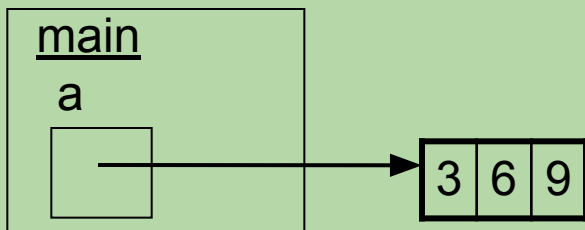


```
def main():  
    a = [1, 2, 3]  
    triple(a)  
    print(a) # prints [3, 6, 9]
```

*during call to triple()*



*after call to triple()*



# What does this program output?

```
def mystery1(x):
```

```
    x *= 2
```

```
    return x
```

```
def mystery2(vals):
```

```
    vals[0] = 111
```

```
    return vals
```

```
x = 7
```

```
vals = [7, 7]
```

```
mystery1(x)
```

```
mystery2(vals)
```

```
print(x, vals)
```

- A. 7 [7, 7]
- B. 14 [7, 7]
- C. 7 [111, 7]
- D. 14 [111, 7]



# What does this program output?

```
def mystery1(x):
```

```
    x *= 2
```

```
    return x
```

```
def mystery2(vals):
```

```
    vals[0] = 111
```

```
    return vals
```

```
x = 7
```

```
vals = [7, 7]
```

```
mystery1(x)
```

```
mystery2(vals)
```

```
print(x, vals)
```

- A. 7 [7, 7]
- B. 14 [7, 7]
- C. **7 [111, 7]**
- D. 14 [111, 7]

# What does this program output?

```
def mystery1(x):
```

```
    x *= 2
```

```
    return x
```

```
def mystery2(vals):
```

```
    vals[0] = 111
```

```
    return vals
```

```
x = 7
```

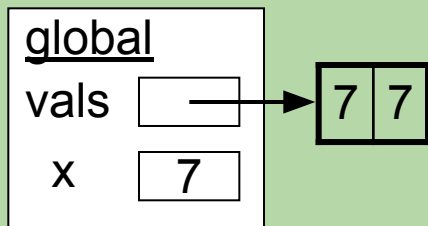
```
vals = [7, 7]
```

```
mystery1(x) # throws return value away!
```

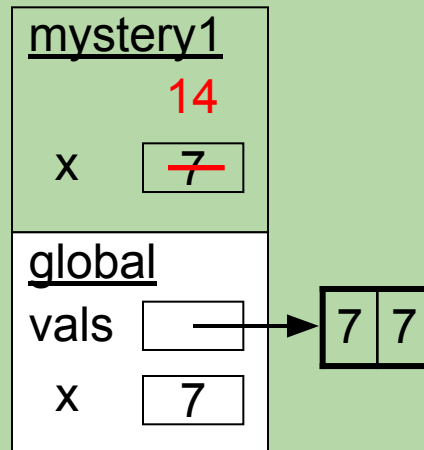
```
mystery2(vals)
```

```
print(x, vals)
```

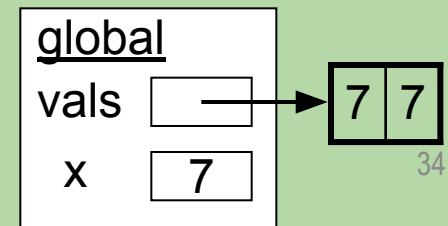
*before* mystery1



*during* mystery1



*after* mystery1



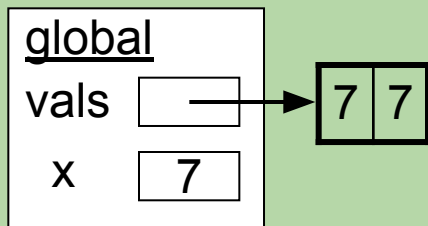
# What does this program output?

```
def mystery1(x):  
    x *= 2  
    return x  
  
def mystery2(vals):  
    vals[0] = 111  
    return vals
```

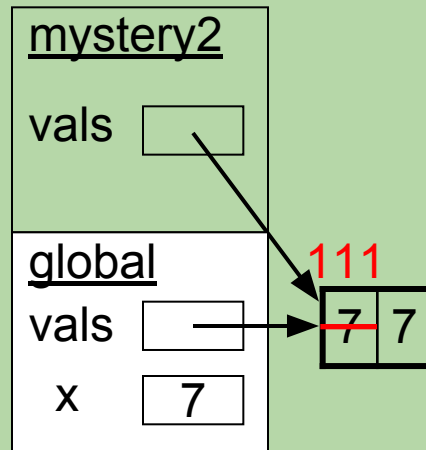
```
x = 7  
vals = [7, 7]  
mystery1(x)  
mystery2(vals)  
print(x, vals)
```

# output: 7 [111, 7]

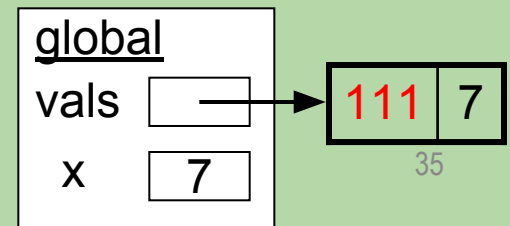
before **mystery2**



during **mystery2**



after **mystery2**

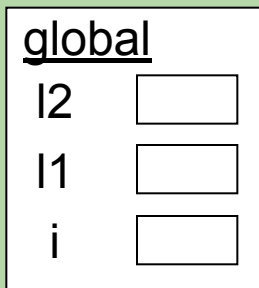


# What does this program print? Draw your own memory diagrams!

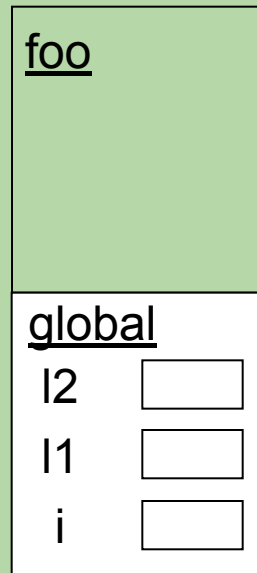
```
def foo(vals, i):  
    i += 1  
    vals[i] *= 2
```

```
i = 0  
l1 = [1, 1, 1]  
l2 = l1  
foo(l2, i)  
print(i, l1, l2)
```

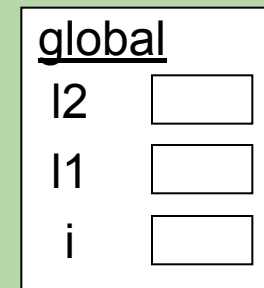
*before foo*



*during foo*



*after foo*



# What does this program print? Draw your own memory diagrams!

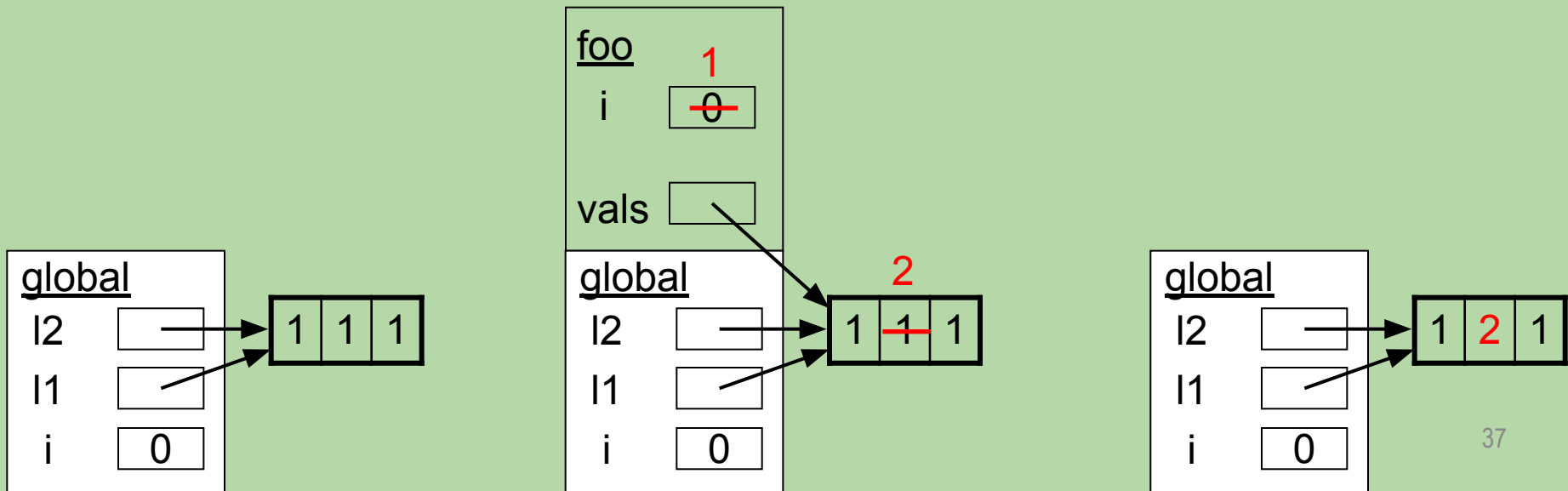
```
def foo(vals, i):  
    i += 1  
    vals[i] *= 2
```

```
i = 0  
l1 = [1, 1, 1]  
l2 = l1  
foo(l2, i)  
print(i, l1, l2) # output: 0 [1, 2, 1] [1, 2, 1]
```

*before foo*

*during foo*

*after foo*



# Extra practice: What about this program?

```
def mystery3(x):
```

```
    x = 111
```

```
    return x
```

```
def mystery4(vals):
```

```
    vals = [111, 111]
```

```
    return vals
```

```
x = 7
```

```
vals = [7, 7]
```

```
mystery3(x)
```

```
mystery4(vals)
```

```
print(x, vals)
```

- A. 7 [7, 7]
- B. 111 [7, 7]
- C. 7 [111, 111]
- D. 111 [111, 111]

# Extra practice: What about this program?

```
def mystery3(x):
```

```
    x = 111
```

```
    return x
```

```
def mystery4(vals):
```

```
    vals = [111, 111]
```

```
    return vals
```

```
x = 7
```

```
vals = [7, 7]
```

```
mystery3(x)
```

```
mystery4(vals)
```

```
print(x, vals)
```

A.      **7 [7, 7]**

B.      111 [7, 7]

C.      7 [111, 111]

D.      111 [111, 111]

# Extra practice: What about this program?

```
def mystery3(x):
```

```
    x = 111
```

```
    return x
```

```
def mystery4(vals):
```

```
    vals = [111, 111]
```

```
    return vals
```

```
x = 7
```

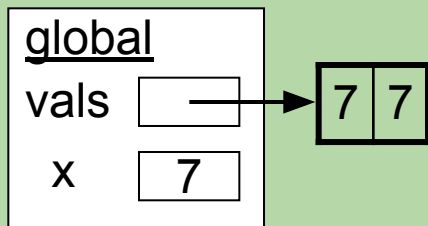
```
vals = [7, 7]
```

```
mystery3(x) # throw return value away!
```

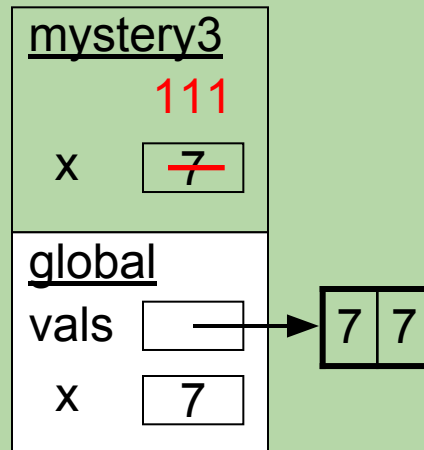
```
mystery4(vals)
```

```
print(x, vals)
```

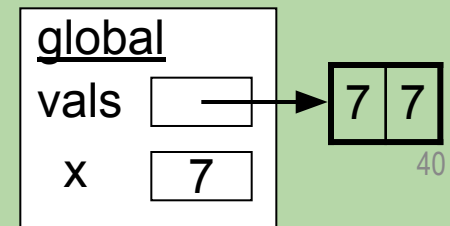
*before* **mystery3**



*during* **mystery3**



*after* **mystery3**





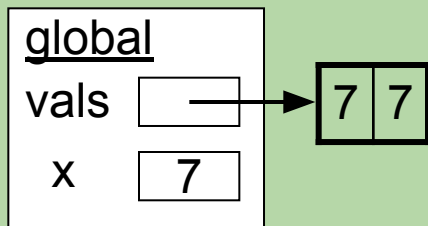
# Extra practice: What about this program?

```
def mystery3(x):  
    x = 111  
    return x  
  
def mystery4(vals):  
    vals = [111, 111]  
    return vals
```

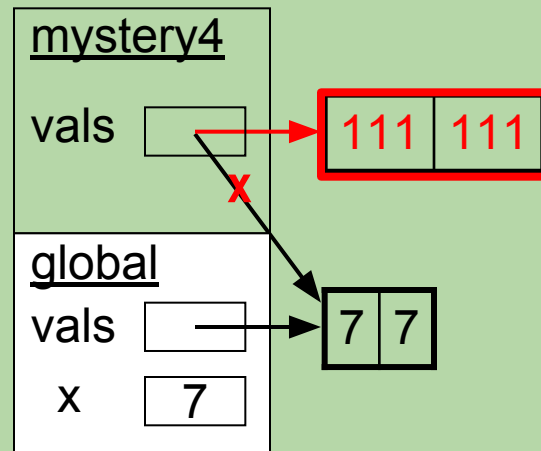
```
x = 7  
vals = [7, 7]  
mystery3(x)  
mystery4(vals)
```

**print(x, vals) # output: 7 [7, 7]**

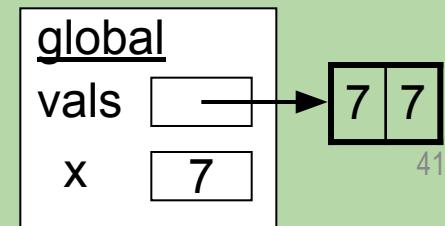
*before* `mystery4`



*during* `mystery4`



*after* `mystery4`



# Recall Our Earlier Example...

```
def mystery1(x):
```

```
    x *= 2
```

```
    return x
```

```
def mystery2(vals):
```

```
    vals[0] = 111
```

```
    return vals
```

```
x = 7
```

```
vals = [7, 7]
```

```
mystery1(x)
```

```
mystery2(vals)
```

```
print(x, vals)
```

How can we make the *global* x reflect mystery1's change?

# Recall Our Earlier Example...

```
def mystery1(x):
```

```
    x *= 2
```

```
    return x
```

```
def mystery2(vals):
```

```
    vals[0] = 111
```

```
    return vals
```

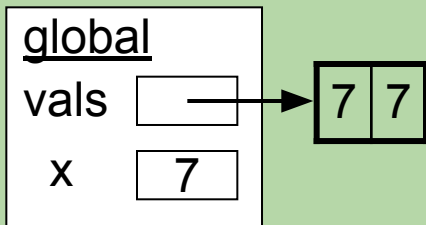
```
x = 7
```

```
vals = [7, 7]
```

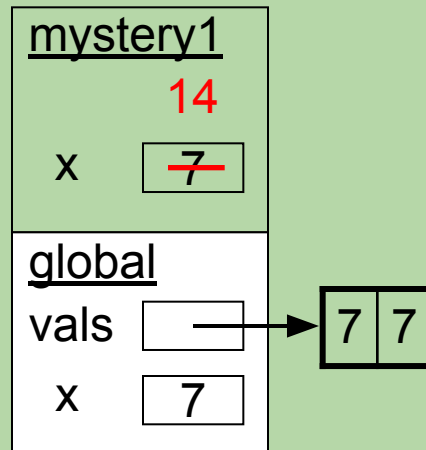
```
x = mystery1(x) # assign the return value!
```

```
mystery2(vals)
```

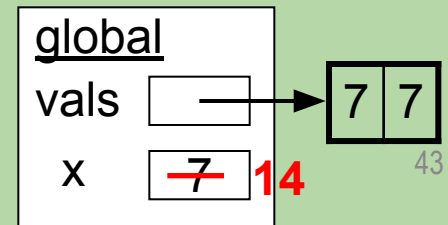
```
before (mystery1)
```



```
during mystery1
```



```
after mystery1
```



# 2-D Lists

*based in part on notes from the CS-for-All curriculum  
developed at Harvey Mudd College*

## 2-D Lists

- Recall that a list can include sublists

```
mylist = [17, 2, [2, 5], [1, 3, 7]]
```

What is `len(mylist)`?

## 2-D Lists

- Recall that a list can include sublists

```
mylist = [17, 2, [2, 5], [1, 3, 7]]
```

What is `len(mylist)`? 4

- To capture a rectangular table or grid of values, use a *two-dimensional* list:

```
table = [[15, 8, 3, 16, 12, 7, 9, 5],  
         [6, 11, 9, 4, 1, 5, 8, 13],  
         [17, 3, 5, 18, 10, 6, 7, 21],  
         [8, 14, 13, 6, 13, 12, 8, 4],  
         [1, 9, 5, 16, 20, 2, 3, 9]]
```

- a list of sublists, each with the same length
- each sublist is one "row" of the table

## 2-D Lists: Try These Questions!

```
table = [[15, 8, 3, 16, 12, 7, 9 5],  
         [ 6, 11, 9, 4, 1, 5, 8, 13],  
         [17, 3, 5, 18, 10, 6, 7, 21],  
         [ 8, 14, 13, 6, 13, 12, 8, 4],  
         [ 1, 9, 5, 16, 20, 2, 3, 9]]
```

- what is `len(table)`?
- what does `table[0]` represent?
  - `table[1]`?
  - `table[-1]`?
- what is `len(table[0])`?
- what is `table[3][1]`?
- how would you change the 1 in the lower-left corner to a 7?

## 2-D Lists: Try These Questions!

```
table = [[15, 8, 3, 16, 12, 7, 9, 5],
         [ 6, 11, 9, 4, 1, 5, 8, 13],
         [17, 3, 5, 18, 10, 6, 7, 21],
         [ 8, 14, 13, 6, 13, 12, 8, 4],
         [ 1, 9, 5, 16, 20, 2, 3, 9]]
```

- what is `len(table)`? 5 (more generally, the # of rows / height)
- what does `table[0]` represent? the first/top row
  - `table[1]`? the second row
  - `table[-1]`? the last/bottom row
- what is `len(table[0])`? 8 (the # of columns / width)
- what is `table[3][1]`? 14
  - row index ↗
  - column index ↖
- how would you change the 1 in the lower-left corner to a 7?  
`table[4][0] = 7` # `table[-1][0] = 7` also works!



# Dimensions of a 2-D List

```
table = [[15, 8, 3, 16, 12, 7, 9, 5],  
         [ 6, 11, 9, 4, 1, 5, 8, 13],  
         [17, 3, 5, 18, 10, 6, 7, 21],  
         [ 8, 14, 13, 6, 13, 12, 8, 4],  
         [ 1, 9, 5, 16, 20, 2, 3, 9]]
```

`len(table)` is the # of rows in table

`table[r]` is the row with index `r`

`len(table[r])` is the # of elements in row `r`

`len(table[0])` is the # of columns in table

# Picturing a 2-D List

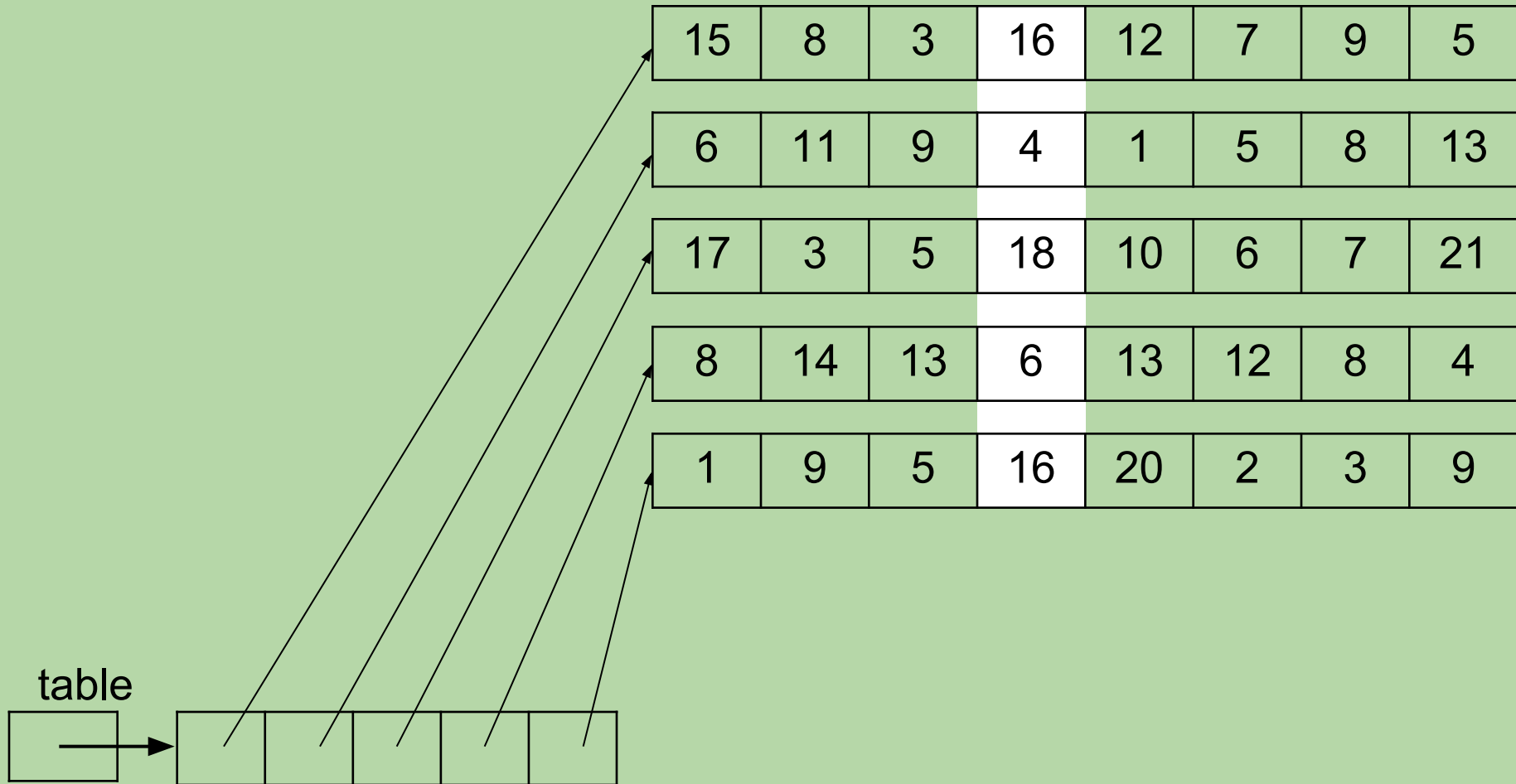
```
table = [[15, 8, 3, 16, 12, 7, 9, 5],  
         [ 6, 11, 9, 4, 1, 5, 8, 13],  
         [17, 3, 5, 18, 10, 6, 7, 21],  
         [ 8, 14, 13, 6, 13, 12, 8, 4],  
         [ 1, 9, 5, 16, 20, 2, 3, 9]]
```

- Here's one way to picture the above list:

|   | 0  | 1  | 2  | 3  | 4  | 5  | 6 | 7  | ← column indices |
|---|----|----|----|----|----|----|---|----|------------------|
| 0 | 15 | 8  | 3  | 16 | 12 | 7  | 9 | 5  |                  |
| 1 | 6  | 11 | 9  | 4  | 1  | 5  | 8 | 13 |                  |
| 2 | 17 | 3  | 5  | 18 | 10 | 6  | 7 | 21 |                  |
| 3 | 8  | 14 | 13 | 6  | 13 | 12 | 8 | 4  |                  |
| 4 | 1  | 9  | 5  | 16 | 20 | 2  | 3 | 9  | row indices →    |

# Picturing a 2-D List (cont)

- Here's a more accurate picture:



# Accessing an Element of a 2-D List

```
table = [[15, 8, 3, 16, 12, 7, 9, 5],  
         [ 6, 11, 9, 4, 1, 5, 8, 13],  
         [17, 3, 5, 18, 10, 6, 7, 21],  
         [ 8, 14, 13, 6, 13, 12, 8, 4],  
         [ 1, 9, 5, 16, 20, 2, 3, 9]]
```

`table[r][c]` is the element at row `r`, column `c` in table

*examples:*

```
>>> print(table[2][1])
```

3

↑      ↑  
row index      column index

# Accessing an Element of a 2-D List

```
table = [[15, 8, 3, 16, 12, 7, 9, 5],  
         [ 6, 11, 9, 4, 1, 5, 8, 13],  
         [17, 3, 5, 18, 10, 6, 7, 21],  
         [ 8, 14, 13, 6, 13, 12, 8, 4],  
         [ 1, 9, 5, 16, 20, 2, 0, 9]]
```

`table[r][c]` is the element at row `r`, column `c` in table

*examples:*

```
>>> print(table[2][1])
```

3

↑      ↑  
row index      column index

```
>>> table[-1][-2] = 0
```

# Using Nested Loops to Process a 2-D List

```
table = [[15, 8, 3, 16, 12, 7, 9 5],  
         [ 6, 11, 9, 4, 1, 5, 8, 13],  
         [17, 3, 5, 18, 10, 6, 7, 21],  
         [ 8, 14, 13, 6, 13, 12, 8, 4],  
         [ 1, 9, 5, 16, 20, 2, 3, 9]]
```

```
for r in range(len(table)):  
    for c in range(len(table[0])):  
        # process table[r][c]
```

# Using Nested Loops to Process a 2-D List

```
table = [[15, 19, 3, 16],  
         [ 6, 21, 9, 4],  
         [17, 3, 5, 18]]  
count = 0  
for r in range(len(table)):  
    for c in range(len(table[0])):  
        if table[r][c] > 15:  
            count += 1  
print(count)
```

---

| <u>r</u> | <u>c</u> | <u>table[r][c]</u> | <u>count</u> |
|----------|----------|--------------------|--------------|
|----------|----------|--------------------|--------------|

# Using Nested Loops to Process a 2-D List

```
table = [[15, 19, 3, 16],
         [ 6, 21, 9, 4],
         [17, 3, 5, 18]]
count = 0
for r in range(len(table)):
    for c in range(len(table[0])):
        if table[r][c] > 15:
            count += 1
```

**print(count)**

**# prints 5**

---

| <u>r</u> | <u>c</u> | <u>table[r][c]</u> | <u>count</u> |
|----------|----------|--------------------|--------------|
|          |          |                    | 0            |
| 0        | 0        | 15                 | 0            |
| 0        | 1        | 19                 | 1            |
| 0        | 2        | 3                  | 1            |
| 0        | 3        | 16                 | 2            |
| 1        | 0        | 6                  | 2            |
| 1        | 1        | 21                 | 3            |
| ...      |          |                    |              |
| 2        | 0        | 17                 | 4            |
| ...      |          |                    |              |
| 2        | 3        | 18                 | 5            |



# Which Of These Counts the Number of Evens?

```
table = [[15, 19, 3, 16],  
         [ 6, 21, 9, 4],  
         [17, 3, 5, 18]]
```

A. 

```
count = 0  
for r in range(len(table)):  
    for c in range(len(table[0])):  
        if table[r][c] % 2 == 0:  
            count += 1
```

B. 

```
count = 0  
for r in len(table):  
    for c in len(table[0]):  
        if c % 2 == 0:  
            count += 1
```

C. 

```
count = 0  
for r in range(len(table[0])):  
    for c in range(len(table)):  
        if table[r][c] % 2 == 0:  
            count += 1
```

D. either A or B      E. either A or C

# Which Of These Counts the Number of Evens?

```
table = [[15, 19, 3, 16],  
         [ 6, 21, 9, 4],  
         [17, 3, 5, 18]]
```

A. **count = 0**  
**for r in range(len(table)):**  
    **for c in range(len(table[0])):**  
        **if table[r][c] % 2 == 0:**  
            **count += 1**

B. count = 0  
for r in len(table):  
    for c in len(table[0]):  
        if c % 2 == 0:  
            count += 1

C. count = 0  
for r in range(len(table[0])):  
    for c in range(len(table)):  
        if table[r][c] % 2 == 0:  
            count += 1

D. either A or B      E. either A or C

# Using Nested Loops to Process a 2-D List

```
table = [[15, 19, 3, 16],  
         [ 6, 21, 9, 4],  
         [17, 3, 5, 18]]  
count = 0  
for r in range(len(table)):  
    for c in range(len(table[0])):  
        if table[r][c] % 2 == 0:  
            count += 1  
print(count)
```

---

| <u>r</u> | <u>c</u> | <u>table[r][c]</u> | <u>count</u> |
|----------|----------|--------------------|--------------|
|----------|----------|--------------------|--------------|

# Using Nested Loops to Process a 2-D List

```
table = [[15, 19, 3, 16],  
         [ 6, 21, 9, 4],  
         [17, 3, 5, 18]]  
count = 0  
for r in range(len(table)):  
    for c in range(len(table[0])):  
        if table[r][c] % 2 == 0:  
            count += 1
```

**print(count)**

**# prints 4**

---

| <u>r</u> | <u>c</u> | <u>table[r][c]</u> | <u>count</u> |
|----------|----------|--------------------|--------------|
|          |          |                    | 0            |
| 0        | 0        | 15                 | 0            |
| 0        | 1        | 19                 | 0            |
| 0        | 2        | 3                  | 0            |
| 0        | 3        | 16                 | 1            |
| 1        | 0        | 6                  | 2            |
| 1        | 1        | 21                 | 2            |
| ...      |          |                    |              |
| 1        | 3        | 4                  | 3            |
| ...      |          |                    |              |
| 2        | 3        | 18                 | 4            |

# What is the output of this program?

```
def mystery5(x):
```

```
    x = x * -1
```

```
    return x
```

```
def mystery6(l1, l2):
```

```
    l1[0] = 0
```

```
    l2 = [1, 1]
```

```
x = 7
```

```
vals = [7, 7]
```

```
mystery5(x)
```

```
mystery6(vals, vals)
```

```
print(x, vals)
```

- A. 7 [7, 7]
- B. -7 [1, 1]
- C. 7 [0, 7]
- D. 7 [1, 1]
- E. -7 [0, 7]

# What is the output of this program?

```
def mystery5(x):
```

```
    x = x * -1
```

```
    return x
```

```
def mystery6(l1, l2):
```

```
    l1[0] = 0
```

```
    l2 = [1, 1]
```

```
x = 7
```

```
vals = [7, 7]
```

```
mystery5(x)
```

```
mystery6(vals, vals)
```

```
print(x, vals)
```

- A. 7 [7, 7]
- B. -7 [1, 1]
- C. **7 [0, 7]**
- D. 7 [1, 1]
- E. -7 [0, 7]

# What is the output of this program?

```
def mystery5(x):
```

```
    x = x * -1
```

```
    return x
```

```
def mystery6(l1, l2):
```

```
    l1[0] = 0
```

```
    l2 = [1, 1]
```

```
x = 7
```

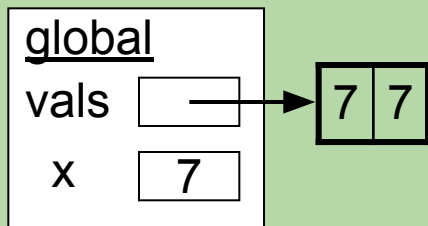
```
vals = [7, 7]
```

```
mystery5(x) # throw return value away!
```

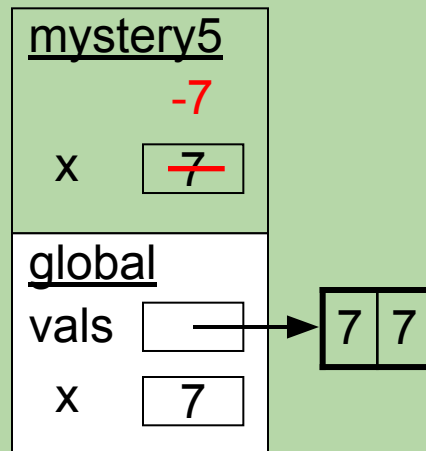
```
mystery6(vals, vals)
```

```
print(x, vals)
```

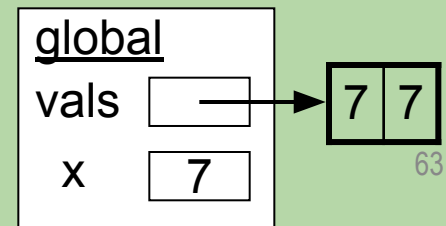
*before* **mystery5**



*during* **mystery5**



*after* **mystery5**



# What is the output of this program?

```
def mystery5(x):
```

```
    x = x * -1
```

```
    return x
```

```
def mystery6(l1, l2):
```

```
    l1[0] = 0
```

```
    l2 = [1, 1]
```

```
x = 7
```

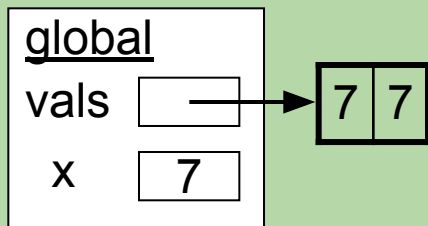
```
vals = [7, 7]
```

```
mystery5(x)
```

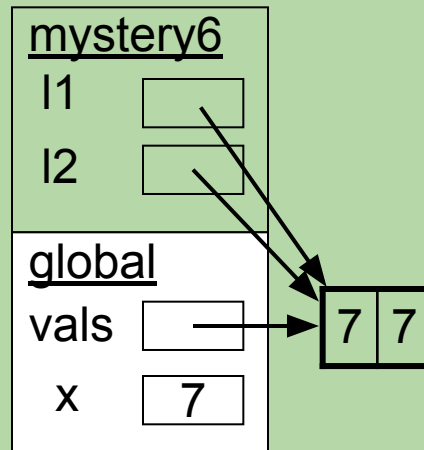
```
mystery6(vals, vals)
```

```
print(x, vals)
```

*before* **mystery6**



*during* **mystery6**





# What is the output of this program?

```
def mystery5(x):
```

```
    x = x * -1
```

```
    return x
```

```
def mystery6(l1, l2):
```

```
    l1[0] = 0
```

```
    l2 = [1, 1]
```

```
x = 7
```

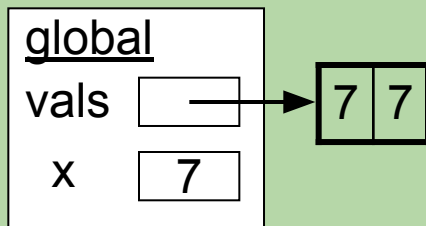
```
vals = [7, 7]
```

```
mystery5(x)
```

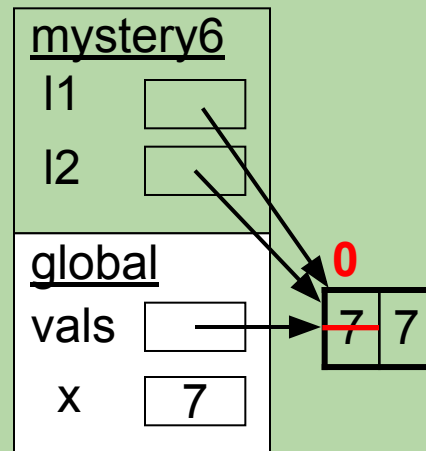
```
mystery6(vals, vals)
```

```
print(x, vals)
```

before `mystery6`



during `mystery6`



# What is the output of this program?

```
def mystery5(x):
```

```
    x = x * -1
```

```
    return x
```

```
def mystery6(l1, l2):
```

```
    l1[0] = 0
```

```
    l2 = [1, 1]
```

```
x = 7
```

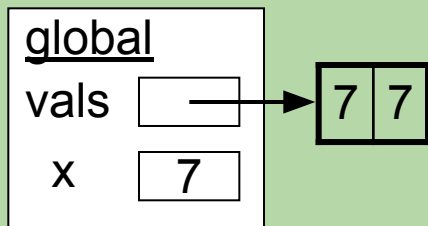
```
vals = [7, 7]
```

```
mystery5(x)
```

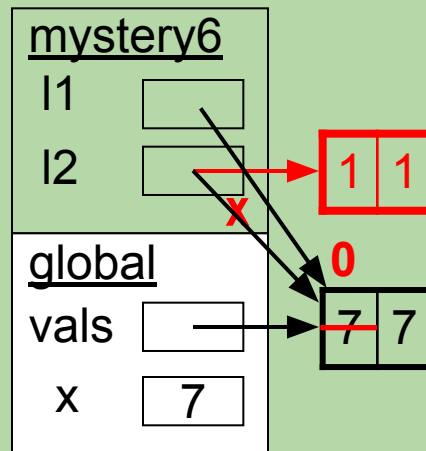
```
mystery6(vals, vals)
```

```
print(x, vals)
```

before `mystery6`



during `mystery6`



# What is the output of this program?

```
def mystery5(x):
```

```
    x = x * -1
```

```
    return x
```

```
def mystery6(l1, l2):
```

```
    l1[0] = 0
```

```
    l2 = [1, 1]
```

```
x = 7
```

```
vals = [7, 7]
```

```
mystery5(x)
```

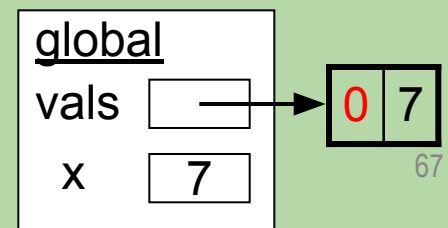
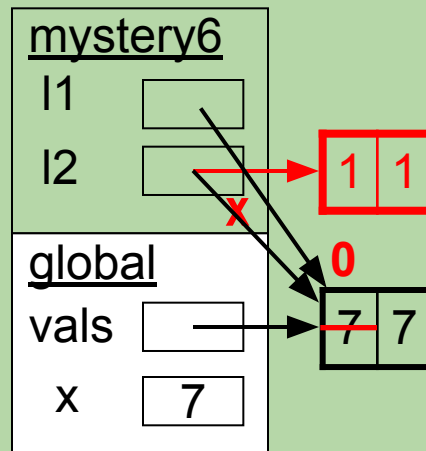
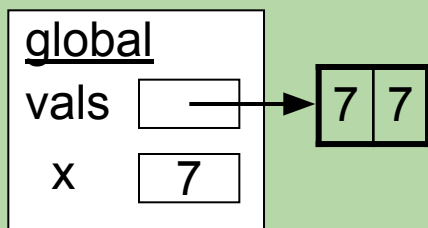
```
mystery6(vals, vals)
```

```
print(x, vals)      # output: 7 [0, 7]
```

*before* `mystery6`

*during* `mystery6`

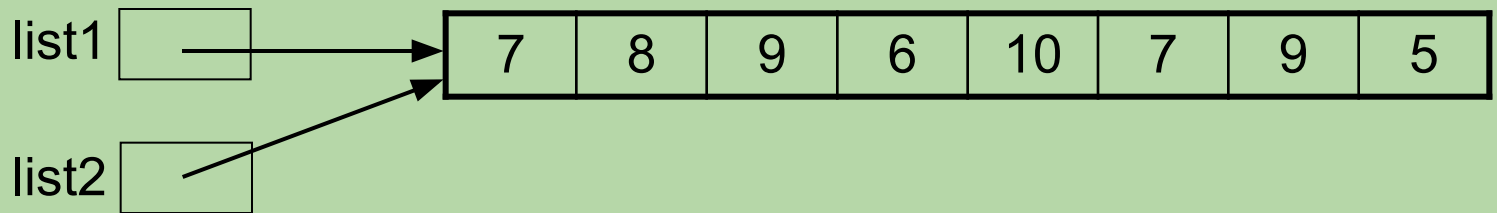
*after* `mystery6`



# Recall: Copying a List

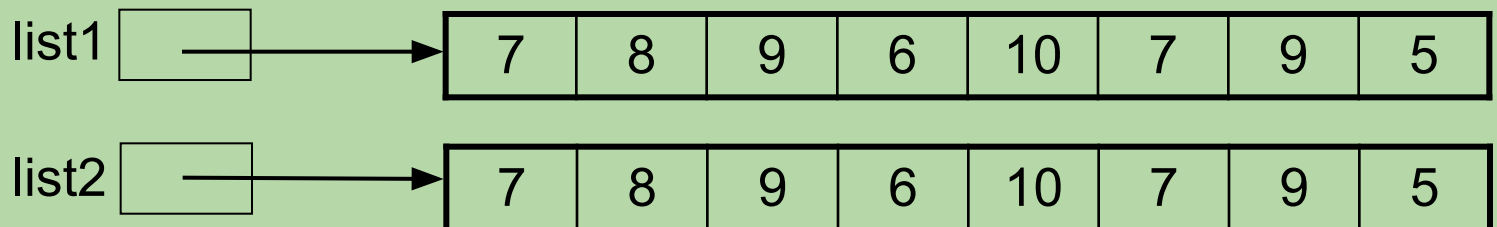
- We can't copy a list by a simple assignment:

```
list1 = [7, 8, 9, 6, 10, 7, 9, 5]  
list2 = list1
```



- We can copy this list using a full slice:

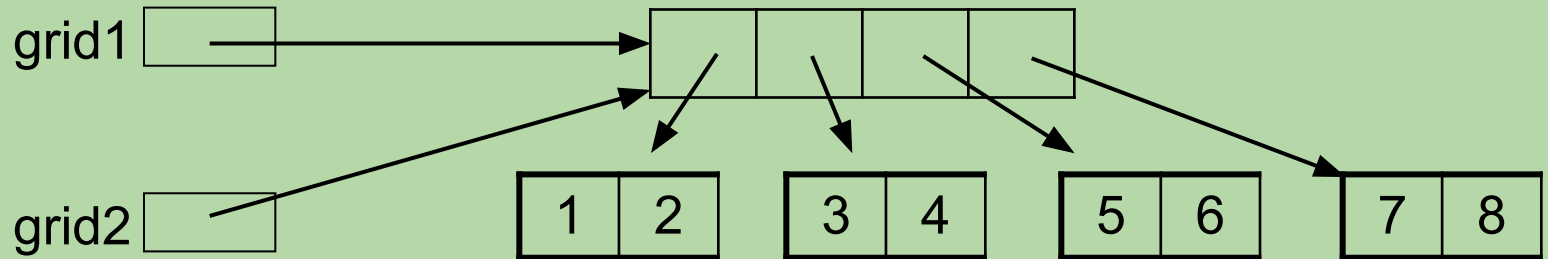
```
list1 = [7, 8, 9, 6, 10, 7, 9, 5]  
list2 = list1[:]
```



# Copying a 2-D List

```
grid1 = [[1, 2], [3, 4], [5, 6], [7, 8]]
```

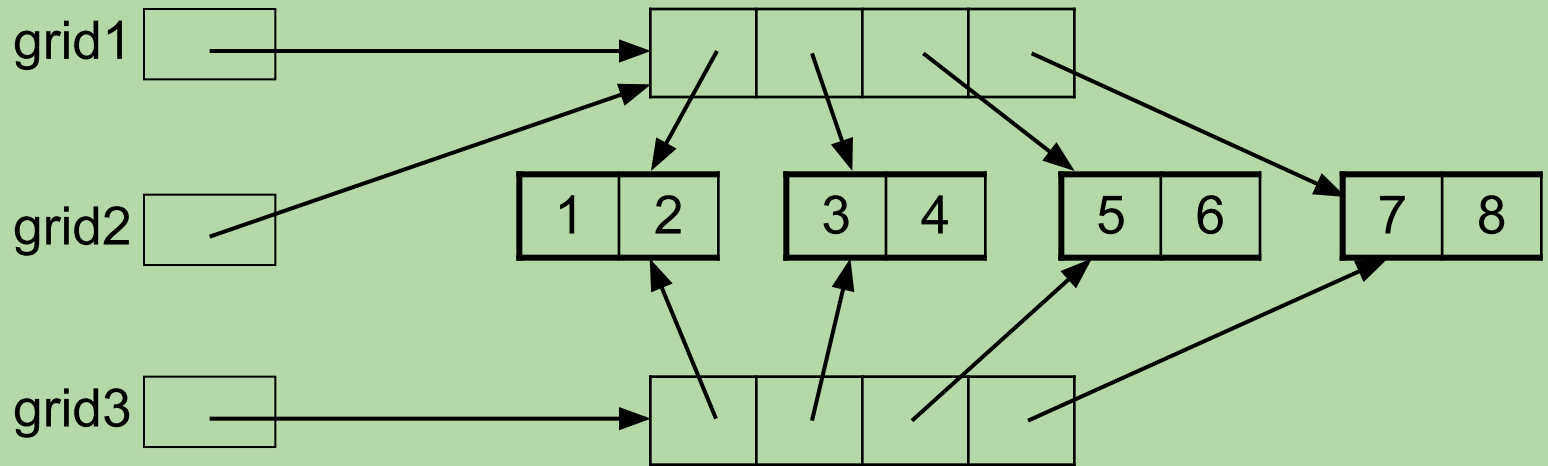
This doesn't copy a list: `grid2 = grid1`



- Does this? `grid3 = grid1[:]`

# Copying a 2-D List

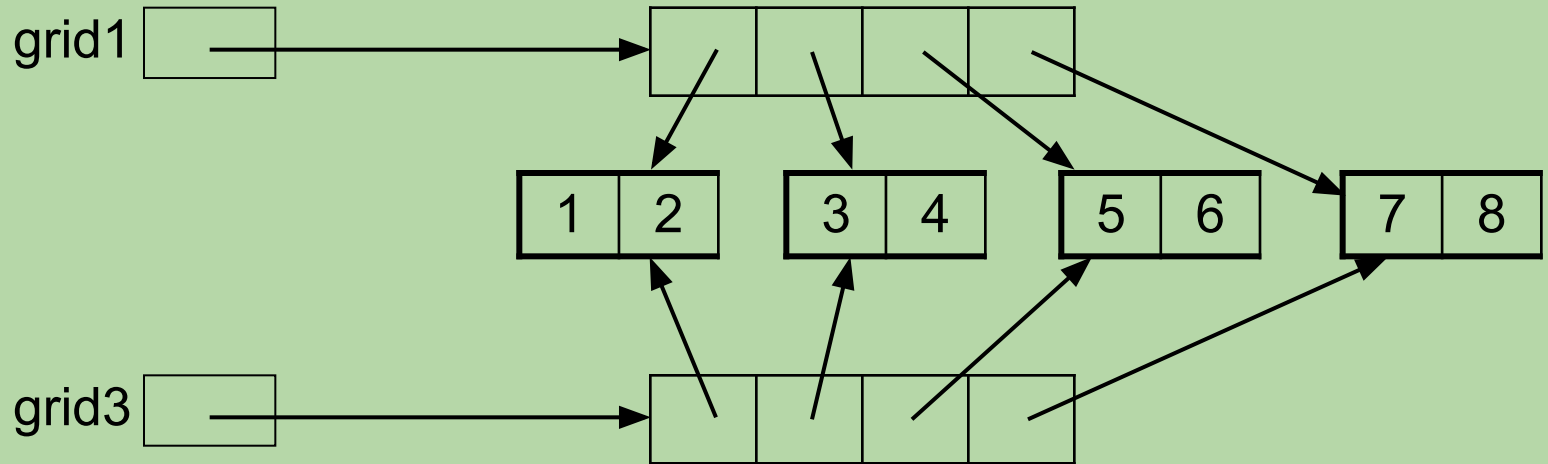
```
grid1 = [[1, 2], [3, 4], [5, 6], [7, 8]]
```



- Does this? `grid3 = grid1[:]` **not fully!**

# A Shallow Copy

```
grid1 = [[1, 2], [3, 4], [5, 6], [7, 8]]  
grid3 = grid1[:]
```



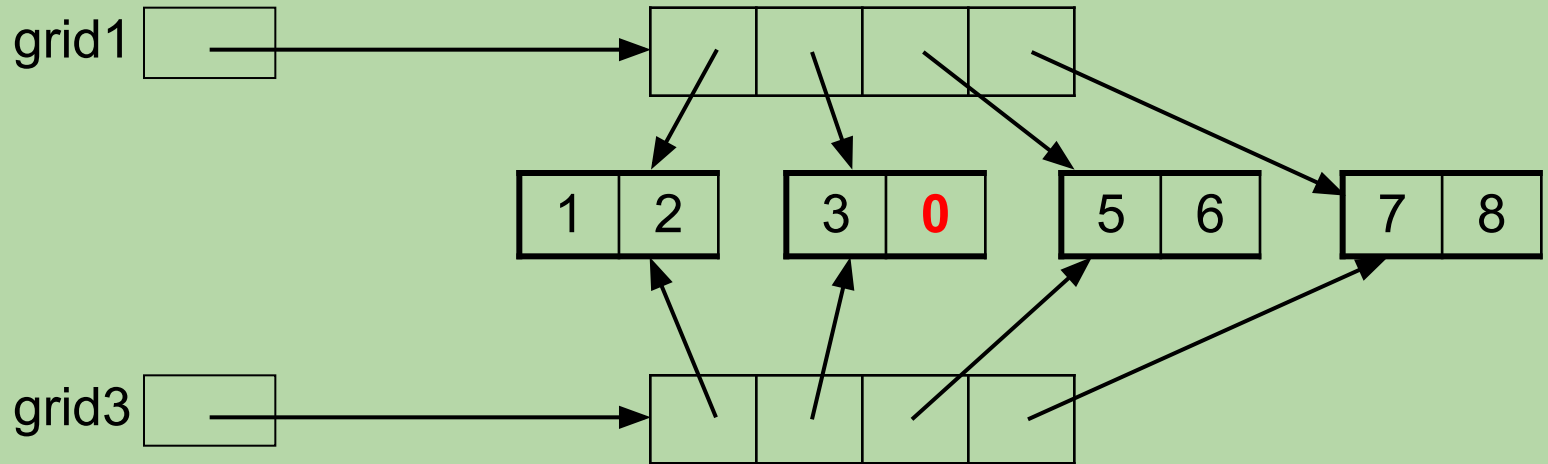
- grid1 and grid3 now share the same sublists.
  - known as a *shallow copy*

- What would this print?

```
grid1[1][1] = 0  
print(grid3)
```

# A Shallow Copy

```
grid1 = [[1, 2], [3, 4], [5, 6], [7, 8]]  
grid3 = grid1[:]
```



- grid1 and grid3 now share the same sublists.
  - known as a *shallow copy*

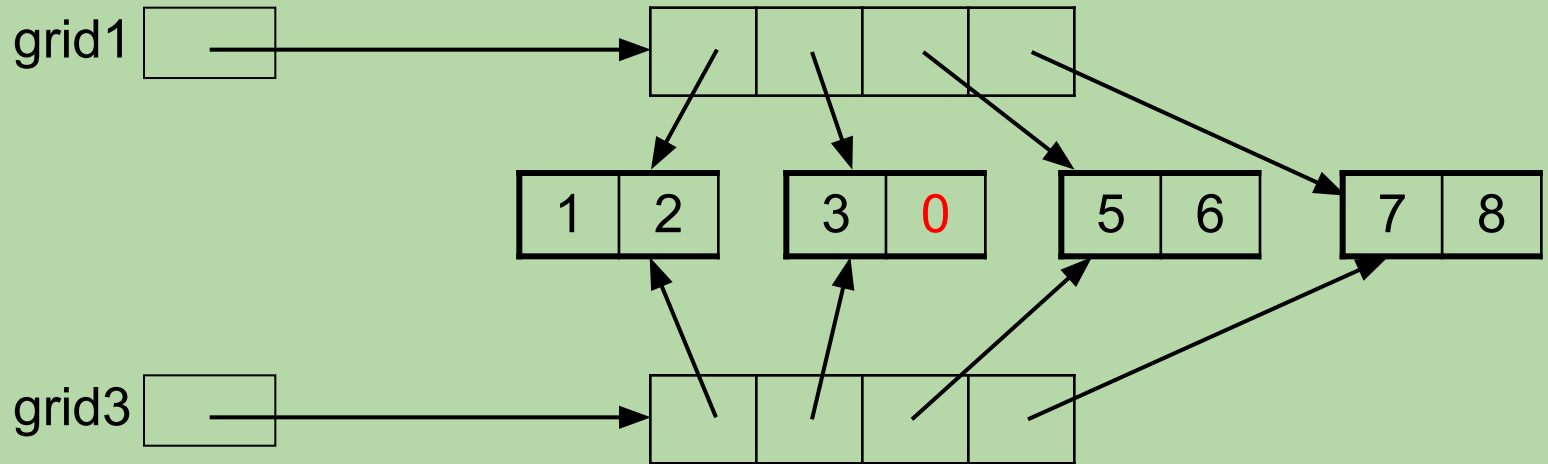
- What would this print?

```
grid1[1][1] = 0  
print(grid3)
```



# A Shallow Copy

```
grid1 = [[1, 2], [3, 4], [5, 6], [7, 8]]  
grid3 = grid1[:]
```



- grid1 and grid3 now share the same sublists.
  - known as a *shallow copy*

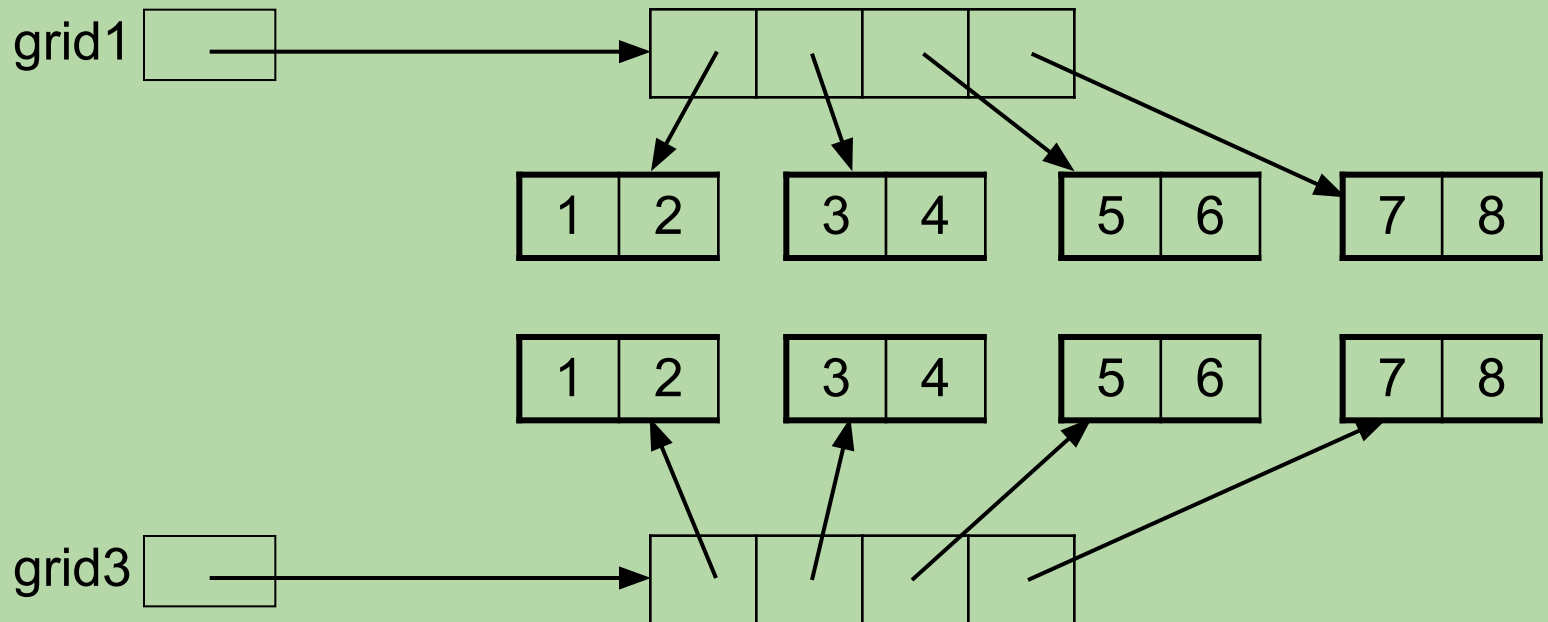
- What would this print?

```
grid1[1][1] = 0
```

```
print(grid3)    [[1, 2], [3, 0], [5, 6], [7, 8]]
```

# A *Deep* Copy: Nothing is Shared

```
grid1 = [[1, 2], [3, 4], [5, 6], [7, 8]]
```



- Here's one way to achieve this:

```
grid3 = []  
for sublist in grid1:  
    grid3 = grid3 + [sublist[:]]
```

In hw03,  
you'll take a  
different  
approach!

# Recall: List Multiplication

```
>>> vals = [1, 2] * 3
```

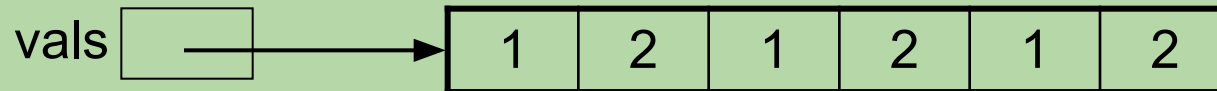
```
>>> vals
```

```
[1, 2, 1, 2, 1, 2]
```

- original list:



- get 3 copies of it, concatenated together:



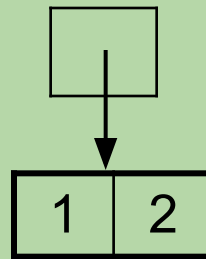
# List Multiplication of a 2-D List

```
>>> grid = [[1, 2]] * 3
```

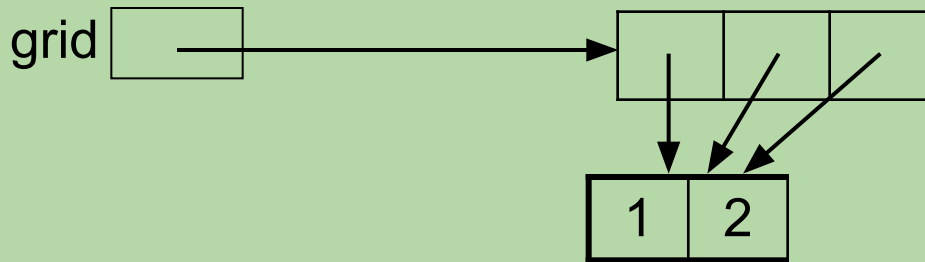
```
>>> grid
```

```
[[1, 2], [1, 2], [1, 2]]
```

- original list:



- get 3 copies of it concatenated together:



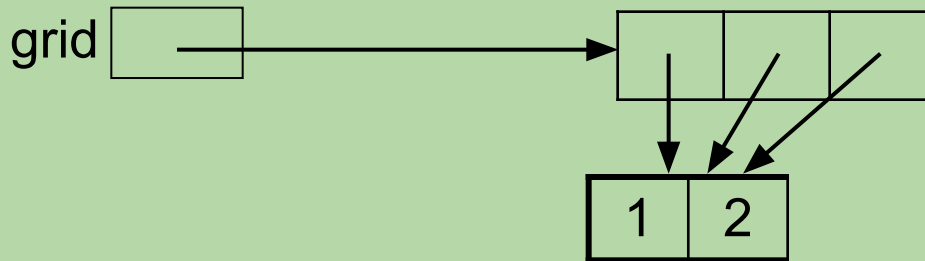
- the reference to the sublist is copied, not the sublist

# List Multiplication of a 2-D List (cont.)

```
>>> grid = [[1, 2]] * 3
```

```
>>> grid
```

```
[[1, 2], [1, 2], [1, 2]]
```



- What will this print?

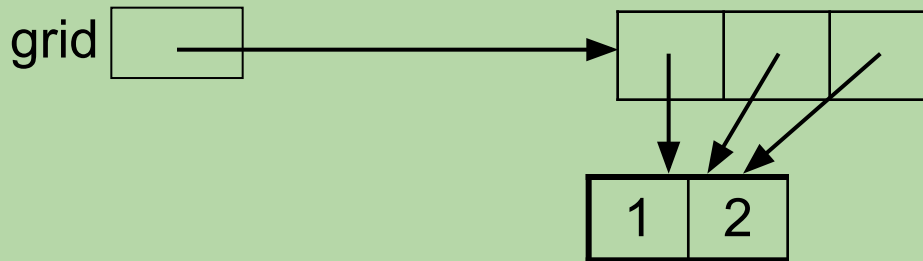
```
grid[1][1] = 5  
print(grid)
```

# List Multiplication of a 2-D List (cont.)

```
>>> grid = [[1, 2]] * 3
```

```
>>> grid
```

```
[[1, 2], [1, 2], [1, 2]]
```



- What will this print?

```
grid[1][1] = 5
```

```
print(grid)
```

```
# output: [[1, 5], [1, 5], [1, 5]]
```