

Lecture 10

Object Oriented Programming and Modeling Project



UTA Joseph's dog Ponyo with various objects. Very object oriented!

Classes: Defining New Types of Objects

Objects, Objects, Everywhere!

- *Recall:* Strings are objects with:

- *attributes* – data values inside the object
- *methods* – functions inside the object

string object for 'hello'

contents	'h'	'e'	'l'	'l'	'o'
length	5				
upper()	replace()				
lower()	split()				
find()	...				
count()					

- In fact, *everything* in Python is an object!
 - integers
 - floats
 - lists
 - booleans
 - file handles
 - functions
 - ...

Classes

- A *class* is a blueprint – a definition of a data type.
 - specifies the attributes and methods of that type
- Objects are built according to the blueprint provided by their class.
 - they are "values" aka *instances* of that type
 - use the type function to determine the class:

```
>>> type(111)
<class 'int'>
```

```
>>> type(3.14159)
<class 'float'>
```

```
>>> type('hello!')
<class 'str'>
```

```
>>> type([1, 2, 3])
<class 'list'>
```

Another Analogy

- A class is like a cookie cutter.
 - specifies the "shape" that all objects of that type should have

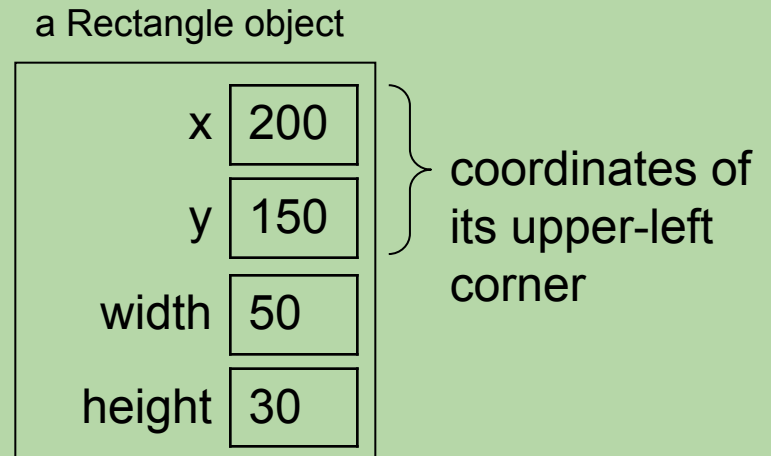
- Objects are like the cookies.
 - created with the "shape" specified by their class



Creating Your Own Classes

- In an *object-oriented* programming language, you can define your own classes.
 - your own types of objects
 - your own data types!

- Example: let's say that we want objects that represent rectangles.



- A Rectangle object could have methods for:
 - computing its area, perimeter, etc.
 - growing it (changing its dimensions), moving it, etc.

An Initial Rectangle Class

```
class Rectangle:
```

```
    """ a blueprint for objects that represent
        a rectangular shape
    """
```

```
    def __init__(self, init_width, init_height):
```

```
        """ the Rectangle constructor """
```

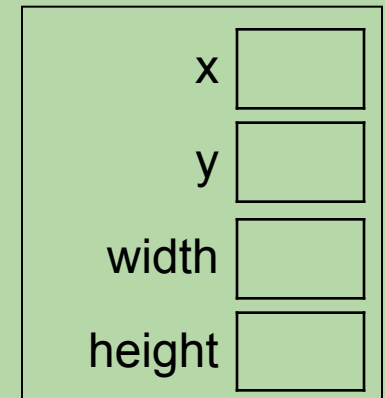
```
        self.x = 0
```

```
        self.y = 0
```

```
        self.width = init_width
```

```
        self.height = init_height
```

- `__init__` is the **constructor**.
 - it's used to create new objects
 - it specifies the attributes



- Inside its methods, an object refers to itself as `self`!

Constructing and Using an Object

```
class Rectangle:
    """ the Rectangle constructor """
    def __init__(self, init_width, init_height):
        self.x = 0
        self.y = 0
        self.width = init_width
        self.height = init_height
```

```
>>> r1 = Rectangle(100, 50)    # calls __init__!
```


Constructing and Using an Object

```
class Rectangle:  
    """ the Rectangle constructor """  
    def __init__(self, init_width, init_height):  
        self.x = 0  
        self.y = 0  
        self.width = init_width  
        self.height = init_height
```

```
>>> r1 = Rectangle(100, 50)    # calls __init__!
```



Constructing and Using an Object

```
class Rectangle:  
    """ the Rectangle constructor """  
    def __init__(self, init_width, init_height):  
        self.x = 0  
        self.y = 0  
        self.width = init_width  
        self.height = init_height
```

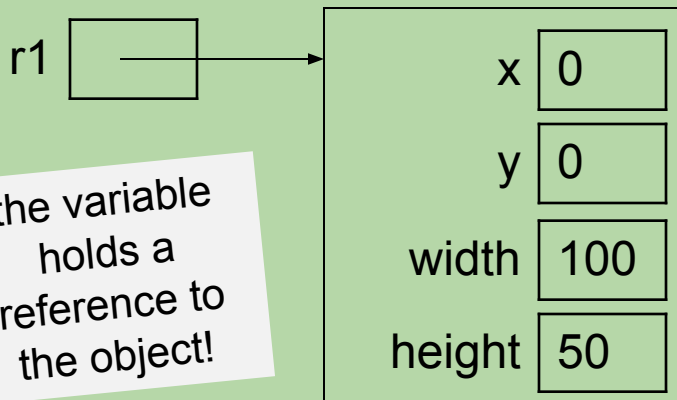
```
>>> r1 = Rectangle(100, 50) # calls __init__!
```

x	0
y	0
width	100
height	50

Constructing and Using an Object

```
class Rectangle:
    """ the Rectangle constructor """
    def __init__(self, init_width, init_height):
        self.x = 0
        self.y = 0
        self.width = init_width
        self.height = init_height
```

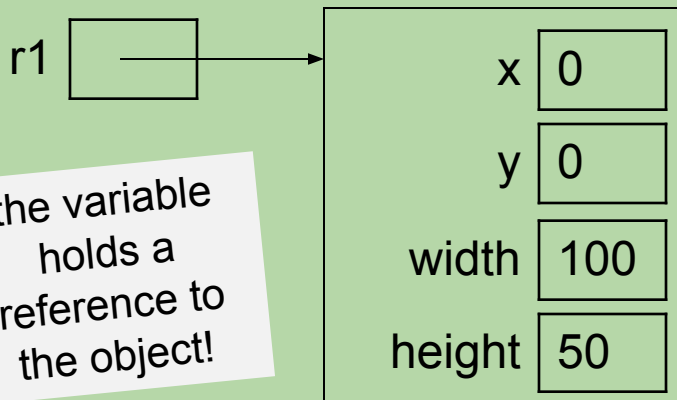
```
>>> r1 = Rectangle(100, 50)    # calls __init__!
```



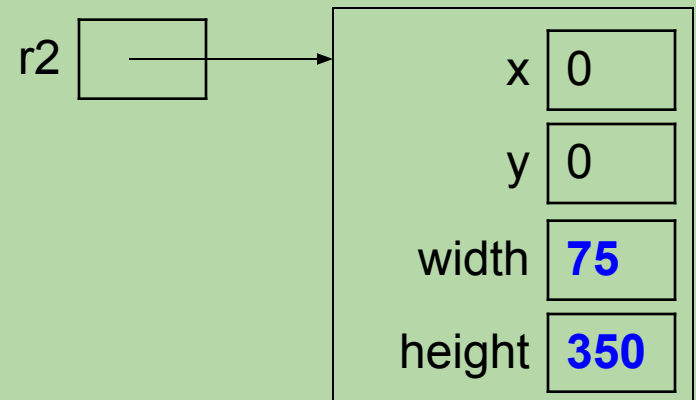
Constructing and Using an Object

```
class Rectangle:
    """ the Rectangle constructor """
    def __init__(self, init_width, init_height):
        self.x = 0
        self.y = 0
        self.width = init_width
        self.height = init_height
```

```
>>> r1 = Rectangle(100, 50)      # calls __init__!
>>> r2 = Rectangle(75, 350)    # construct another one!
```

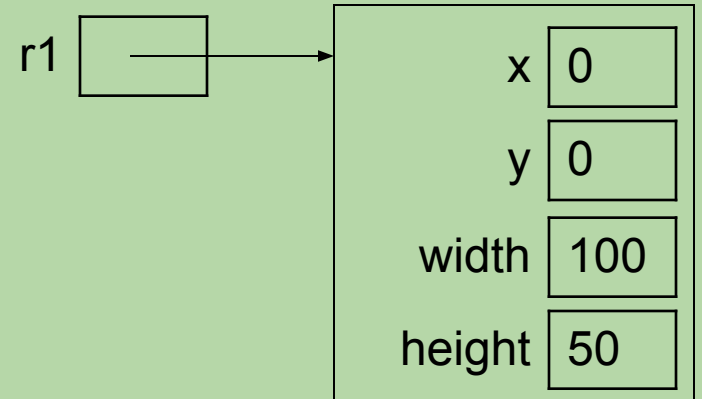


the variable
holds a
reference to
the object!



Accessing and Modifying an Object's Attributes

```
>>> r1 = Rectangle(100, 50)
```



- Access the attributes using *dot notation*:

```
>>> r1.width  
100
```

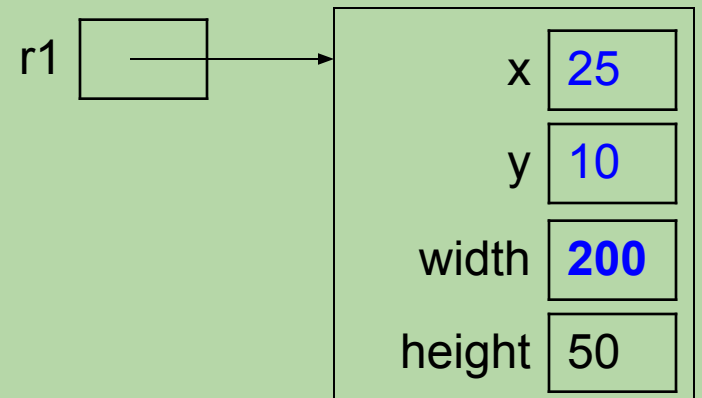
```
>>> r1.height  
50
```

- Modify them as you would any other variable:

```
>>> r1.x = 25
```

```
>>> r1.y = 10
```

```
>>> r1.width *= 2
```



Application Programs

- Our Rectangle class is *not* a program.
- Instead, it will be used by code defined elsewhere.
 - referred to as ***Application programs*** or ***Application code***
 - referred to as ***Client programs*** or ***Client code***
- More generally, when we define a new type of object, we create a building block that can be used in other code.
 - just like the objects from the built-in classes:
str, list, int, etc.
 - our programs have been *applications* that use those classes!
 - our programs have been *clients* of those classes!

Initial Application Program

```
# construct two Rectangle objects
r1 = Rectangle(100, 50)
r2 = Rectangle(75, 350)
```

```
# print dimensions and area of each
print('r1:', r1.width, 'x', r1.height)
area1 = r1.width * r1.height
print('area =', area1)
```

```
print('r2:', r2.width, 'x', r2.height)
area2 = r2.width * r2.height
print('area =', area2)
```

```
# grow both Rectangles
r1.width += 50
r1.height += 10
r2.width += 5
r2.height += 30
```

```
# print new dimensions
print('r1:', r1.width, 'x', r1.height)
print('r2:', r2.width, 'x', r2.height)
```

Using Methods to Capture an Object's Behavior

- Rather than having the Application grow the Rectangle objects, we'd like to give each Rectangle object the ability to grow itself.
- We do so by adding a method to the class:

```
class Rectangle:
```

```
    """ the Rectangle constructor """
```

```
    def __init__(self, init_width, init_height):
```

```
        self.x = 0
```

```
        self.y = 0
```

```
        self.width = init_width
```

```
        self.height = init_height
```

```
    def grow(self, dwidth, dheight):
```

```
        self.width += dwidth
```

```
        self.height += dheight
```

note that the first “parameter” for a class method is always ‘self’

when we call this method, the self parameter is implicit:
r.grow(dwidth, dheight)

Calling a Method

```
class Rectangle:
```

```
...
```

```
def grow(self, dwidth, dheight):
```

```
    self.width += dwidth
```

```
    self.height += dheight
```

```
>>> r1 = Rectangle(100, 50)
```

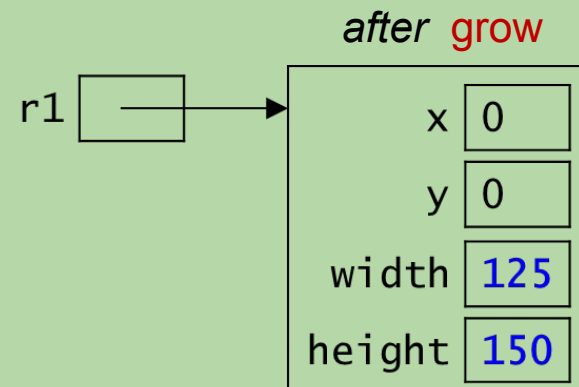
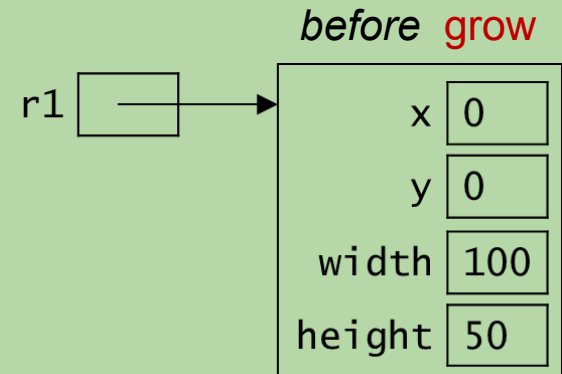
```
>>> r1.grow(25, 100)
```

```
>>> r1.width
```

```
125
```

```
>>> r1.height
```

```
150
```



Another Example of a Method

- Here's a method for getting the area of a Rectangle:

```
def area(self):  
    return self.width * self.height
```

- Sample method calls:

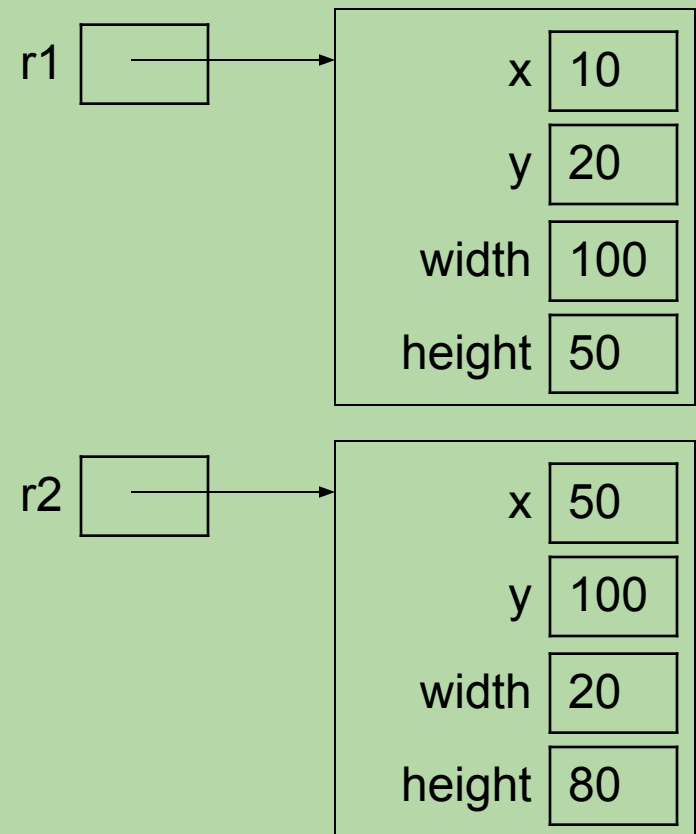
```
>>> r1.area()
```

```
5000
```

```
>>> r2.area()
```

```
1600
```

- we're asking r1 and r2 to give us their areas
- nothing in the parentheses because the necessary info. is in the objects' attributes!



Second Version of our Rectangle Class

assume this is in rectangle.py

```
class Rectangle:
    """ a blueprint for objects that represent
        a rectangular shape
    """
    def __init__(self, init_width, init_height):
        """ the Rectangle constructor """
        self.x = 0
        self.y = 0
        self.width = init_width
        self.height = init_height

    def grow(self, dwidth, dheight):
        self.width += dwidth
        self.height += dheight

    def area(self):
        return self.width * self.height
```

Original Application Program...

```
from rectangle import *

# construct two Rectangle objects
r1 = Rectangle(100, 50)
r2 = Rectangle(75, 350)

# print dimensions and area of each
print('r1:', r1.width, 'x', r1.height)
area1 = r1.width * r1.height
print('area =', area1)

print('r2:', r2.width, 'x', r2.height)
area2 = r2.width * r2.height
print('area =', area2)

# grow both Rectangles
r1.width += 50
r1.height += 10
r2.width += 5
r2.height += 30

# print new dimensions
print('r1:', r1.width, 'x', r1.height)
print('r2:', r2.width, 'x', r2.height)
```

Simplified Application Program

```
from rectangle import *  
  
# construct two Rectangle objects  
r1 = Rectangle(100, 50)  
r2 = Rectangle(75, 350)  
  
# print dimensions and area of each  
print('r1:', r1.width, 'x', r1.height)  
print('area =', r1.area())  
  
print('r2:', r2.width, 'x', r2.height)  
print('area =', r2.area())  
  
# grow both Rectangles  
r1.grow(50, 10)  
r2.grow(5, 30)  
  
# print new dimensions  
print('r1:', r1.width, 'x', r1.height)  
print('r2:', r2.width, 'x', r2.height)
```

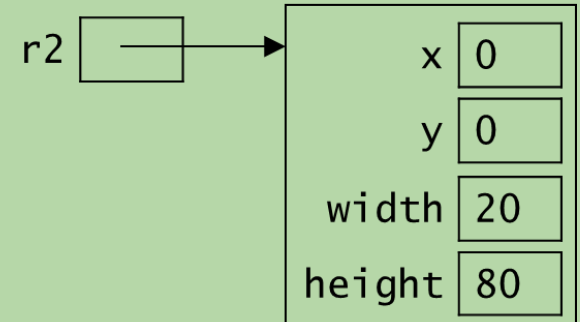
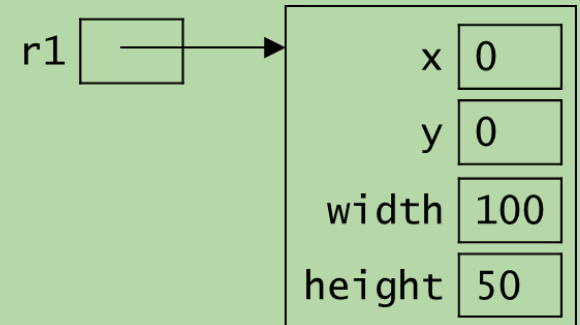
Be Objective!

```
class Rectangle:  
    ...  
    def grow(self, dwidth, dheight):  
        ...  
    def area(self):  
        ...
```

```
r1 = Rectangle(100, 50)
```

```
r2 = Rectangle(20, 80)
```

- Give an expression for:
 - the width of r1:
 - the height of r2:
- Write an assignment that changes r1's x-coordinate to 50:
- Write a method call that:
 - increases r2's width by 5 and height by 10:
 - gets r1's area:

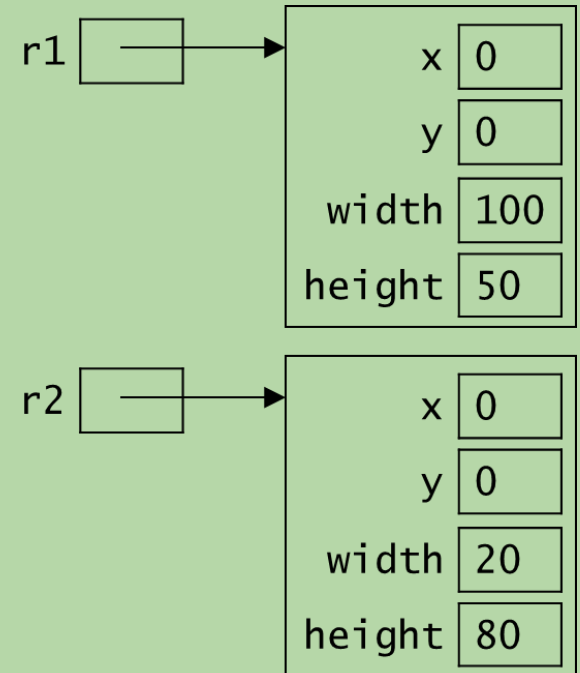


Be Objective!

```
class Rectangle:
    ...
    def grow(self, dwidth, dheight):
        ...
    def area(self):
        ...
```

```
r1 = Rectangle(100, 50)
r2 = Rectangle(20, 80)
```

- Give an expression for:
 - the width of r1: `r1.width`
 - the height of r2: `r2.height`
- Write an assignment that changes r1's x-coordinate to 50:
`r1.x = 50`
- Write a method call that:
 - increases r2's width by 5 and height by 10: `r2.grow(5, 10)`
 - gets r1's area: `r1.area()`



Method vs. Function

- Our area *method* is part of the Rectangle class:

```
class Rectangle:
```

```
    ...  
    def area(self):    # methods have a self  
        return self.width * self.height
```

- thus, it is inside Rectangle objects
- sample call:

```
r.area()
```

- Here's a *function* that takes two Rectangle objects as inputs:

```
def total_area(r1, r2): # functions don't  
    return r1.area() + r2.area()
```

- it is *not* part of the class and is *not* inside Rectangle objects
- sample call:

```
total_area(r, other_r)
```

- it is a client of the Rectangle class!

Methods That Modify an Object

```
class Rectangle:
    """ a blueprint for objects that represent
        a rectangular shape
    """
    def __init__(self, init_width, init_height):
        """ the Rectangle constructor """
        self.x = 0
        self.y = 0
        self.width = init_width
        self.height = init_height

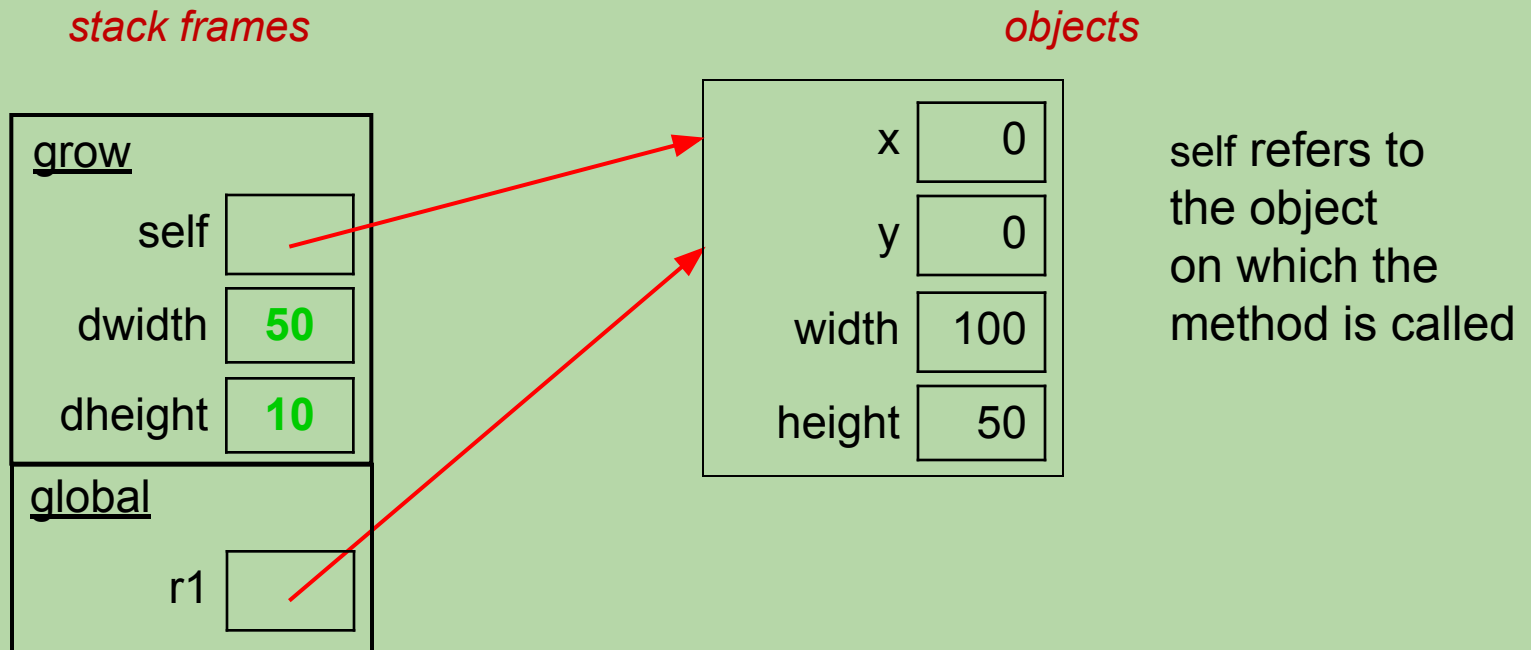
    def grow(self, dwidth, dheight):
        self.width += dwidth
        self.height += dheight
        # why don't we need a return?

    def area(self):
        return self.width * self.height
```

Methods That Modify an Object

```
r1 = Rectangle(100, 50)
r1.grow(50, 10)
print('r1:', r1.width, 'x', r1.height)
```

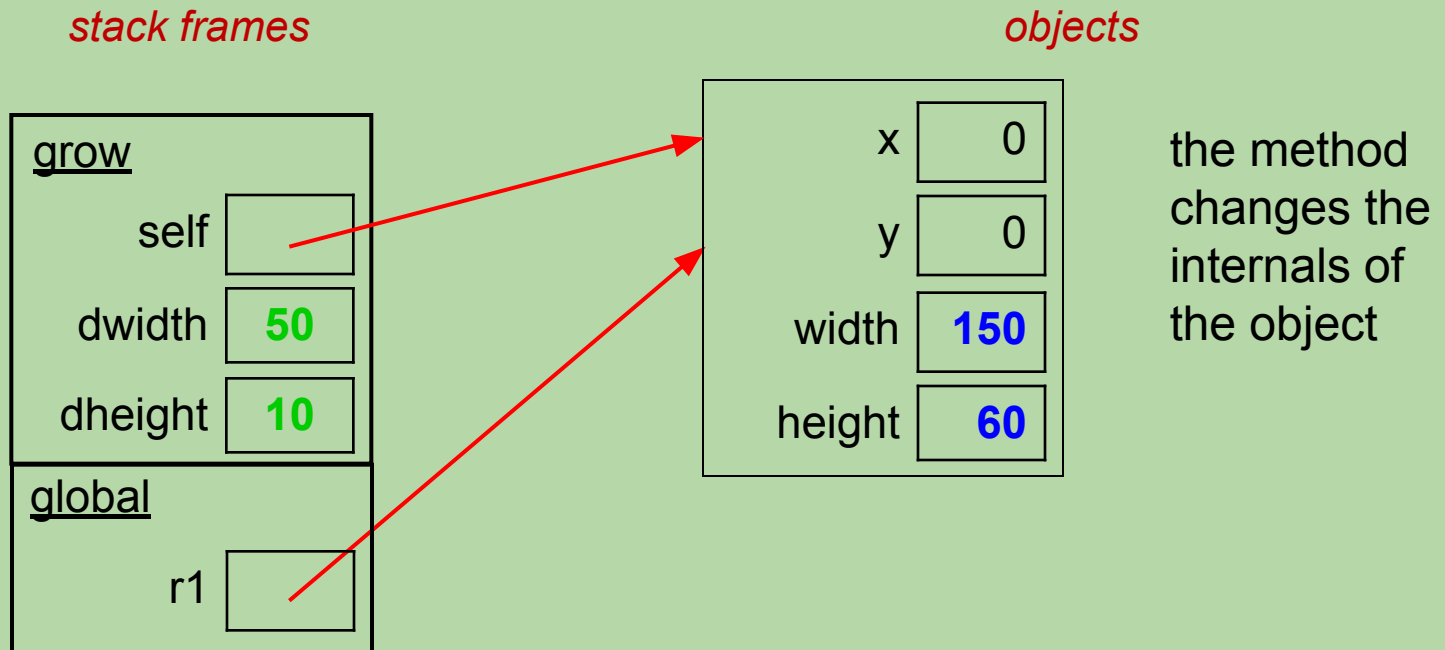
```
def grow(self, dwidth, dheight):
    self.width += dwidth
    self.height += dheight
```



Methods That Modify an Object

```
r1 = Rectangle(100, 50)
r1.grow(50, 10)
print('r1:', r1.width, 'x', r1.height)
```

```
def grow(self, dwidth, dheight):
    self.width += dwidth
    self.height += dheight
```



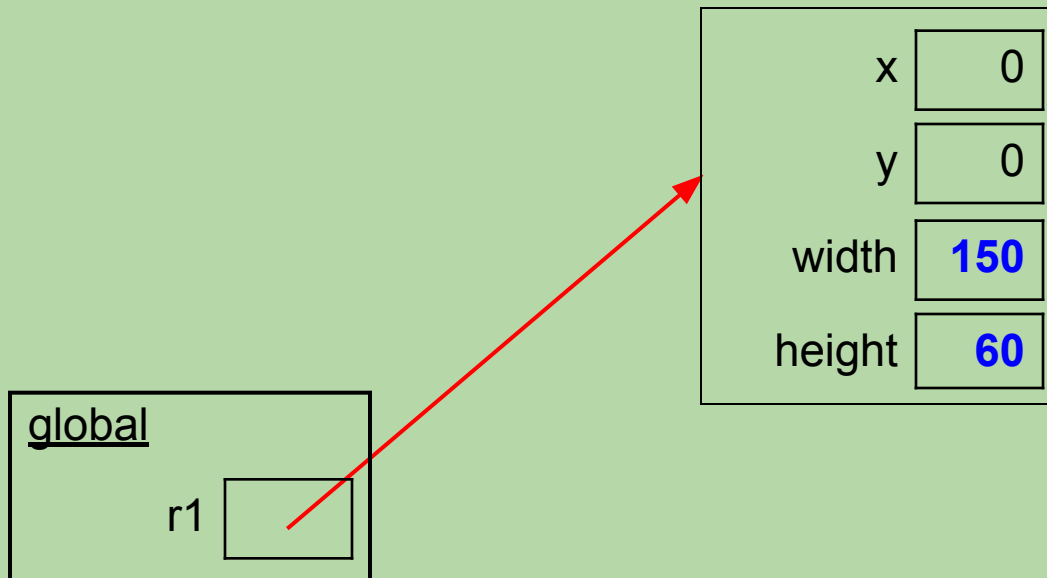
Methods That Modify an Object

```
r1 = Rectangle(100, 50)
r1.grow(50, 10)
print('r1:', r1.width, 'x', r1.height)
```

```
def grow(self, dwidth, dheight):
    self.width += dwidth
    self.height += dheight
```

stack frames

objects



those changes
are still there
after the
method returns

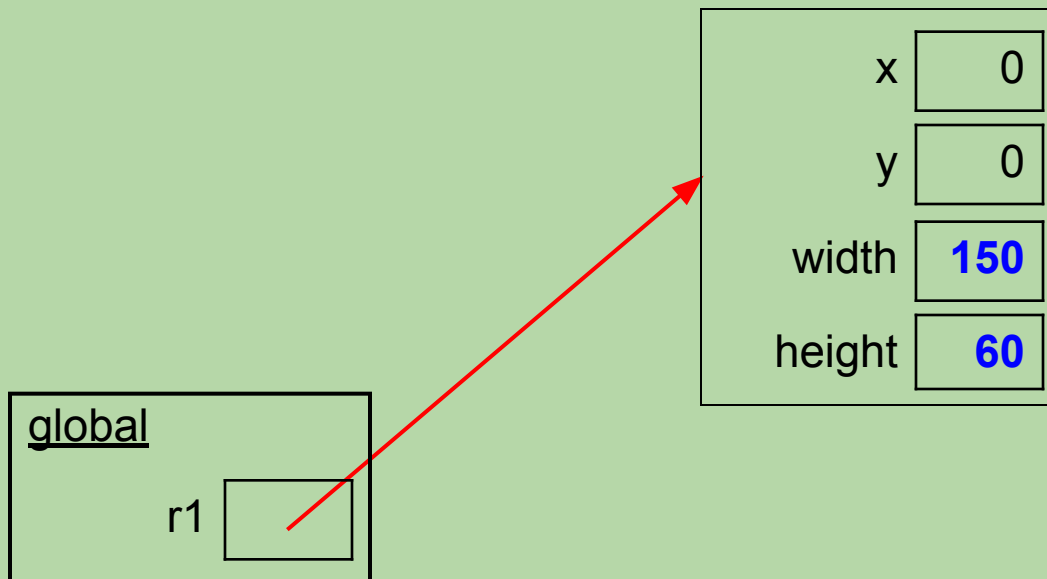
Methods That Modify an Object

```
r1 = Rectangle(100, 50)
r1.grow(50, 10)
print('r1:', r1.width, 'x', r1.height)
```

output: r1: 150 x 60

stack frames

objects



Which of these is a correct perimeter method?

A.

```
def perimeter(self, width, height):  
    return 2*width + 2*height
```

B.

```
def perimeter():  
    return 2*self.width + 2*self.height
```

C.

```
def perimeter(self):  
    return 2*self.width + 2*self.height
```

D. more than one of these

E. none of these

Which of these is a correct perimeter method?

A. `def perimeter(self, width, height):
 return 2*width + 2*height`

B. `def perimeter():
 return 2*self.width + 2*self.height`

C. `def perimeter(self):
 return 2*self.width + 2*self.height`

D. more than one of these

E. none of these

Fill in the blank to call the perimeter method.

```
class Rectangle:  
    ...  
    def perimeter(self):  
        return 2*self.width + 2*self.height
```

r = Rectangle(35, 20)

perim = _____

- A. perimeter(r)
- B. perimeter(self, r)
- C. perimeter(self, 35, 20)
- D. r.perimeter(35, 20)
- E. r.perimeter()

Fill in the blank to call the perimeter method.

```
class Rectangle:  
    ...  
    def perimeter(self):  
        return 2*self.width + 2*self.height
```

```
r = Rectangle(35, 20)
```

```
perim = r.perimeter()
```

- A. perimeter(r)
- B. perimeter(self, r)
- C. perimeter(self, 35, 20)
- D. r.perimeter(35, 20)
- E. **r.perimeter()**

scale Method

```
class Rectangle:  
    ...  
    def perimeter(self):  
        return 2*self.width + 2*self.height  
  
    def scale(_____):
```

Write a method called `scale` that will scale the dimensions of a `Rectangle` by a specified factor.

sample call:
`r.scale(5)`

scale Method

```
class Rectangle:  
    ...  
    def perimeter(self):  
        return 2*self.width + 2*self.height  
  
    def scale(self, factor):  
        self.width *= factor  
        self.height *= factor
```

scale Method

```
class Rectangle:  
    ...  
    def perimeter(self):  
        return 2*self.width + 2*self.height  
  
    def scale(self, factor):  
        self.width *= factor  
        self.height *= factor
```

```
r = Rectangle(35, 20)  
perim = r.perimeter()
```

How would we triple the dimensions of r?

scale Method

```
class Rectangle:  
    ...  
    def perimeter(self):  
        return 2*self.width + 2*self.height  
  
    def scale(self, factor):  
        self.width *= factor  
        self.height *= factor
```

```
r = Rectangle(35, 20)  
perim = r.perimeter()
```

```
# How would we triple the dimensions of r?  
r.scale(3)
```

Why doesn't scale need to return anything?

Memory Diagrams for Method Calls

```
# Rectangle Application code
```

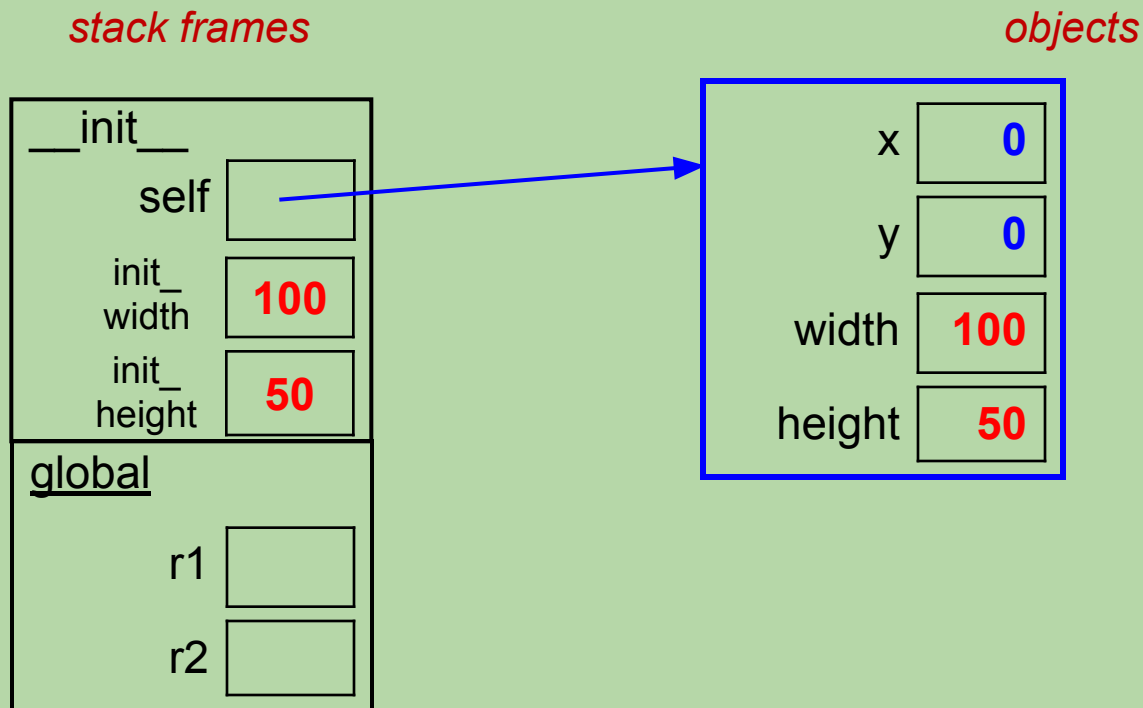
```
r1 = Rectangle(100, 50)
```

```
r2 = Rectangle(20, 80)
```

```
r1.scale(5)
```

```
r2.scale(3)
```

```
print(r1.width, r1.height, r2.width, r2.height)
```



Memory Diagrams for Method Calls

```
# Rectangle Application code
```

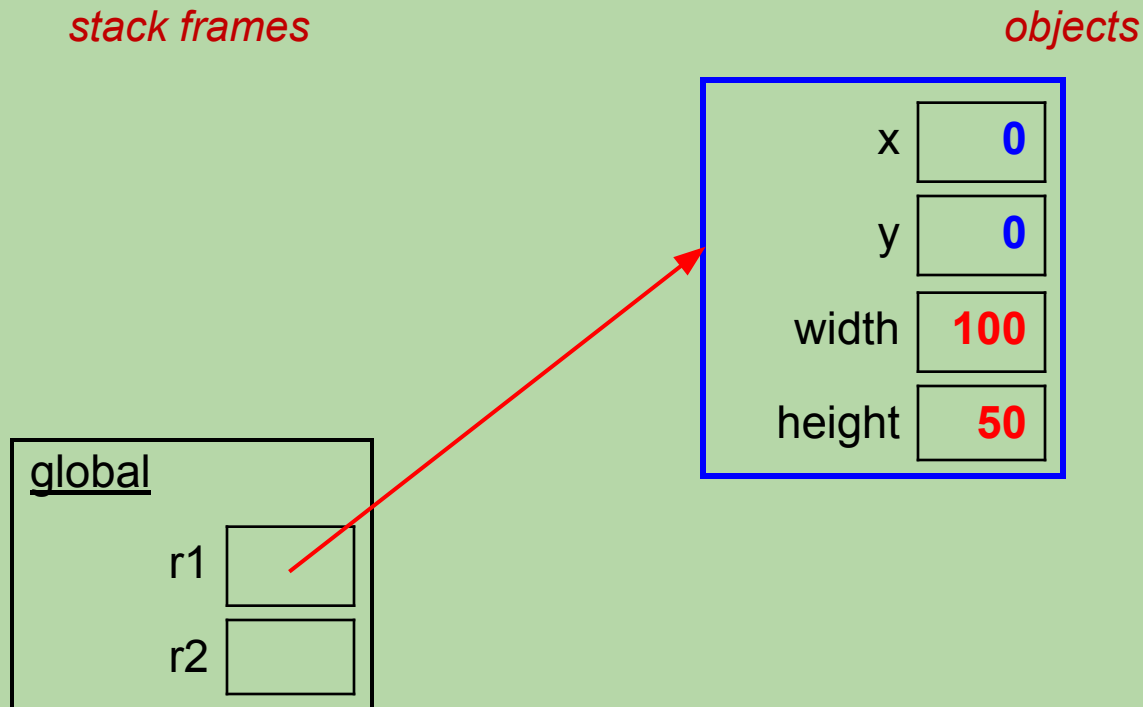
```
r1 = Rectangle(100, 50)
```

```
r2 = Rectangle(20, 80)
```

```
r1.scale(5)
```

```
r2.scale(3)
```

```
print(r1.width, r1.height, r2.width, r2.height)
```



Memory Diagrams for Method Calls

```
# Rectangle Application code
```

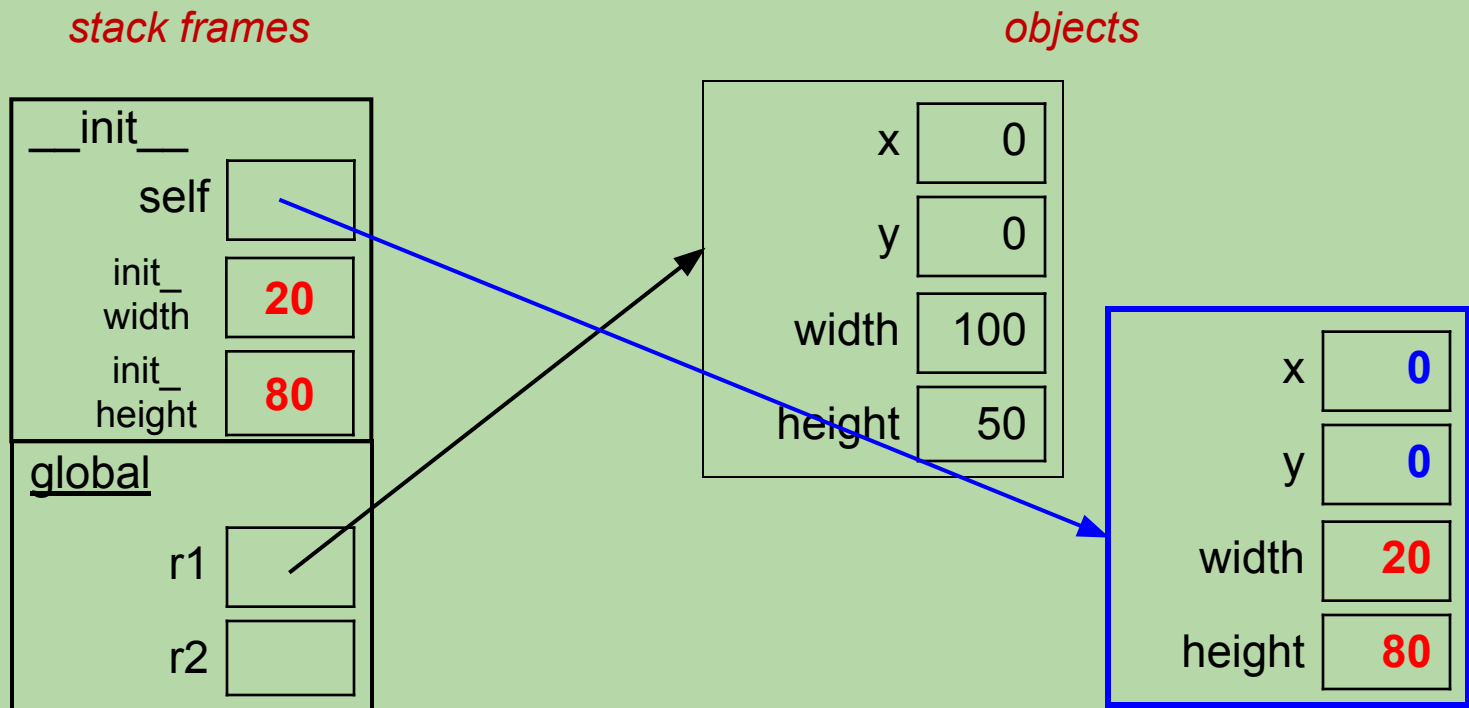
```
r1 = Rectangle(100, 50)
```

```
r2 = Rectangle(20, 80)
```

```
r1.scale(5)
```

```
r2.scale(3)
```

```
print(r1.width, r1.height, r2.width, r2.height)
```



Memory Diagrams for Method Calls

```
# Rectangle Application code
```

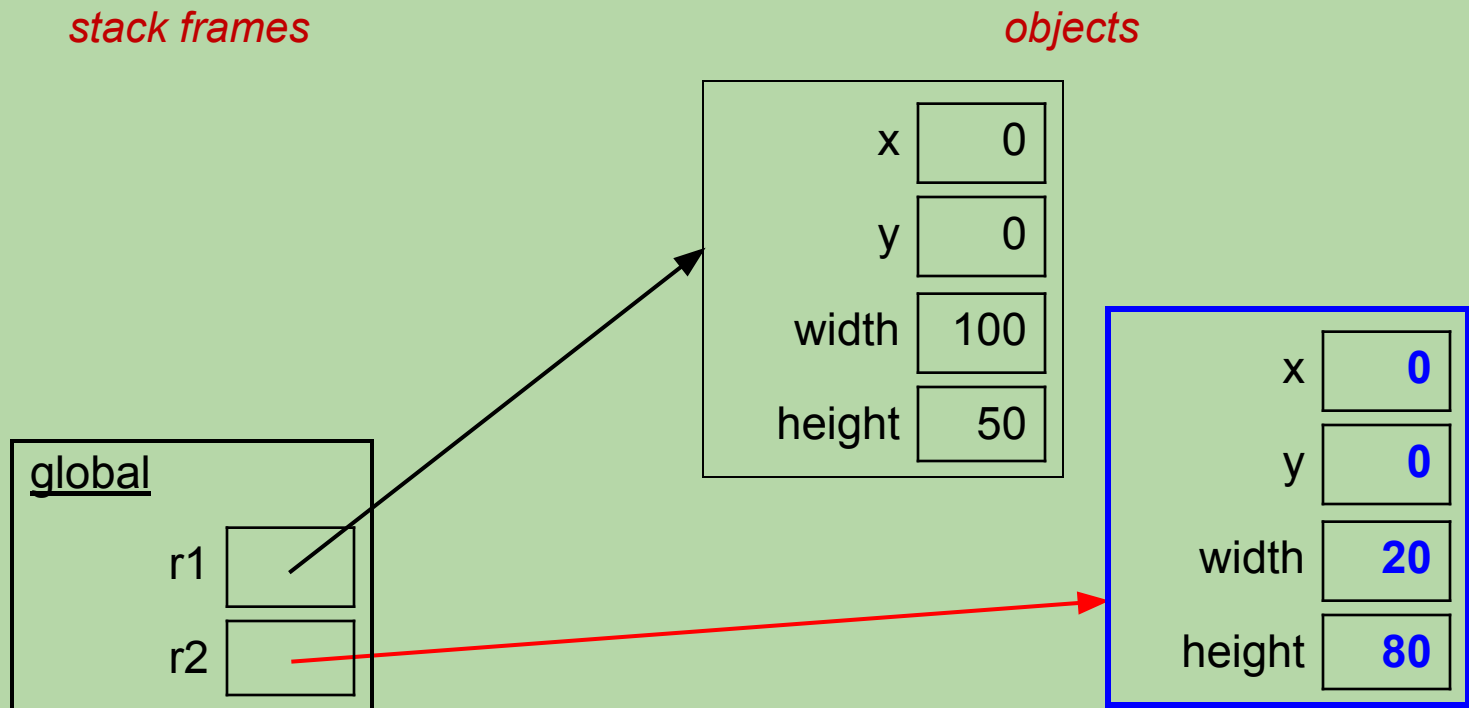
```
r1 = Rectangle(100, 50)
```

```
r2 = Rectangle(20, 80)
```

```
r1.scale(5)
```

```
r2.scale(3)
```

```
print(r1.width, r1.height, r2.width, r2.height)
```



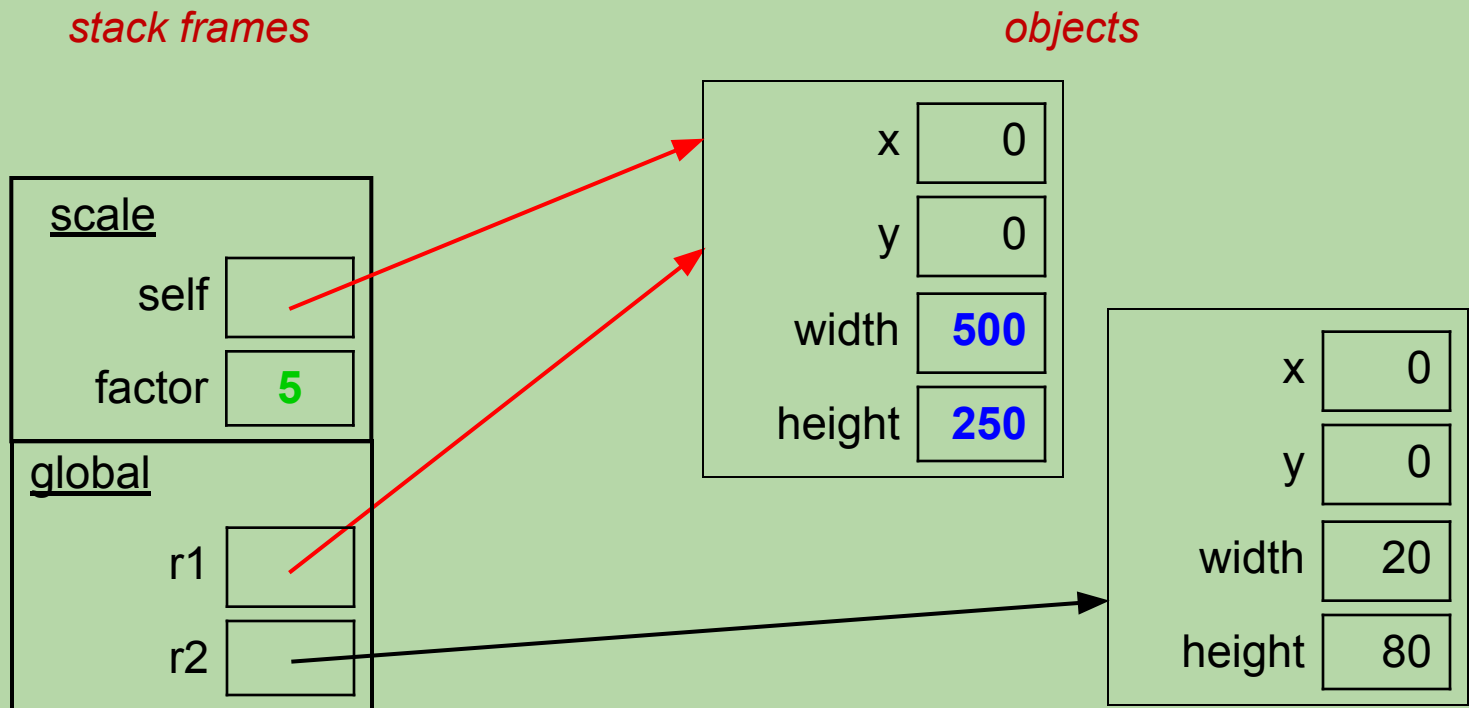
Memory Diagrams for Method Calls

```
# Rectangle Application code  
r1 = Rectangle(100, 50)  
r2 = Rectangle(20, 80)
```

```
r1.scale(5)
```

```
r2.scale(3)
```

```
print(r1.width, r1.height, r2.width, r2.height)
```



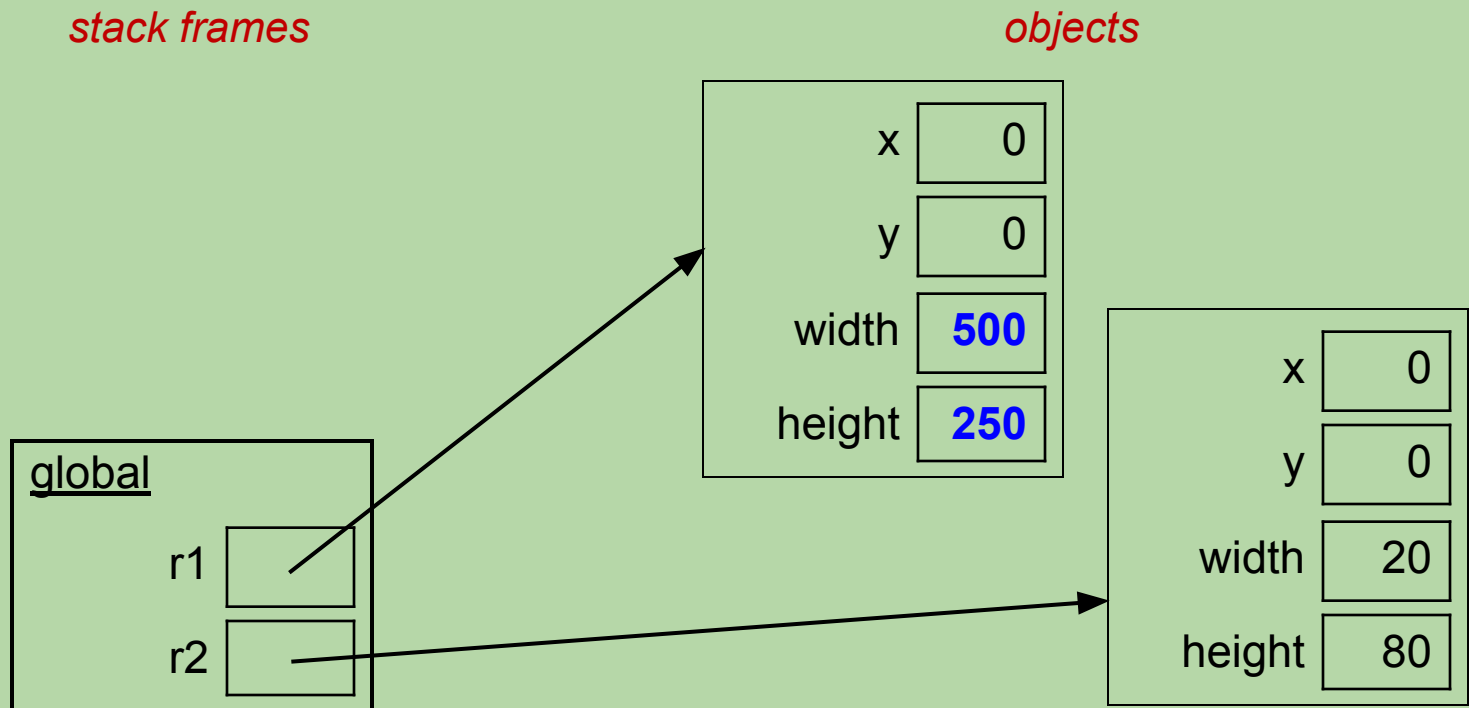
Memory Diagrams for Method Calls

```
# Rectangle Application code  
r1 = Rectangle(100, 50)  
r2 = Rectangle(20, 80)
```

```
r1.scale(5)
```

```
r2.scale(3)
```

```
print(r1.width, r1.height, r2.width, r2.height)
```



Memory Diagrams for Method Calls

```
# Rectangle Application code
```

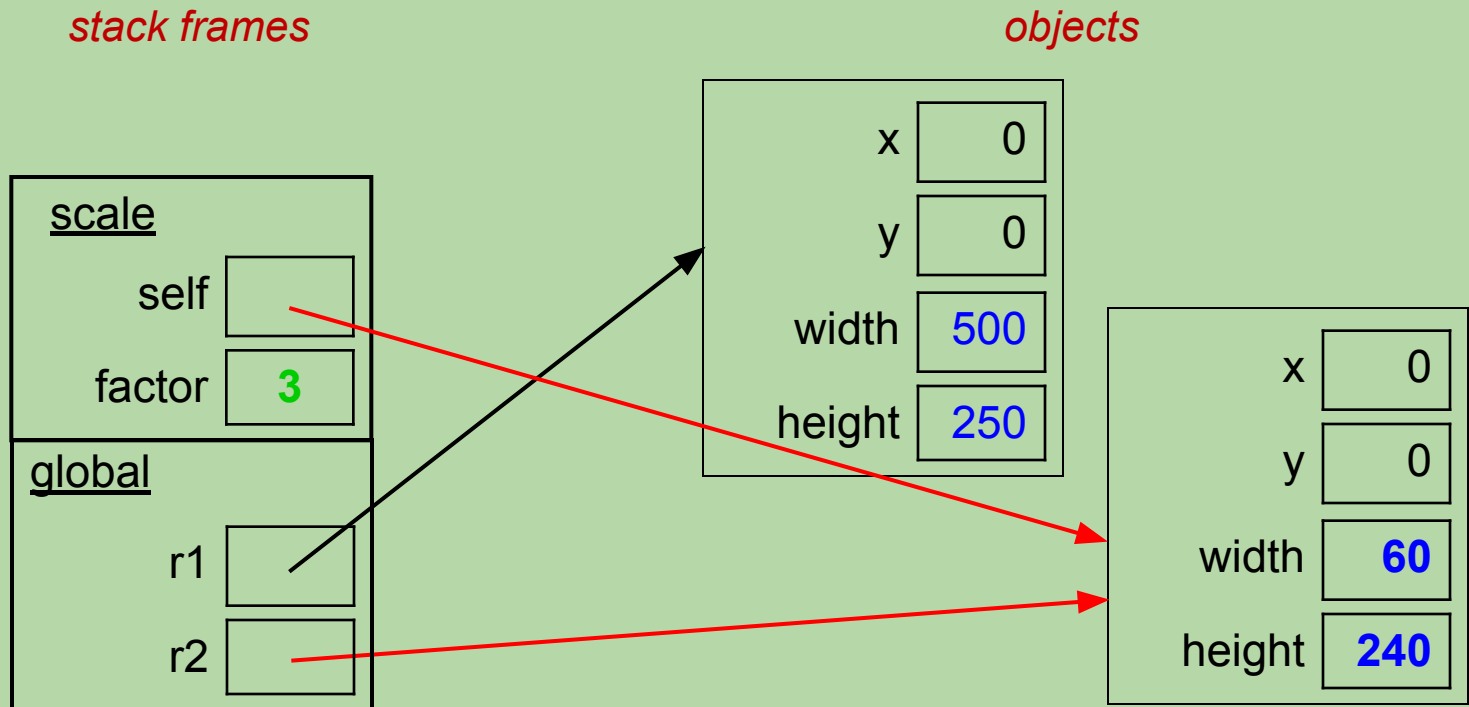
```
r1 = Rectangle(100, 50)
```

```
r2 = Rectangle(20, 80)
```

```
r1.scale(5)
```

```
r2.scale(3)
```

```
print(r1.width, r1.height, r2.width, r2.height)
```



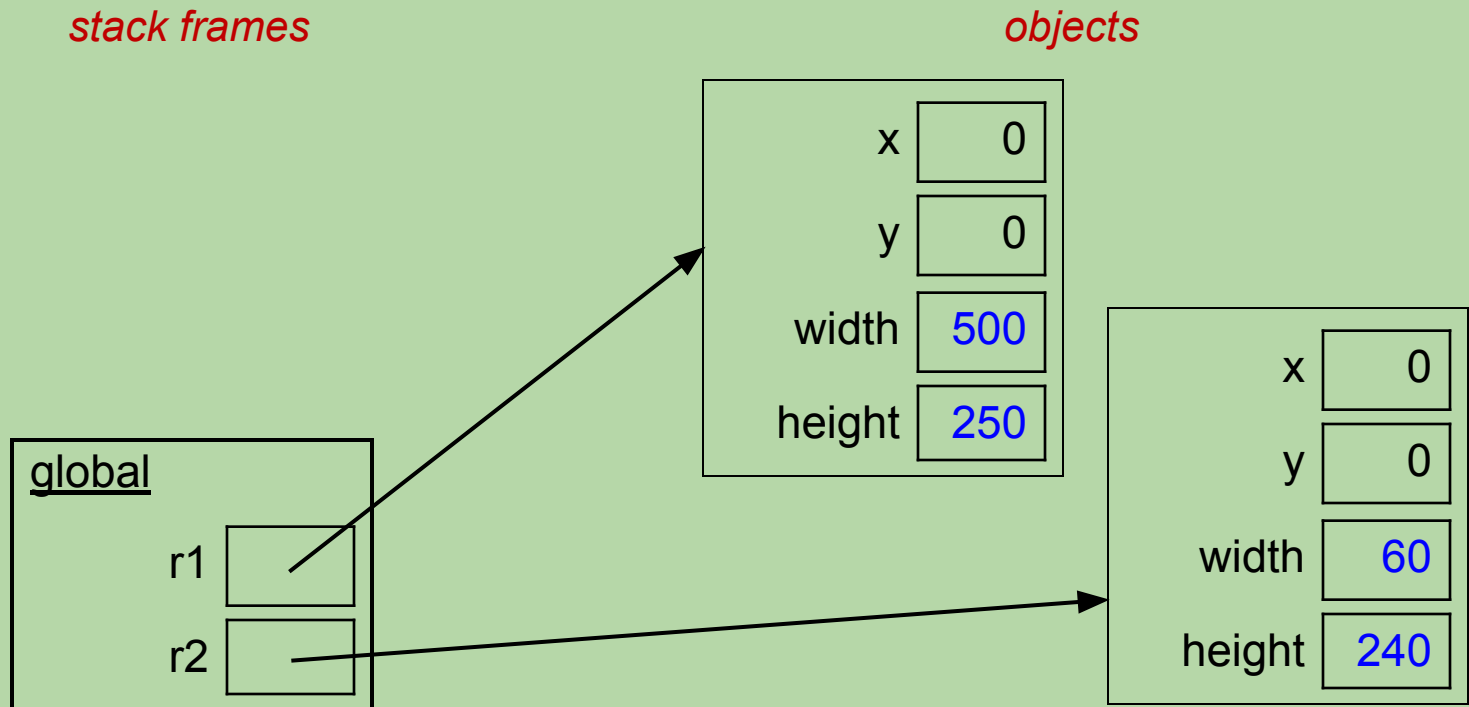
Memory Diagrams for Method Calls

```
# Rectangle Application code  
r1 = Rectangle(100, 50)  
r2 = Rectangle(20, 80)
```

```
r1.scale(5)
```

```
r2.scale(3)
```

```
print(r1.width, r1.height, r2.width, r2.height)
```



Memory Diagrams for Method Calls

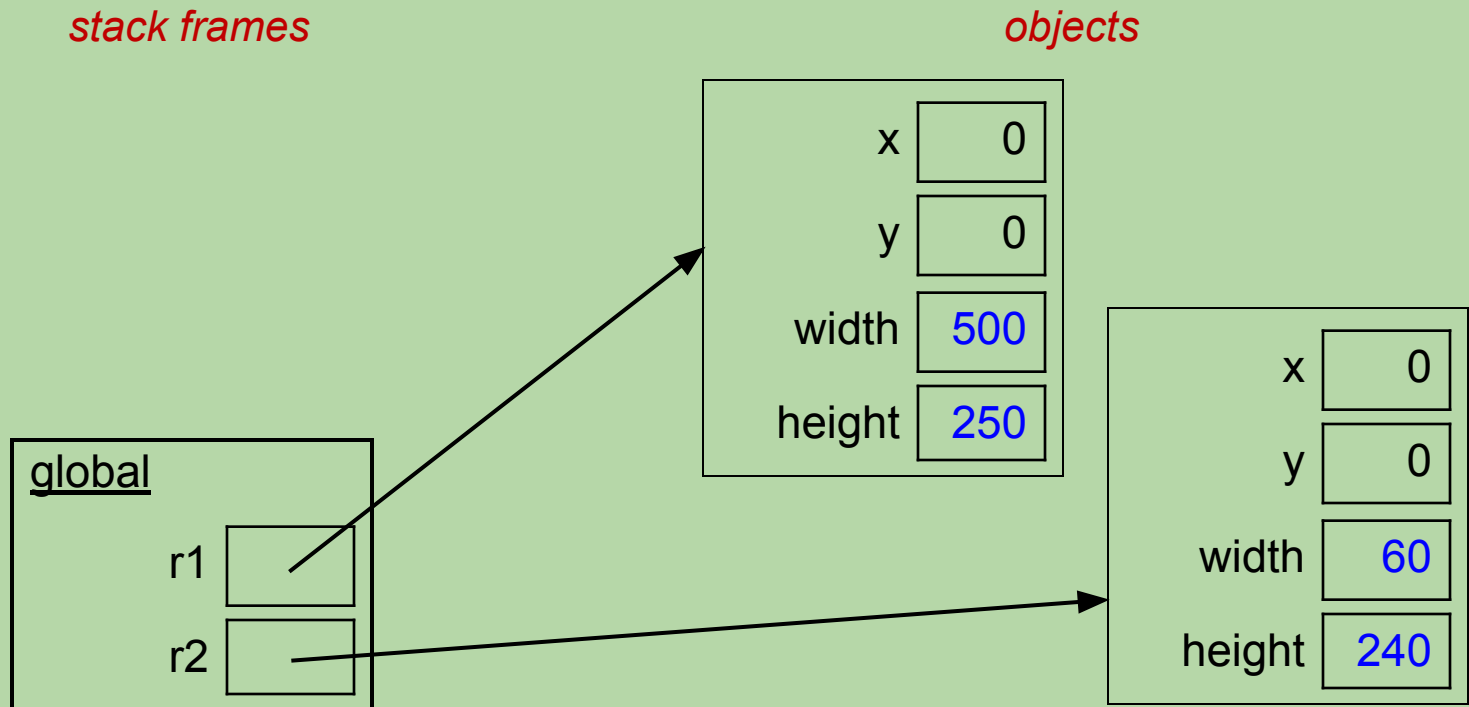
```
# Rectangle Application code  
r1 = Rectangle(100, 50)  
r2 = Rectangle(20, 80)
```

```
r1.scale(5)
```

```
r2.scale(3)
```

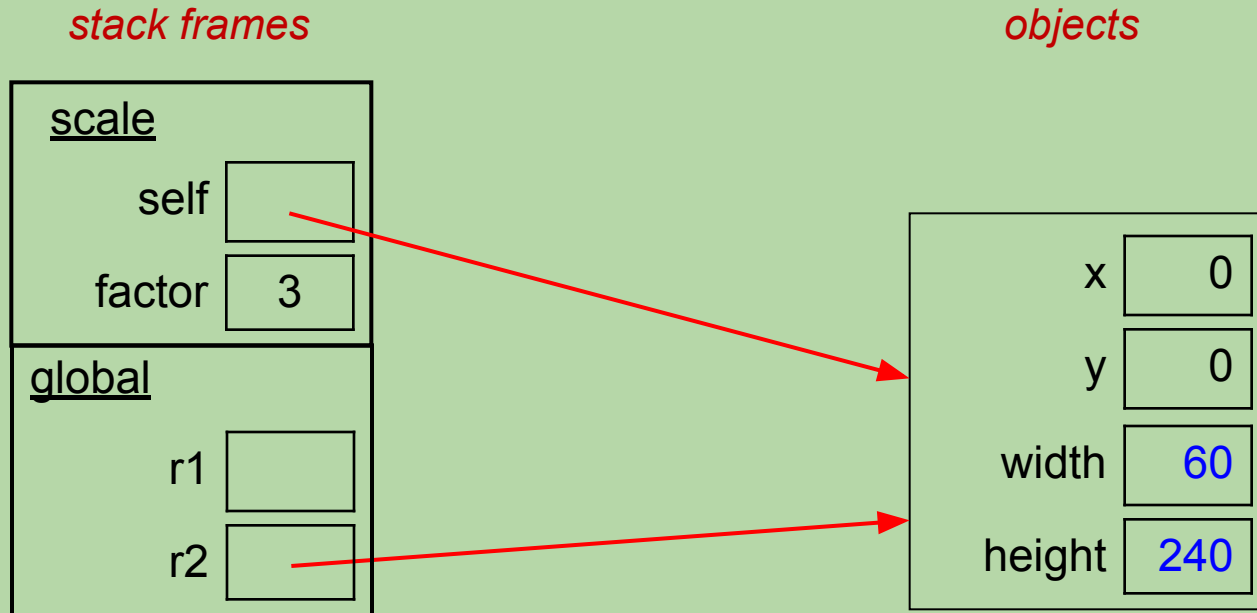
```
print(r1.width, r1.height, r2.width, r2.height)
```

output: 500 250 60 240



No Return Value Is Needed After a Change

- A method operates directly on the called object, so any changes it makes will be there after the method returns.
 - example: the call `r2.scale(3)` from the last slide



- `scale` gets a copy of the *reference* in `r2`
- thus, `scale`'s changes can be "seen" using `r2` after `scale` returns



Project 2

Modeling



UTA Annie honestly could've been a baby model

Text Processing: Stemming

- word → *stem/root* of the word
- Examples:

stem('love') → 'lov'

stem('loving') → 'lov'

stem('stems') → 'stem'

stem('stemming') → 'stem'

stem('stem') → 'stem'

stem('party') → 'parti'

stem('parties') → 'parti'

Which Word(s) Does It "Get Wrong"?

```
def stem(word):  
    if word[-3:] == 'ing':  
        word = word[:-3]  
    elif word[-2:] == 'er':  
        word = word[:-3]  
    elif:  
        # lots more cases!  
        ...  
  
    return word
```

-
- A. playing
 - B. stemming
 - C. spammer
 - D. reader
 - E. more than one (which ones?)

Which Word(s) Does It "Get Wrong"?

```
def stem(word):  
    if word[-3:] == 'ing':  
        word = word[:-3]  
    elif word[-2:] == 'er':  
        word = word[:-3]  
    elif:  
        # lots more cases!  
        ...  
  
    return word
```

- A. playing
- B. **stemming**
- C. spammer
- D. **reader**
- E. more than one (which ones?)

How could you fix the ones it gets wrong?

Be Careful!

```
def stem(word):  
    if word[-3:] == 'ing':  
        if word[-4] == word[-5]:  
            word = word[:-4]  
        else:  
            word = word[:-3]  
    elif word[-2:] == 'er':  
        word = word[:-3]  
    elif:  
        # lots more cases!  
        ...  
    return word
```

stem('stemming') → 'stem'

stem('killing') → 'kil'

stem('sing') → IndexError
(original version gives 's')

Things to Consider When Stemming

- You could include the length of the word in some rules.
- You could use a dictionary of special cases.
- Be careful about the order in which rules are applied.
- Consider the use of recursion in some cases:

```
stem('readers')
```

```
    remove the 's' to get 'reader'
```

```
    stem_rest = stem('reader')
```

```
        remove 'er' to get 'read'
```

```
        return 'read'
```

Things to Consider When Stemming

- You could include the length of the word in some rules.
- You could use a dictionary of special cases.
- Be careful about the order in which rules are applied.
- Consider the use of recursion in some cases:

```
stem('readers')
```

```
    remove the 's' to get 'reader'
```

```
    stem_rest = stem('reader')
```

```
        remove 'er' to get 'read'
```

```
        return 'read'
```

```
    return stem_rest
```


```
     'read'
```

- *It doesn't need to be perfect!*

There's No "Right Answer"!

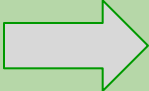
- Example: Rather than doing this:

stem('party')  'parti'

stem('parties')  'parti'

we could do this instead

stem('party')  'party'

stem('parties')  'party'

Classifying a New Body of Text

Suppose we're just focused on the word frequencies:

William Shakespeare

WS: { "love": 50,
"spell": 8,
"thou": 42 }

J.K. Rowling

JKR: { "love": 25,
"spell": 275,
"potter": 700 }

New: { "love": 3, "thou": 1,
"potter": 2 }

How could we give a similarity score for this **new** dictionary against each one above?

Naïve Bayes Scoring Algorithm

multiply each word's probability as if they were all independent

WS: { **"love"**: 50,
"spell": 8,
"thou": 42 }

**100 words
in all**

score vs. WS

50
100

love

New: { **"love"**: 3, **"thou"**: 1,
"potter": 2 }

Naïve Bayes Scoring Algorithm

multiply each word's probability as if they were all independent

WS: { **"love"**: 50,
"spell": 8,
"thou": 42 }

100 words
in all

score vs. WS

$$\frac{50}{100} \cdot \frac{50}{100} \cdot \frac{50}{100}$$

love love love

New: { **"love"**: 3, "thou": 1,
"potter": 2 }

Naïve Bayes Scoring Algorithm

multiply each word's probability as if they were all independent

WS: { "love": 50,
"spell": 8,
"thou": 42 }

100 words
in all

score vs. WS

$$\frac{50}{100} \cdot \frac{50}{100} \cdot \frac{50}{100} \cdot \frac{42}{100}$$

love love love thou

New: { "love": 3, "thou": 1,
"potter": 2 }

Naïve Bayes Scoring Algorithm

multiply each word's probability as if they were all independent

"potter" is not here.

WS: { "love": 50,
"spell": 8,
"thou": 42 }

100 words in all

score vs. WS

$$\frac{50}{100} \cdot \frac{50}{100} \cdot \frac{50}{100} \cdot \frac{42}{100} \cdot \frac{0}{100} \cdot \frac{0}{100}$$

love love love thou potter potter

New: { "love": 3, "thou": 1,
"potter": 2 }

Naïve Bayes Scoring Algorithm

multiply each word's probability as if they were all independent

"potter" is not here.

WS: { "love": 50,
"spell": 8,
"thou": 42 }

100 words in all

score vs. WS

$$\frac{50}{100} \cdot \frac{50}{100} \cdot \frac{50}{100} \cdot \frac{42}{100} \cdot \frac{0}{100} \cdot \frac{0}{100}$$

love love love thou potter potter

score = 0

New: { "love": 3, "thou": 1,
"potter": 2 }

Naïve Bayes Scoring Algorithm

multiply each word's probability as if they were all independent

"potter" is not here.

WS: { "love": 50,
"spell": 8,
"thou": 42 }

100 words in all

score vs. WS

$$\frac{50}{100} \cdot \frac{50}{100} \cdot \frac{50}{100} \cdot \frac{42}{100} \cdot \frac{0.5}{100} \cdot \frac{0.5}{100}$$

love love love thou potter potter

score = 0.00000131

New: { "love": 3, "thou": 1,
"potter": 2 }

Naïve Bayes Scoring Algorithm

multiply each word's probability as if they were all independent

"potter" is not here.

"thou" is not here.

WS: { "love": 50,
"spell": 8,
"thou": 42 }

100 words in all

JKR: { "love": 25,
"spell": 275,
"potter": 700 }

1000 words in all

score vs. WS

$$\frac{50}{100} \cdot \frac{50}{100} \cdot \frac{50}{100} \cdot \frac{42}{100} \cdot \frac{0.5}{100} \cdot \frac{0.5}{100}$$

love love love thou potter potter

score = 0.00000131

>

score vs. JKR

$$\frac{25}{1000} \cdot \frac{25}{1000} \cdot \frac{25}{1000} \cdot \frac{0.5}{1000} \cdot \frac{700}{1000} \cdot \frac{700}{1000}$$

love love love thou potter potter

score ≈ 0.00000000382

New: { "love": 3, "thou": 1,
"potter": 2 }

more likely to be WS!

problem: scores can become too small!

Naïve Bayes Scoring Algorithm

multiply each word's probability as if they were all independent

"potter" is not here.

"thou" is not here.

WS: { "love": 50,
"spell": 8,
"thou": 42 }

100 words in all

JKR: { "love": 25,
"spell": 275,
"potter": 700 }

1000 words in all

score vs. WS

score vs. JKR

$$\frac{50}{100} \cdot \frac{50}{100} \cdot \frac{50}{100} \cdot \frac{42}{100} \cdot \frac{0.5}{100} \cdot \frac{0.5}{100}$$

love love love thou potter potter

$$3\log\left(\frac{50}{100}\right) + 1\log\left(\frac{42}{100}\right) + 2\log\left(\frac{0.5}{100}\right)$$

score \approx -13.54

$$\frac{25}{1000} \cdot \frac{25}{1000} \cdot \frac{25}{1000} \cdot \frac{0.5}{1000} \cdot \frac{700}{1000} \cdot \frac{700}{1000}$$

love love love thou potter potter

$$3\log\left(\frac{25}{1000}\right) + 1\log\left(\frac{0.5}{1000}\right) + 2\log\left(\frac{700}{1000}\right)$$

score \approx -19.38

>

New: { "love": 3,
"thou": 1,
"potter": 2 }

more likely to be WS!

problem: scores can become too small!
solution: sum logs!