# Lecture 15 <br> MATLAB II: Conditional Statements and Arrays 



## Conditional Statements

## Recall boolean Expressions

-The boolean operators in MATLAB are:

```
> greater than
< less than
>= greater than or equals
<= less than or equals
== equality
~= inequality
```

-The resulting type is logical 1 for true or o for false
-The logical operators are:
$\|$ or for scalars
\&\& and for scalars
~ not

- Also, xor function which returns logical true if only one of the arguments is true


## If Statement

- The if statement is used to determine whether or not a statement or group of statements is to be executed
- General form:

```
if condition
        action
    end
```

- the condition is any boolean expression
- the action is any number of valid statements (including, possibly, just one)
- if the condition is true, the action is executed - otherwise, it is skipped entirely


## If-else Statements

-The if-else statement chooses between two actions

- General form:

```
if condition
    action1
    else
    action2
    end
```

- One and only one action is executed; which one depends on the value of the condition (action1 if it is logical true or action2 if it is false)


## Nested if-else statements are ugly :-(

```
if condl
    actionl
else
    if cond2
        action2
    else
        if cond3
            % cond1 and cond2 False, cond3 True
            action3
            else
                actionN
            end
    end
end
```


## if-elseif statements are better :-|

MATLAB has an elseif clause which shortens nested if-else

```
if condl
        actionl
elseif cond2
        action2
elseif cond3
    % cond1 and cond2 False, cond3 True
    action3
else
    % if no other conditions met
    default_action
end
```


## switch statements are (sometimes) best :-)

MATLAB also has a switch statement!

```
switch var
    case case1 % var == casel
        actionl;
    case case2 % var == case2
        action2;
    case {case3,case4}
    % var == case3 || var == case4
    action3;
    otherwise
    % var doesn't match any case
    default_action;
end
```


## Example: branching.m

```
%%
x=-5;
%%
% Implements }\textrm{x}=\textrm{abs}(\textrm{x})\mathrm{ ;
if }x<
        x = -x;
end
%%
% Forces x into the interval [a,b]
if x>b
        x = b;
elseif x<a
        x = a;
end
x
    %%
% Forces x into the interval [a,b], and changes it's value to x^2.
x = 2; a=3; b=7;
if }x>
        x = b^2;
elseif x<a
    x = a^2;
else
    x = x^2;
end
x
% Is there a better way?
%%
g=3; x=25; thresh =.1
% One step of Heron's squareroot
if abs(g^2-x)>thresh
    g=(g+x/g)/2
end
```


## iClicker Question: What is the value of $x$ ?

$$
\begin{aligned}
& \begin{array}{l}
x=3 ; a=2 ; b=7 ; \\
\text { if } x>b \\
x=b ; \\
\text { elseif } x<a \\
\quad x=a^{\wedge} 2 ; \\
\text { else } \\
\quad x=x^{\wedge} 3 ;
\end{array} \\
& \text { end }
\end{aligned}
$$

A) $x=3$
C) $x=9$
B) $x=27$
D) undefined

## iClicker Question: What is the value of $x$ ?

$$
\begin{aligned}
& x=3 ; a=2 ; b=7 ; \\
& \text { if } x>b \\
& \quad x=b ; \\
& \text { elseif } x<a \\
& \qquad x=a^{\wedge} 2 ; \\
& \text { else } \\
& \quad x=x^{\wedge} 3 ; \\
& \text { end }
\end{aligned}
$$

A) $x=3$
C) $x=9$
B) $x=27$
D) undefined

## Common Pitfalls

- Using = instead of == for equality in conditions
-Putting a space in the keyword elseif
- Not using quotes when comparing a char variable to character,

$$
\text { letter }==\mathrm{y}
$$

instead of
letter == 'y'
-Writing conditions that are more complicated than necessary, such as

$$
\text { if }(x<5)==1 \text { instead of just if }(x<5)
$$

## Example: myQuadMin.m

function xmin $=\operatorname{myQuadMin}(a, b, c, L, R)$
\% xmin $=$ quadMinizer $(a, b, c, L, R)$
\% Returns $x$ in the interval [L, R] that minimizes the quadratic function \% $a x^{\wedge} 2+b x+c$. Assumes $a>=0$, and $L<R$.

## Example: myQuadMin.m

```
if a>0 % Parabola
    x0 = -b/(2*a); % argmin ax^2+bx+c for a>0
    if R<x0
        % [L,R] is to left of x0
        xmin = R;
    elseif L<=x0 && x0<=R
        % [L,R] contains x0
        xmin = x0;
    else
        % [L,R] is to right of x0
        xmin = L;
    end
elseif a==0 % Straight line
    if b>0
        % bx+c is sloping up
        xmin = L;
    elseif b<0
        % bx+c is sloping down
        xmin = R;
    else
        % bx+c is flat
        xmin = L;
    end
end
```


## Programming Style Guidelines

- Use indentation to show the structure of a script or function. In particular, the actions in an if statement should be indented.
-When the else clause isn't needed, use an if statement rather than an if-else statement


## Arrays

## Arrays and Matrices

-Array_Basics.mlx

## Arrays and Matrices

-An array is used to store sets of values of same type; each value is stored in an element of the array

- A matrix is a two-dimensional array
- A vector is a one-dimensional array
- Other programming languages mostly work with numbers one at a time, MATLAB® was designed from the ground up to operate primarily on whole matrices and arrays
- Most MATLAB classes come with multidimensional array support


## Examples

1-Dimensional Arrays (Vectors)

- Point in $R^{\wedge} n$, Polynomial Coefficients
-Time Series - temp(t), annual snow falls, music, $v(t)$, price(t)
- Strings, texts, webpages, DNA sequences

2-Dimensional Arrays (Matrices)

- System of equations, Linear Transforms, Covariance
- Images ( $m$ by $n$ black and white image)
- Digital elevation data, Collections of points
- Stock market prices

3-Dimensional Arrays (3-D Matrix)

- Black and White Video
- Color Images


## Matrices

- A matrix (2-D array) looks like a table; it has both rows and columns
- A matrix with $m$ rows and $n$ columns is said to be " $m$ by $n$ ". Write this " $m x n$ ". Its first dimension is $m$; the second is $n$.
-This is a $2 \times 3$ matrix:

| 9 | 6 | 3 |
| :--- | :--- | :--- |
| 5 | 7 | 2 |

-The first row of is [9 63 3], the second row is [lllll 7 l
-The first column is [954], the last column is [32]'

## Vectors and Scalars

$\square$ A vector (1-D array) is a special case of a matrix in which one of the dimensions is 1
$\square$ a row vector with $n$ elements is $1 \times n$, e.g. $1 \times 4$ :

| 5 | 88 | 3 | 11 |
| :--- | :--- | :--- | :--- |

$\square$ a column vector with $m$ elements is $m \times 1$, e.g. $3 \times 1$ :
3
7
4
$\square$ A scalar is an even more special case ; it is $1 \times 1$, or in other words, just a single value

## Creating Row Vectors

$\square$ Direct method: Use square brackets, with elements separated by either commas or spaces

$$
\left.\left.\left.\begin{array}{l}
\gg v=\left[\begin{array}{llll}
1 & 2 & 3 & 4
\end{array}\right] \\
v=1
\end{array} 2 \begin{array}{llll} 
& 3 & 4
\end{array}\right] \begin{array}{llll}
1, & 2, & 3, & 4
\end{array}\right], \begin{array}{llll}
-10 & v
\end{array}\right] .
$$

## Colon Operator

The colon operator creates evenly spaced row vectors;

## start:step:max

produces a vector whose first element is start and whose subsequent elements are step apart, the last element is <= max.

```
>> 5:3:14
ans = [5 8 11 14]
>> 2:4 % default step size is 1
ans = [\begin{array}{lll}{2 3 4]}\end{array}]
>> 4:-1:1 % can go in reverse
ans = [4 3 2 1]
>> 0:.3:1 % fractional step sizes OK
ans = [0 . 3 . 6 .9]
```


## linspace

linspace (a,b,n) creates a linearly (evenly) spaced row vector with $\boldsymbol{n}$ values starting at $\boldsymbol{a}$ and ending at $\boldsymbol{b}$.
>> linspace $(4,7,3)$
ans $=\left[\begin{array}{lll}4 & 5.5 & 7\end{array}\right]$

If n is omitted, the default is 100 points

## colon vs. linspace

- Use first: step:max when you need to specify the first element and the step size. Last element returned is $<=$ max.
- Use linspace ( $\mathrm{a}, \mathrm{b}, \mathrm{n}$ ) when you need to specify the first element a and last element b. Step size calculated base on number points n .


## Concatenation

- Vectors can be created by joining together existing vectors, or adding elements to existing vectors
-This is called concatenation
-For example:

$$
\begin{aligned}
& \text { >> v = 2:5; } \\
& \text { >> } x=\left[\begin{array}{lll}
33 & 11 & 2
\end{array}\right] ; \\
& \text { >> w = [lll} \mathbf{v} \text { x] \% concatenate } v \text { and } x \\
& \begin{array}{lllllll}
\mathrm{w}=2 & 3 & 4 & 5 & 33 & 11 & 2
\end{array} \\
& \text { >> v }=\left[\begin{array}{ll}
v & 44
\end{array}\right] \% \text { append } 44 \text { to } v \\
& \mathrm{v}=2 \begin{array}{lllll} 
& 3 & 4 & 5 & 44
\end{array}
\end{aligned}
$$

## Referring to Elements

-The elements in a vector are indexed sequentially; an example index is shown above the elements here:

| 1 | 2 |  | 3 | 4 |
| :--- | :--- | :--- | :--- | :--- |
| 5 | 33 | 11 | -4 | 2 |

- Refer to an element using its index or subscript in parentheses, $\operatorname{vec}(4)$ is the $4^{\text {th }}$ element of a vector
- Can also refer to a subset of a vector by using an index vector which is a vector of indices e.g.
$\operatorname{vec}([25])$ refers to the $2^{\text {nd }}$ and $5^{\text {th }}$ elements of vec;
$\operatorname{vec}([1: 4])$ refers to the first 4 elements


## Modifying Vectors

Elements in a vector can be changed via the assignment

```
>> vec(3) = 11;
>> vec(1:4) = [3 6 3 1];
>> vec(5:10) = 7;
```

Assignment to elements that do not yet exist is allowed (but not good style); if there is a gap between the end of the vector and the new specified element(s), zeros are filled in, e.g.
>> vec $=[39]$;
$\gg \operatorname{vec}(4: 6)=\left[\begin{array}{lll}33 & 2 & 7\end{array}\right]$
vec =
3
9
0
33
2
7

## Column Vectors

A column vector is an $m x 1$ vector; can create in square brackets with semicolons e.g.
>> $x=[4 ; 7$; 2]
x =
4
7
2
-The colon operator only creates row vectors, but you can transpose row vectors to get a column vectors (and vice-versa) using the transpose operator '
>> $x=\left[\begin{array}{lll}4 & 7 & 2\end{array}\right] '$
x =
4
7
2

## Creating Matrix Variables

$\square$ Separate values within rows with blanks or commas, and separate the rows with semicolons
$\square$ Can use any method to get values in each row (any method to create a row vector, including colon operator)

```
    >> mat = [1:3; 6 11 -2]
    mat =
\begin{tabular}{rrr}
1 & 2 & 3 \\
6 & 11 & -2
\end{tabular}
```

$\square$ There must ALWAYS be the same number of values in every row!!

## Functions that create matrices

-There are many built-in functions to create matrices

- $\operatorname{rand}(\mathbf{n})$ creates an $n x n$ matrix of uniform random numbers (real)
- $\operatorname{rand}(\mathbf{m}, \mathbf{n})$ create an $m x n$ matrix of uniform random numbers (real)
- randi([range], $\mathbf{m}, \mathbf{n}$ ) creates an $m x n$ matrix of random integers in the specified range
- zeros(n) creates an $n x n$ matrix of all zeros
- zeros( $\mathbf{m}, \mathbf{n}$ ) creates an mxn matrix of all zeros
- ones(n) creates an $n x n$ matrix of all ones
- ones( $\mathbf{m}, \mathbf{n}$ ) creates an $m x n$ matrix of all ones

Note: there is no twos function - or thirteens - just zeros and ones!

## Matrix Elements

-To refer to an element in a matrix, you use the matrix variable name followed by the index of the row, and then the index of the column, in parentheses

$$
\begin{aligned}
& \gg \text { mat }=[1: 3 ; 6 \text { lll } 11 \text {-2 }] \\
& \text { mat }= \\
& 123 \\
& \begin{array}{lll}
6 & 11 & -2
\end{array} \\
& \gg \operatorname{mat}(2,1) \\
& \text { ans = } \\
& 6
\end{aligned}
$$

- ALWAYS refer to the row first, column second


## Dimensions

-There are several functions to determine the dimensions of a vector or matrix:
-length(vec) returns the \# of elements in a vector

- length(mat) returns the largest dimension (row or column) for a matrix - :o( DO NOT USE length on arrays that are not vectors!
- size returns the \# elements in each dimension of an array
- Important: can capture multiple values in an assignment statement

$$
[\mathrm{rc}]=\operatorname{size}(\mathrm{mat})
$$

- numel returns the total \# of elements in an array
- Very important to be general in programming: do not assume fixed dimensions of a vector or matrix - use numel or size to find out or avoid knowing via use of end and : inside the paranthesis!!


## Functions that change dimensions

Many functions change the dimensions of a matrix:
$\square$ reshape changes dimensions of a matrix to any matrix with the same number of elements, linear order does not change
arot90 rotates a matrix 90 degrees
counter-clockwise
afliplr flips columns of a matrix from left to right
qflipud flips rows of a matrix up to down
qrepmat replicates a matrix; creates $m \times n$ copies of
the matrix

## Advanced Indexing

-See Array_Indexing.mlx

## Advanced Indexing

- Isolated colon : refers to entire dimension
mat (i, :) - the ith row of mat
this is equivalent to mat (i, 1:size (mat, 2))
- To refer to the last row or column use end
mat (end, $k$ ) - the kth value in the last row
- Value of end and isolated colon : is determined by context within subscript.
mat (end, end) - value of mat(size(mat,1), size(mat,2))
- Use of index vectors is also allowed
$m([24],[15])$ returns the matrix
$[m(2,1) m(2,5) ; m(4,1) m(4,5)]$


## Advanced Indexing



## Linear Array Indexing

The following works on all arrays (1-D, 2-D, etc.)
$\square A(:)$ forces $A$ into a column vector containing all elements of A
$\square A(k)$ is the kth element of $A(:)$
$\square A$ (M) is a array with the same dimensions as $M$. For matrix $M$, the result would have elements $A(M(i, j))$
$a=$

| 16 | 2 | 3 | 13 |
| ---: | ---: | ---: | ---: |
| 5 | 11 | 10 | 8 |
| 9 | 7 | 6 | 12 |
| 4 | 14 | 15 | 1 |

>> a([1 2; 3 4])
ans =

165
94

## Removing Elements

$\square$ An empty vector is a vector with no elements; an empty vector can be created using square brackets with nothing inside []
$\square$ Delete element(s) from a vector by assigning [] >> $\operatorname{vec}(1)=[]$; remove first element >> vec[end-2:end]=[]; \% remove last 3 elements
$\square$ Delete row(s) or column(s) from a matrix by assigning [] >> mat([1 end],:)=[]; \% remove first and last row

Note: cannot delete an individual element from a matrix. Can you see why?

## iClicker Question: Which vehicle is for Prof. G?



A
2012 Honda Pilot 90,000 miles \$0 / month


B $\begin{gathered}2019 \text { Chevy Silverado } \\ 0 \text { miles } \\ \$ 800 / \text { month }\end{gathered}$


2015 Jeep Wrangler 50,000 miles $\$ 500$ / month

$E \quad \begin{gathered}2019 \text { Jeep Wrangler } \\ 0 \text { miles } \\ \$ 800 / \text { month }\end{gathered}$

