

Introduction to Computer Vision

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Stereo

Goals

- Today
 - Finish stereo
 - Start something new
- Monday
 - Finish something new

Project

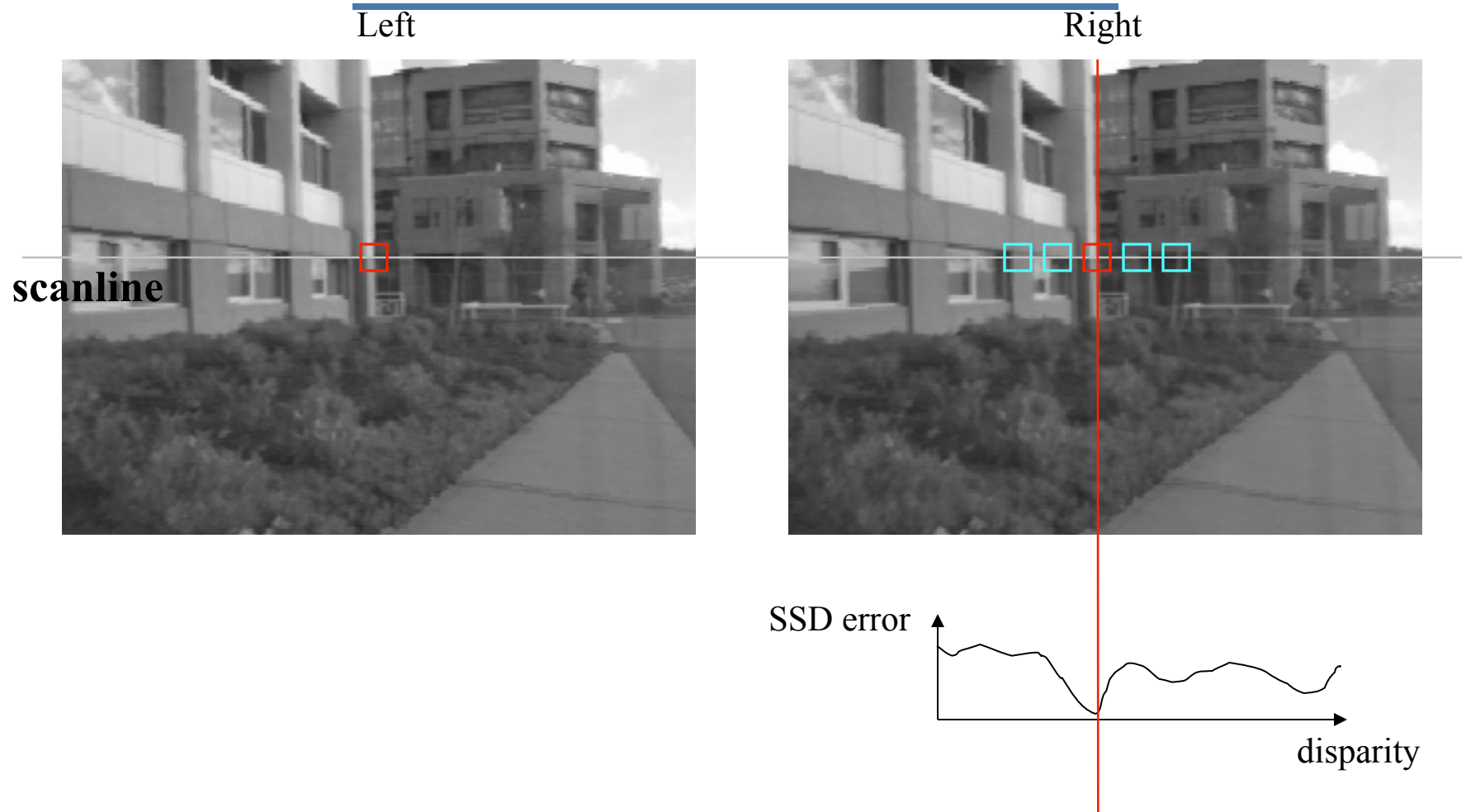
- Proposals evaluated over weekend
- Due date extended to Dec 16.

Pseudocode

condense1 step

```
% generate cumulative distribution for posterior at t-1
....
% generate a vector of uniform random numbers.
% if a the number is greater than refreshRate then
    % generate a vector of uniform random numbers
    % use these to search the cumulative probability
    % find the indices of the corresponding particles
    % for each of these particles, predict the new state
    % for each of these new states compute the log likelihood
% else generate a particle at random and compute its log likelihood.
% find the maximum log likelihood and subtract it from all the other log
  likelihoods
% construct the posterior at time t by exponentiating all the log likelihoods
  and normalizing so they sum to 1.
```

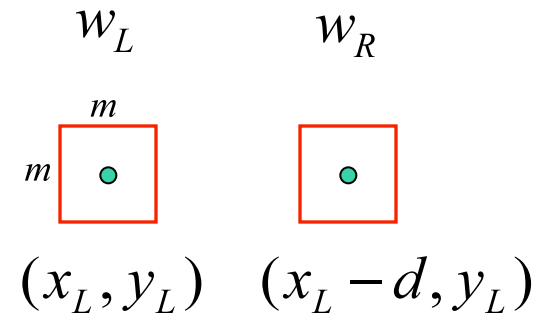
Correspondence Using SSD



Sum of Squared (Pixel) Differences

Left

Right



w_L and w_R are corresponding m by m windows of pixels.

The SSD cost measures the intensity differences as a function of disparity :

$$SSD_r(x, y, d) = \sum_{(x', y') \in W_m(x, y)} (I_L(x', y') - I_R(x' - d, y'))^2$$

Correspondence Using SSD

Left



Disparity Map



Images courtesy of Point Grey Research

Bayesian Interpretation



$$p_M(\mathbf{d} \mid I_L, I_R)$$

How do we proceed?

Bayesian inference

Prior model $p_P(\mathbf{d})$

Likelihood model $p_M(I_L, I_R | \mathbf{d})$

Posterior model

$$p(\mathbf{d} | I_L, I_R) = k p_M(I_L, I_R | \mathbf{d}) p_P(\mathbf{d})$$

Maximum a Posteriori (MAP estimate):

$$\text{maximize } p(\mathbf{d} | I_L, I_R)$$

Measurement model

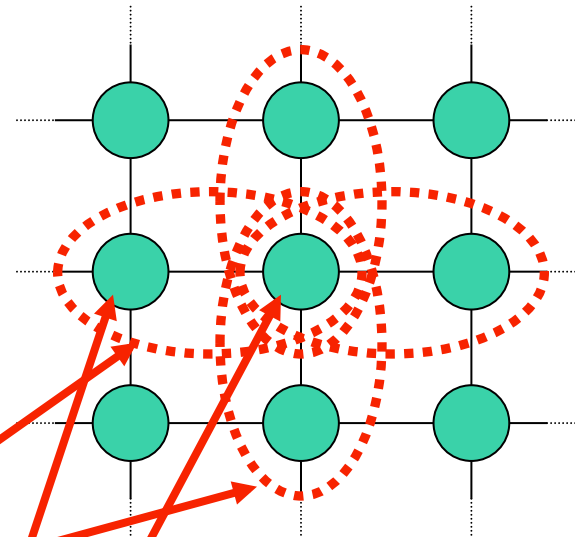
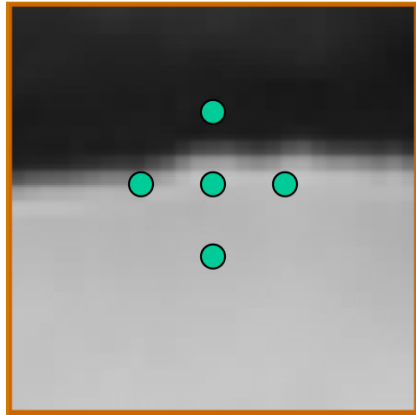
Likelihood of intensity correspondence

$$p_M(I_L, I_R | \mathbf{d}) = \frac{1}{Z_M} e^{-E_0(x, y; d)}$$

$$E_0(x, y; d) = \rho(I_L(x' + d, y') - I_R(x', y'))$$

Corresponds to Gaussian noise for quadratic r

Pairwise Markov Random Fields



Image

$$p(\mathbf{x}) = \frac{1}{Z}$$

$$\prod_{\text{neighbors } (x_i, x_j)}$$

$$\Psi(x_i, x_j)$$

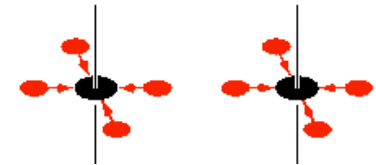
Clique "potential"

Markov Random Field

Probability distribution on disparity field $d(x,y)$

$$p(\mathbf{x}) = \frac{1}{Z} \prod_{\substack{\text{neighbors} \\ (x_i, x_j)}} \Psi(x_i, x_j)$$

$$p_P(\mathbf{d}) = \frac{1}{Z_P} e^{-E_P(\mathbf{d})}$$

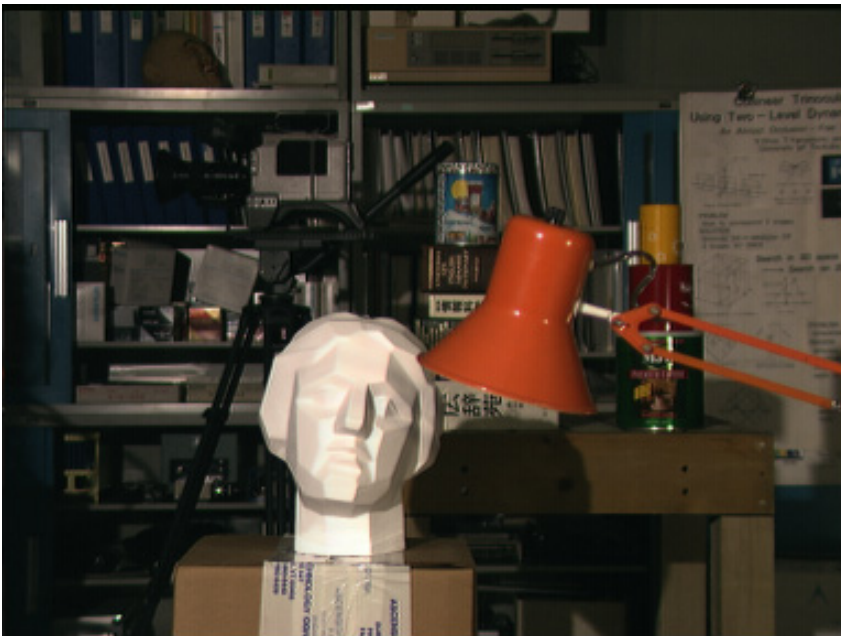


$$E_P(\mathbf{d}) = \sum_{x,y} \rho_P(d_{x+1,y} - d_{x,y}) + \rho_P(d_{x,y+1} - d_{x,y})$$

Enforces *smoothness* or *coherence* on field

Stereo results

– Data from University of Tsukuba



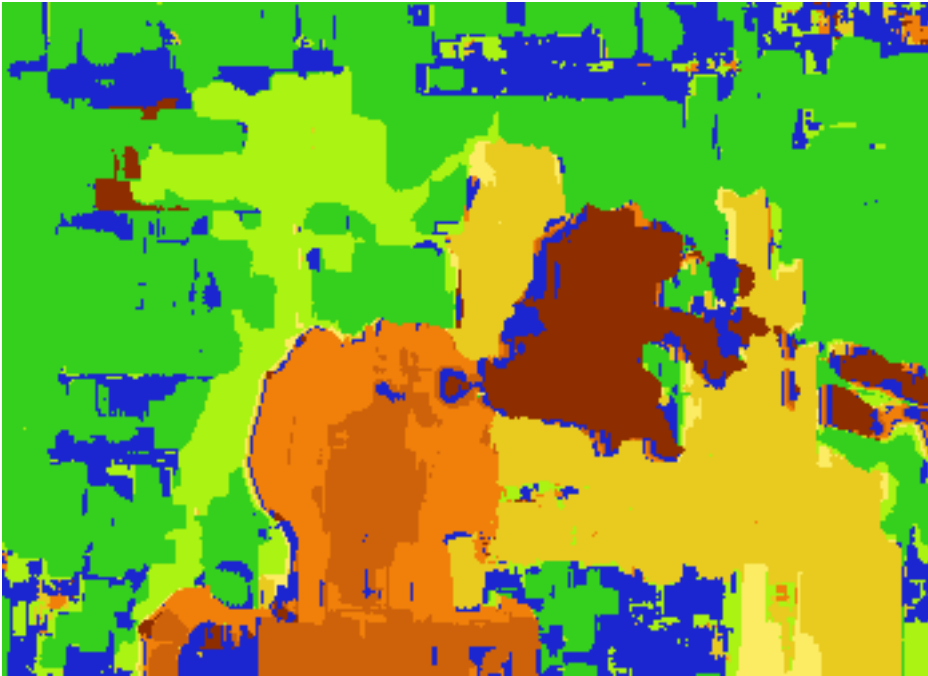
Scene



Ground truth

(Seitz)

Results with window correlation



Window-based matching
(best window size)



Ground truth

(Seitz)

Results with better method



Reasonably good method

Boykov et al., [Fast Approximate Energy Minimization via Graph Cuts](#),
International Conference on Computer Vision, September 1999.



Ground truth

(Seitz)

Results with better method



Best method on Middlebury stereo site

<http://vision.middlebury.edu/stereo/eval/>.

Ground truth

(Seitz)

Choice?

- Markov random field models of images
 - Detail and novel research
- Object recognition
 - High level overview of the current field