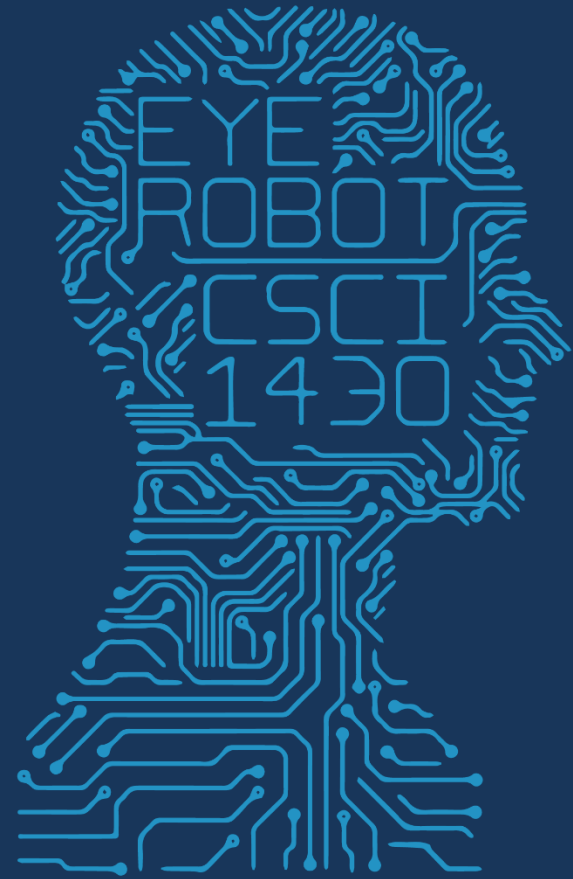




1950

FUTURE VISION



2017 MWF 1PM 368

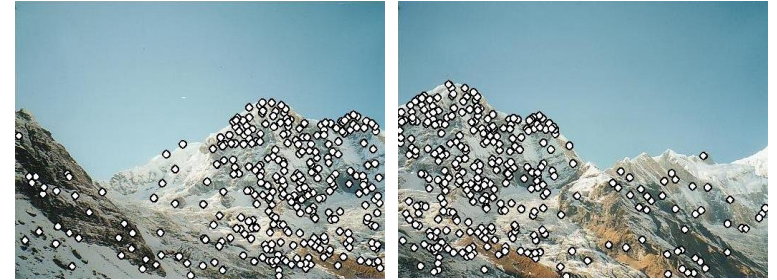
COMPUTER VISION

# Local features: main components

---

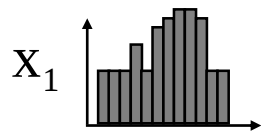
## 1) Detection:

Find a set of distinctive key points.

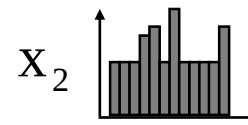
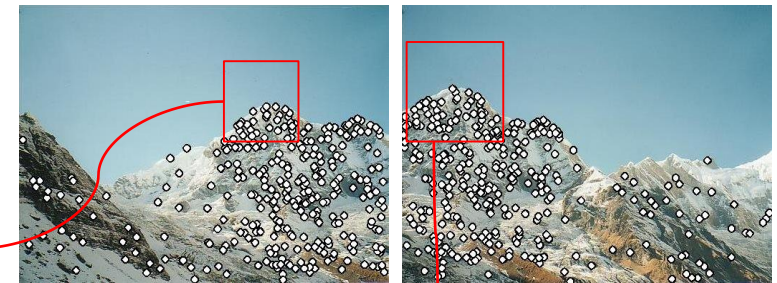


## 2) Description:

Extract feature descriptor around each interest point as vector.



$$\mathbf{x}_1 = [x_1^{(1)}, \dots, x_d^{(1)}]$$

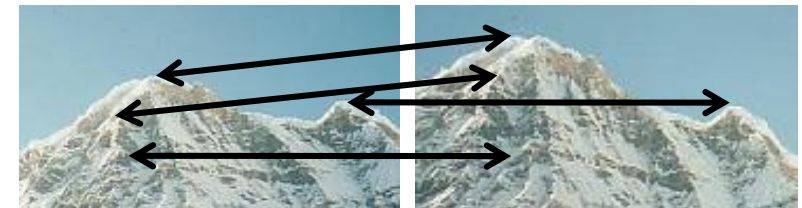


$$\mathbf{x}_2 = [x_1^{(2)}, \dots, x_d^{(2)}]$$

## 3) Matching:

Compute distance between feature vectors to find correspondence.

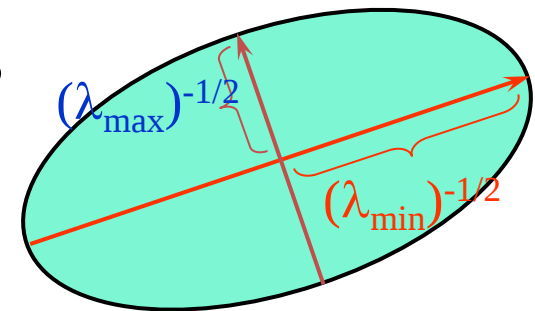
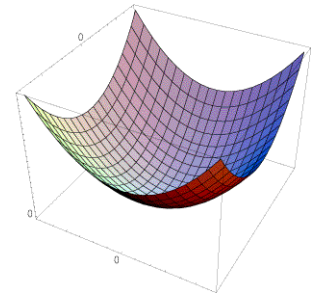
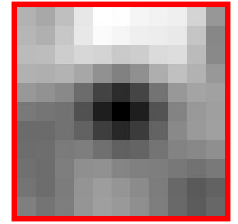
$$d(\mathbf{x}_1, \mathbf{x}_2) < T$$



# Review: Harris corner detector

- Approximate distinctiveness by local auto-correlation.
- Approximate local auto-correlation by second moment matrix **M**.
- Distinctiveness (or cornerness) relates to the eigenvalues of **M**.
- Instead of computing eigenvalues directly, we can use determinant and trace of **M**.

$E(u, v)$



$$M = \sum_{x,y} w(x, y) \begin{bmatrix} I_x^2 & I_x I_y \\ I_x I_y & I_y^2 \end{bmatrix}$$

# Trace / determinant and eigenvalues

- Given  $n \times n$  matrix  $A$  with eigenvalues  $\lambda_{1\dots n}$

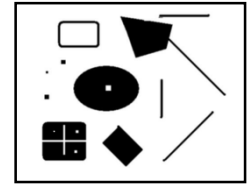
$$\text{tr}(A) = \sum_{i=1}^n A_{ii} = \sum_{i=1}^n \lambda_i = \lambda_1 + \lambda_2 + \dots + \lambda_n.$$

$$\det(A) = \prod_{i=1}^n \lambda_i = \lambda_1 \lambda_2 \dots \lambda_n.$$

- $R = \lambda_1 \lambda_2 - \alpha(\lambda_1 + \lambda_2)^2 = \det(M) - \alpha \text{trace}(M)^2$

# Harris Detector [Harris88]

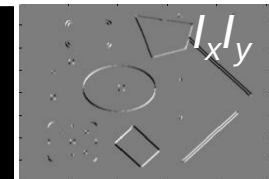
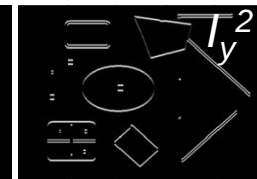
$$M(\sigma_I, \sigma_D) = g(\sigma_I) * \begin{bmatrix} I_x^2(\sigma_D) & I_x I_y(\sigma_D) \\ I_x I_y(\sigma_D) & I_y^2(\sigma_D) \end{bmatrix}$$



1. Image derivatives  
(optionally, blur first)



2. Square of derivatives



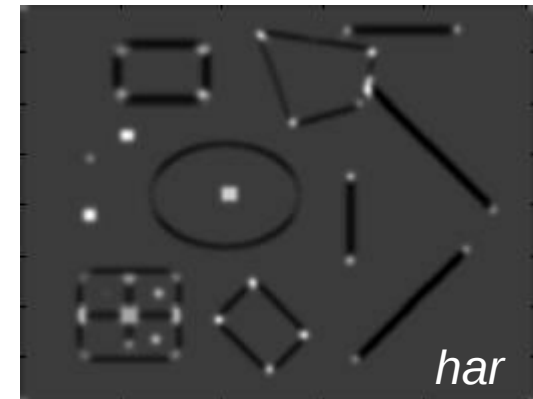
3. Gaussian filter  $g(\sigma_I)$



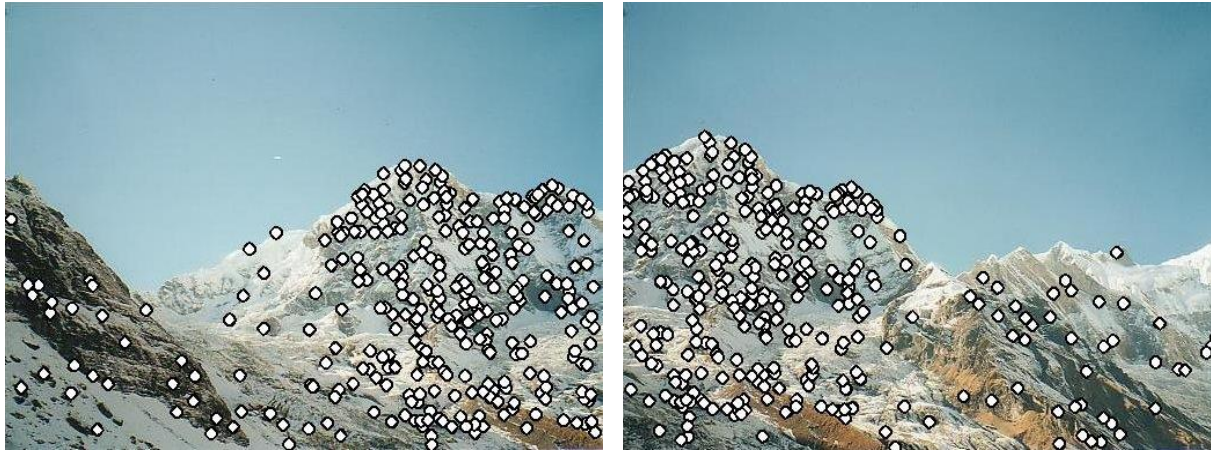
4. Cornerness function – both eigenvalues are strong

$$\begin{aligned} har &= \det[M(\sigma_I, \sigma_D)] - \alpha [\text{trace}(M(\sigma_I, \sigma_D))]^2 \\ &= g(I_x^2)g(I_y^2) - [g(I_x I_y)]^2 - \alpha [g(I_x^2) + g(I_y^2)]^2 \end{aligned}$$

5. Non-maxima suppression

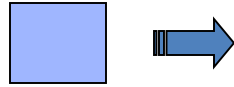


# Characteristics of good features



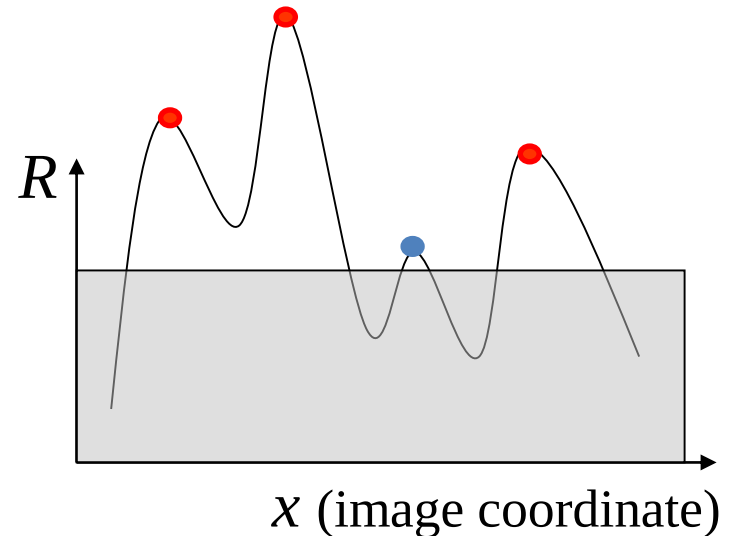
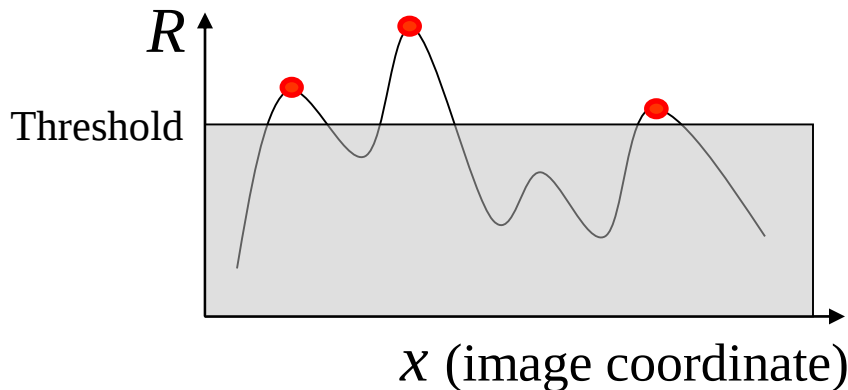
- **Repeatability**
  - The same feature can be found in several images despite geometric and photometric transformations
- **Saliency**
  - Each feature is distinctive
- **Compactness and efficiency**
  - Many fewer features than image pixels
- **Locality**
  - A feature occupies a relatively small area of the image; robust to clutter and occlusion

# Affine intensity change



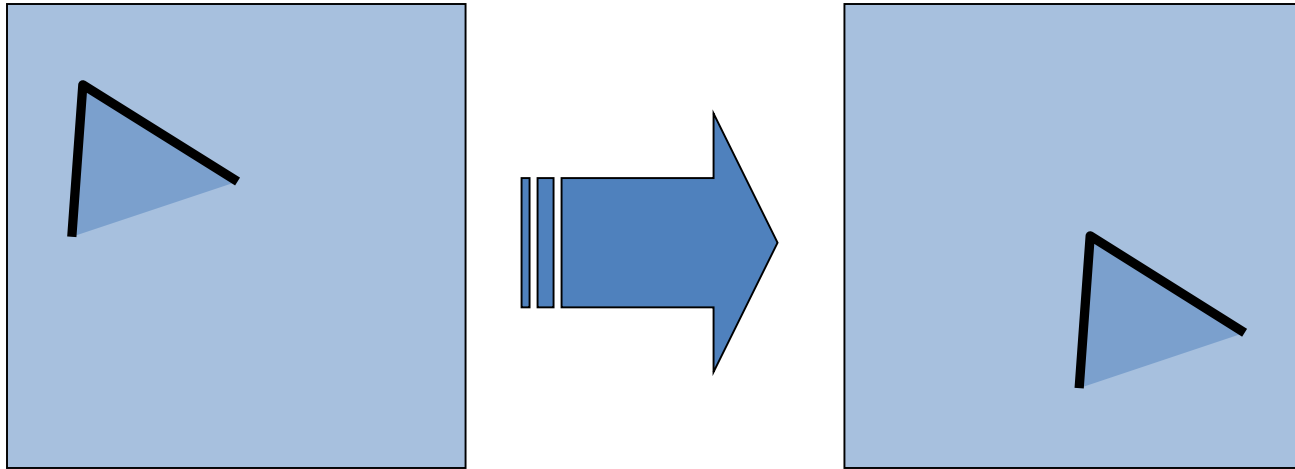
$$I \rightarrow a I + b$$

- Only derivatives are used => invariance to intensity shift  $I \rightarrow I + b$
- Intensity scaling:  $I \rightarrow a I$



*Partially invariant to affine intensity change*

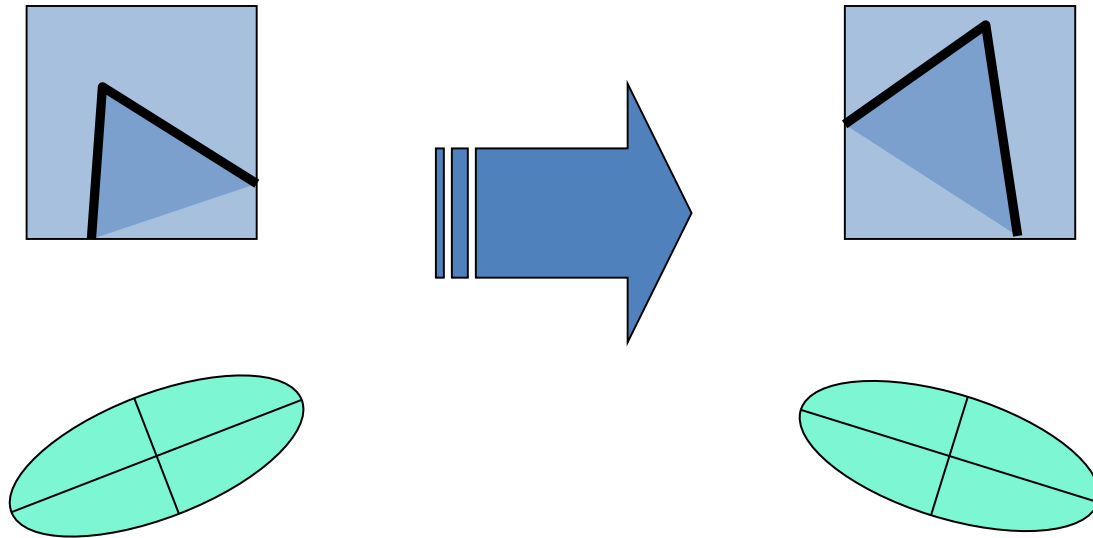
# Image translation



- Derivatives and window function are shift-invariant.

Corner location is covariant w.r.t. translation

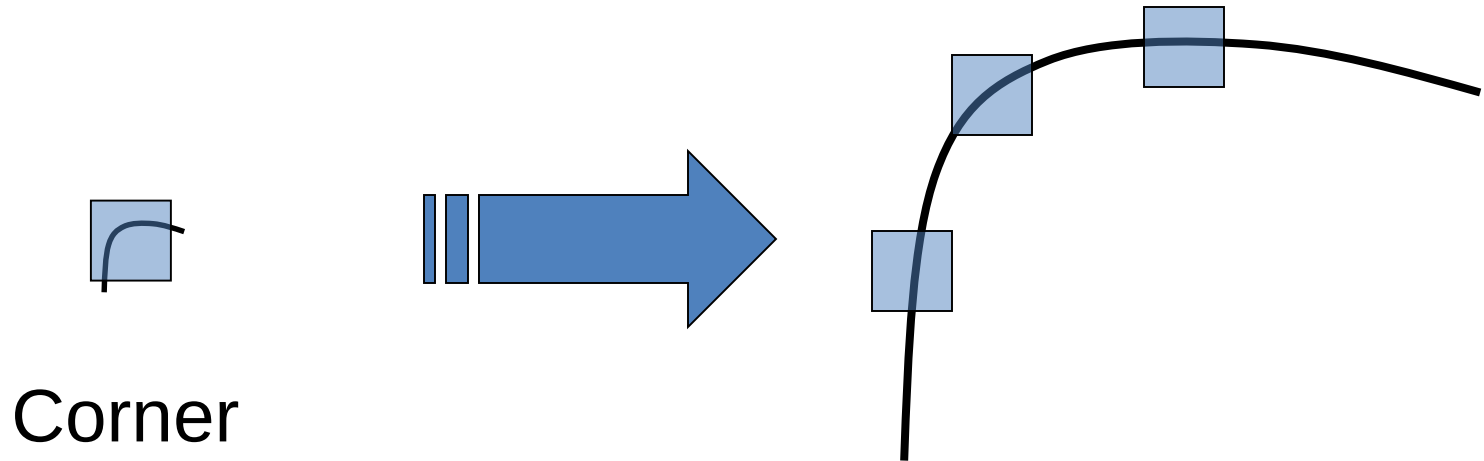
# Image rotation



Second moment ellipse rotates but its shape (i.e., eigenvalues) remains the same.

Corner location is covariant w.r.t. rotation

# Scaling



Corner location is not covariant to scaling!

# Automatic Scale Selection

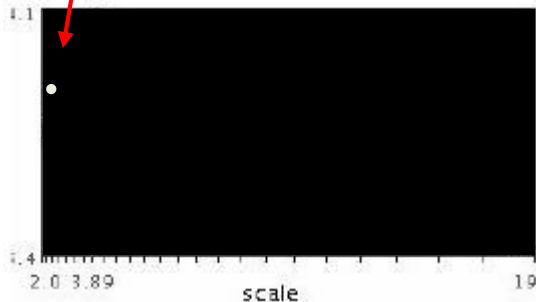


$$f(I_{i_1 \dots i_m}(x, \sigma)) = f(I_{i_1 \dots i_m}(x', \sigma'))$$

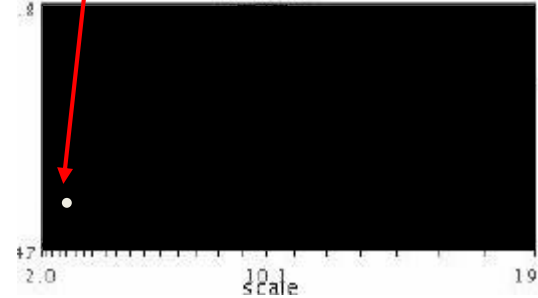
How to find corresponding patch sizes?

# Automatic Scale Selection

- Function responses for increasing scale (scale signature)



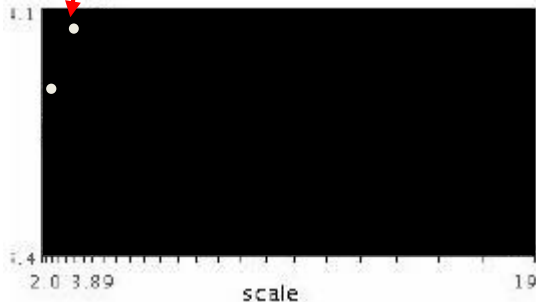
$$f(I_{i_1...i_m}(x, \sigma))$$



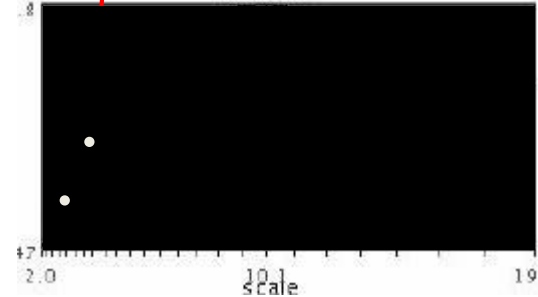
$$f(I_{i_1...i_m}(x', \sigma'))$$

# Automatic Scale Selection

- Function responses for increasing scale (scale signature)



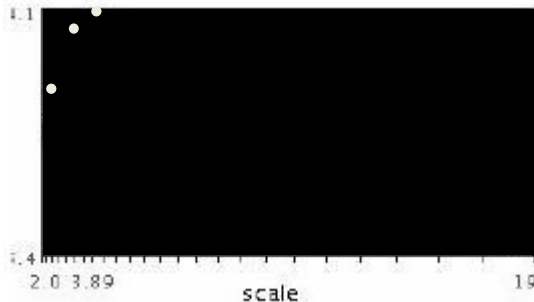
$$f(I_{i_1...i_m}(x, \sigma))$$



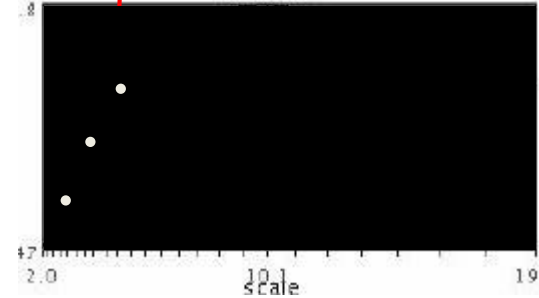
$$f(I_{i_1...i_m}(x', \sigma'))$$

# Automatic Scale Selection

- Function responses for increasing scale (scale signature)



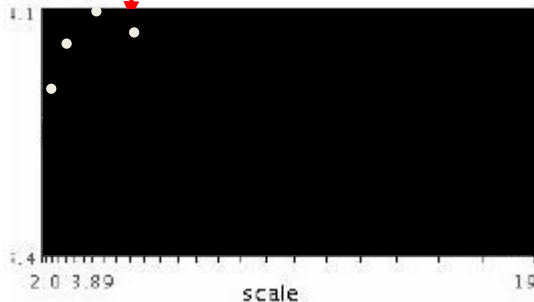
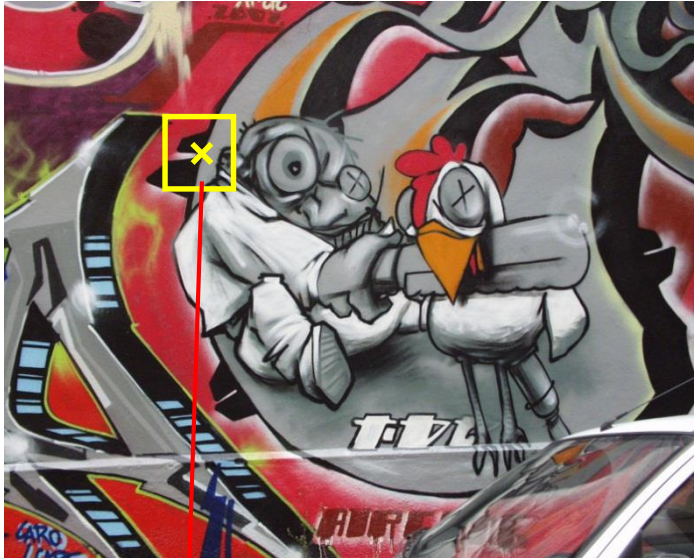
$$f(I_{i_1 \dots i_m}(x, \sigma))$$



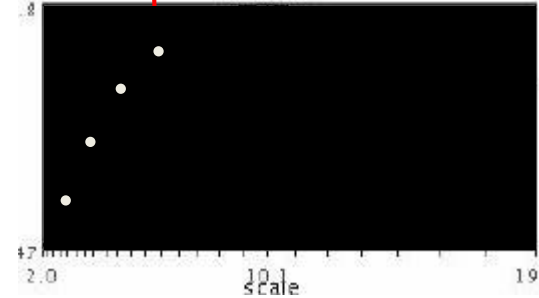
$$f(I_{i_1 \dots i_m}(x', \sigma'))$$

# Automatic Scale Selection

- Function responses for increasing scale (scale signature)



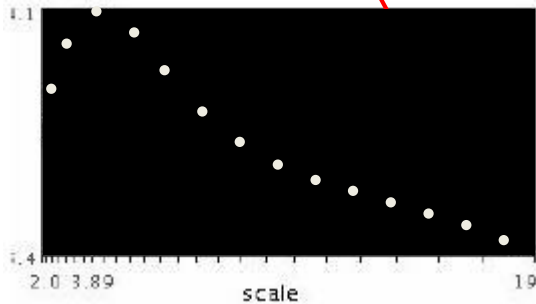
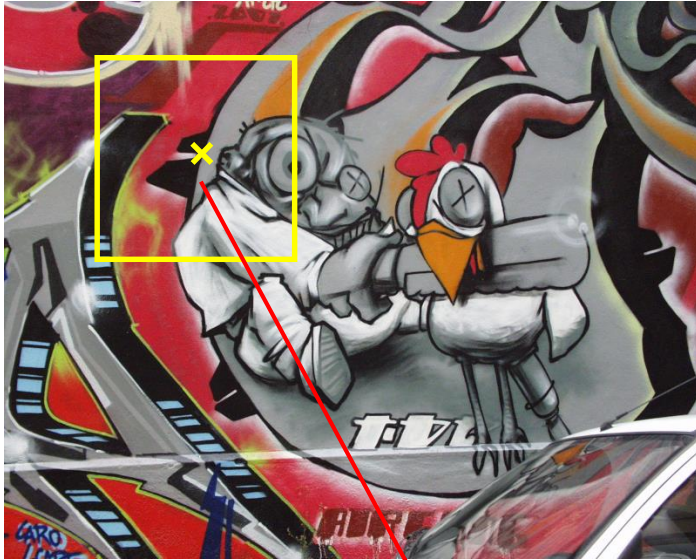
$$f(I_{i_1 \dots i_m}(x, \sigma))$$



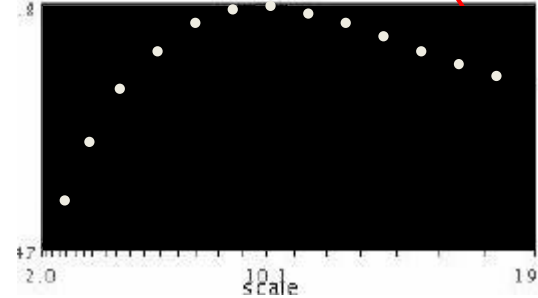
$$f(I_{i_1 \dots i_m}(x', \sigma'))$$

# Automatic Scale Selection

- Function responses for increasing scale (scale signature)



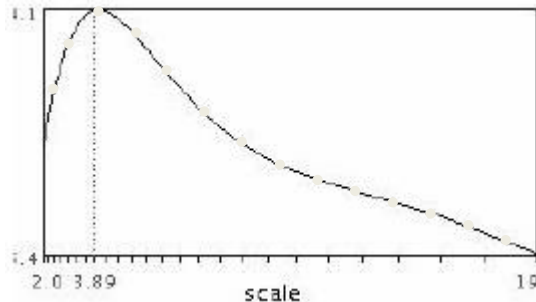
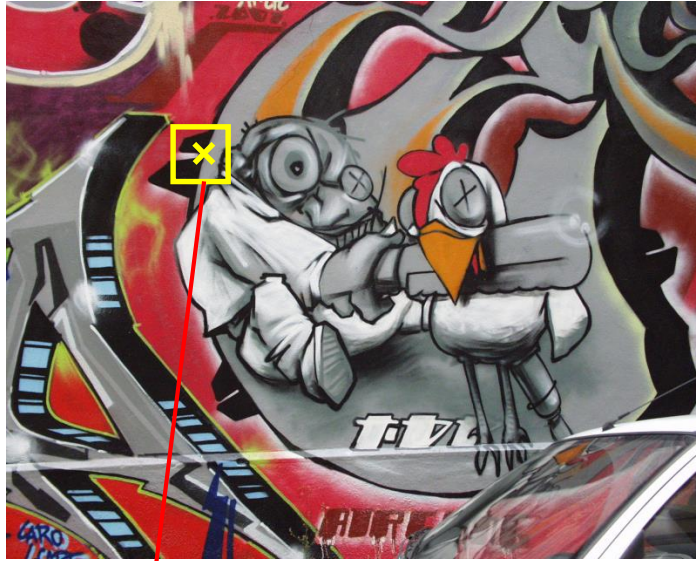
$$f(I_{i_1...i_m}(x, \sigma))$$



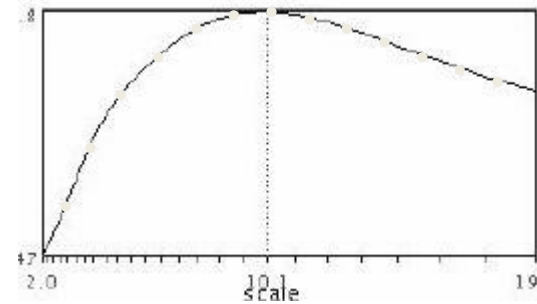
$$f(I_{i_1...i_m}(x', \sigma'))$$

# Automatic Scale Selection

- Function responses for increasing scale (scale signature)



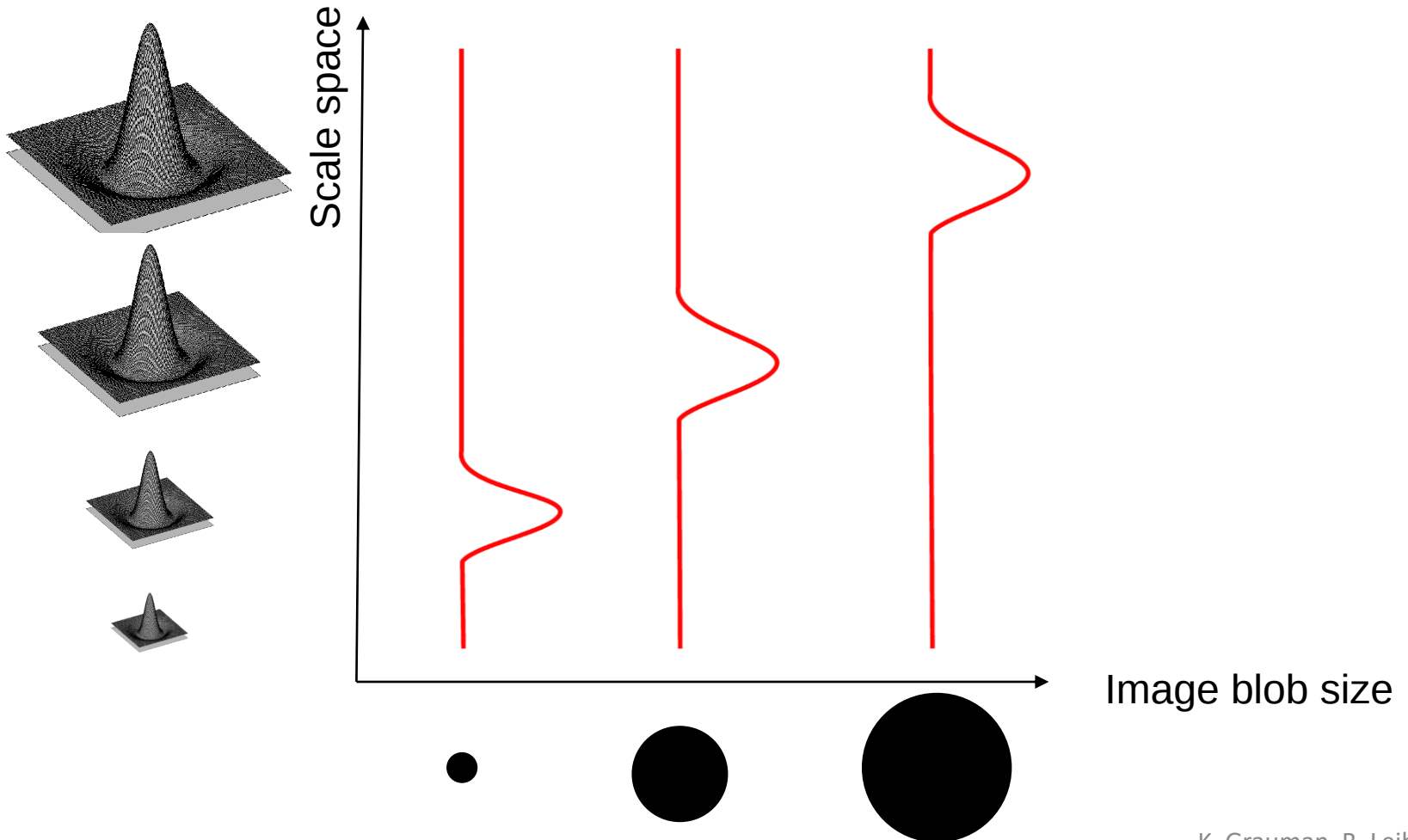
$$f(I_{i_1...i_m}(x, \sigma))$$



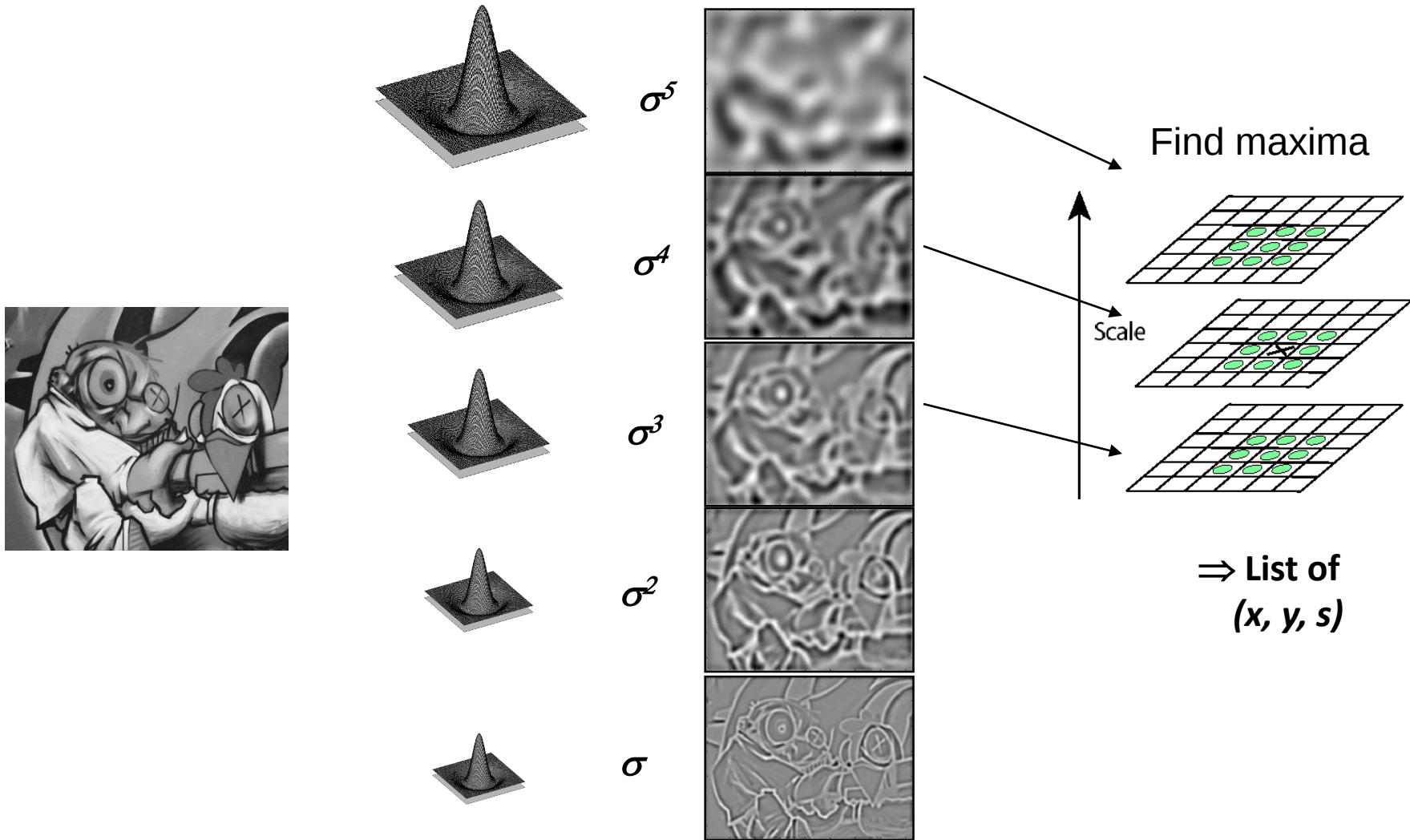
$$f(I_{i_1...i_m}(x', \sigma'))$$

# What Is A Useful Signature Function?

- “Blob” detector
  - Laplacian ( $2^{\text{nd}}$  derivative) of Gaussian (LoG)

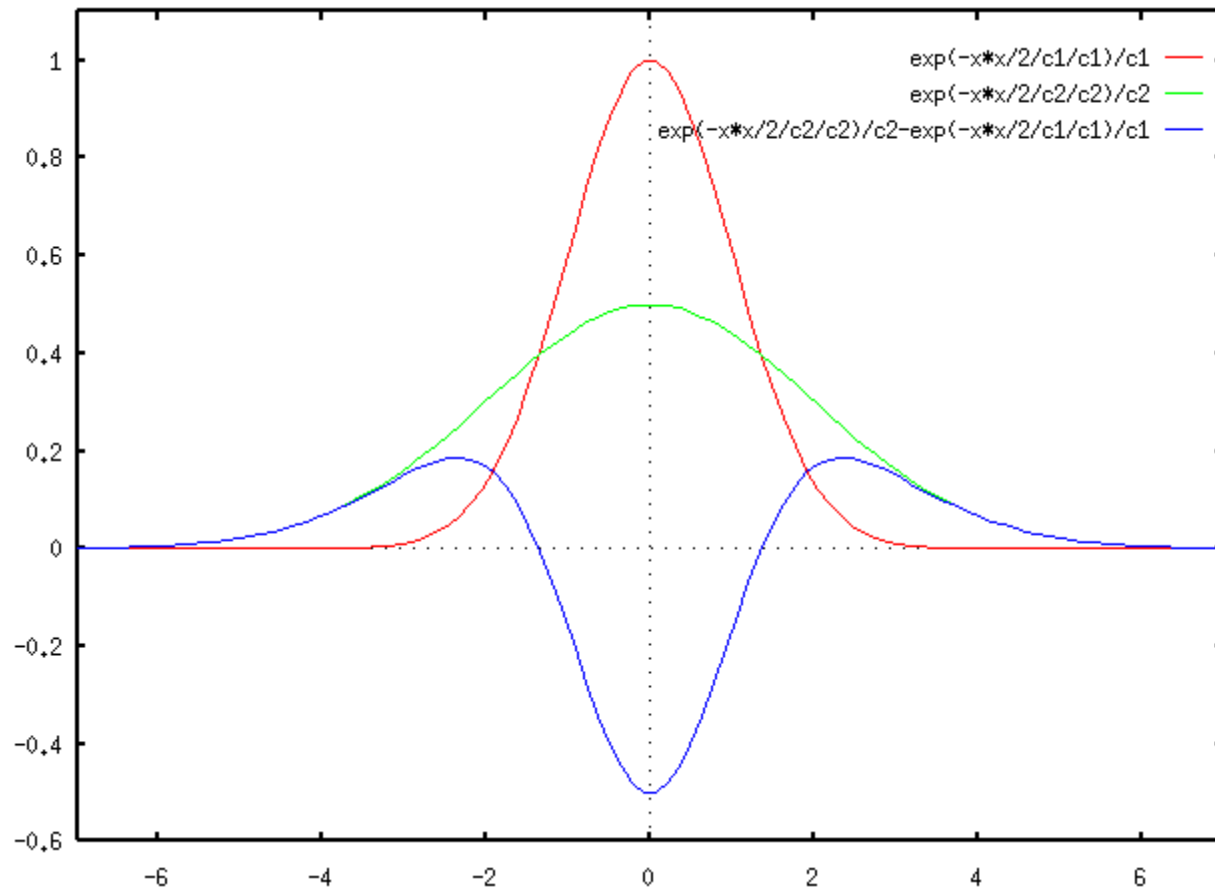


# Find local maxima in position-scale space



# Difference-of-Gaussian (DoG)

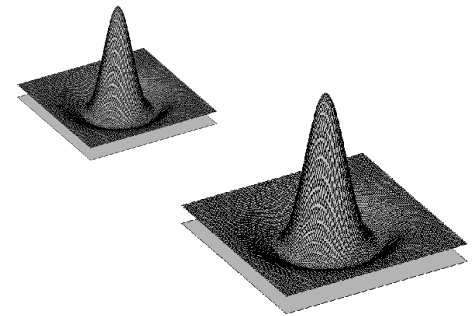
Approximate LoG with DoG (!)



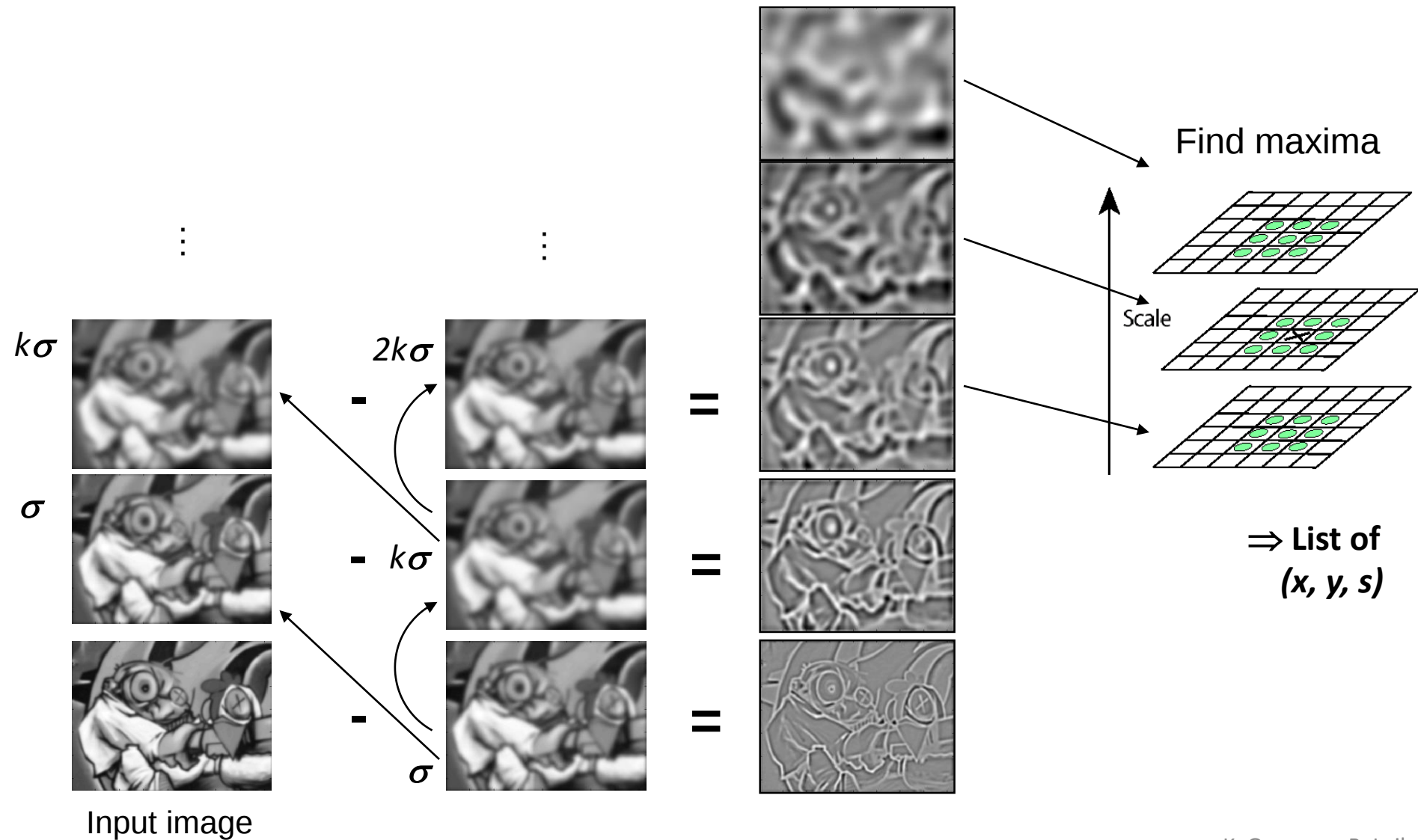
# Difference-of-Gaussian (DoG)

Approximate LoG with DoG (!)

1. Blur image with  $\sigma$  Gaussian kernel
2. Blur image with  $k\sigma$  Gaussian kernel
3. Subtract 2. from 1.

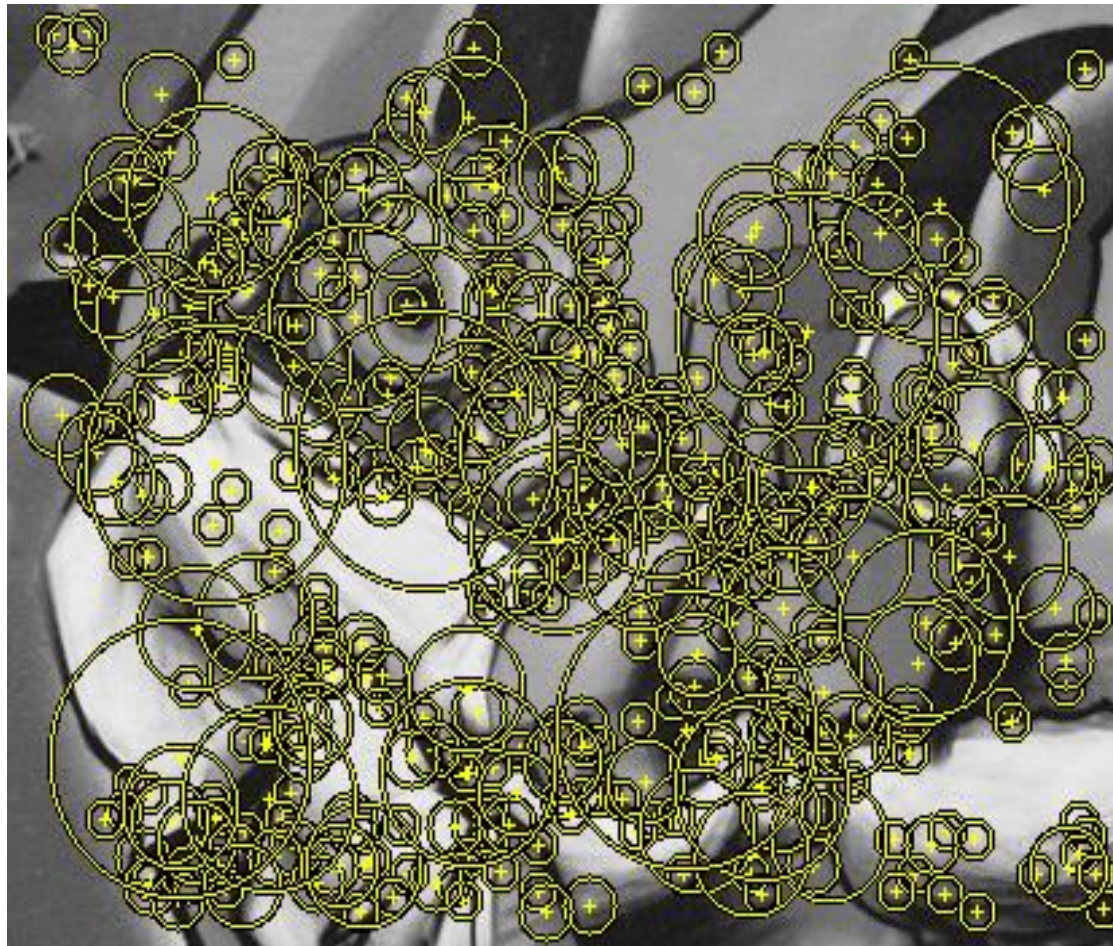


# Find local maxima in position-scale space of Difference-of-Gaussian



# Results: Difference-of-Gaussian

- Larger circles = larger scale
- Descriptors with maximal scale response

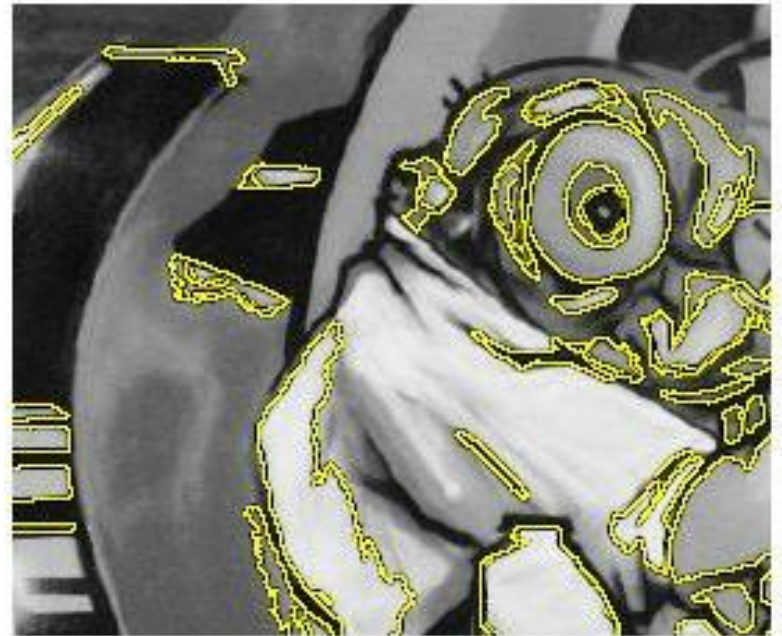


# Maximally Stable Extremal Regions [Matas '02]

- Based on Watershed segmentation algorithm
- Select regions that stay stable over a large parameter range



# Example Results: MSER



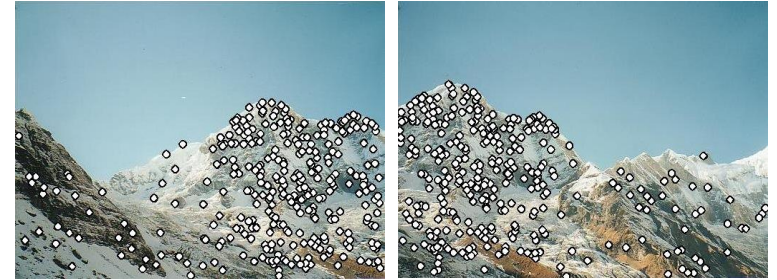
# Local Image Descriptors

Read Szeliski 4.1

# Local features: main components

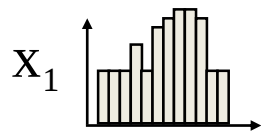
## 1) Detection:

Find a set of distinctive key points.

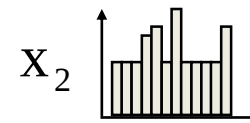
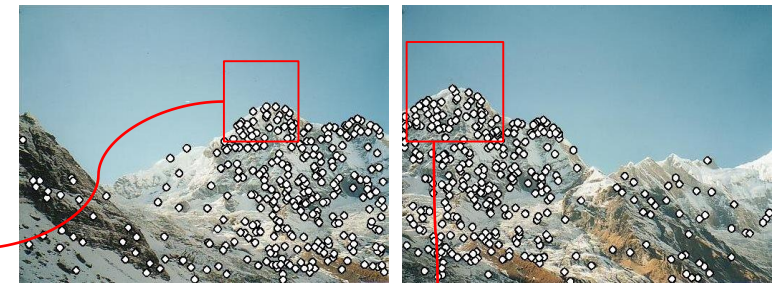


## 2) Description:

Extract feature descriptor around each interest point as vector.



$$\mathbf{x}_1 = [x_1^{(1)}, \dots, x_d^{(1)}]$$

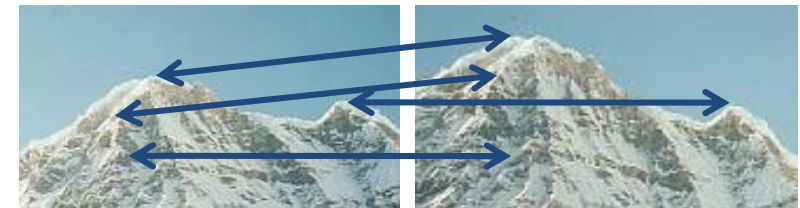


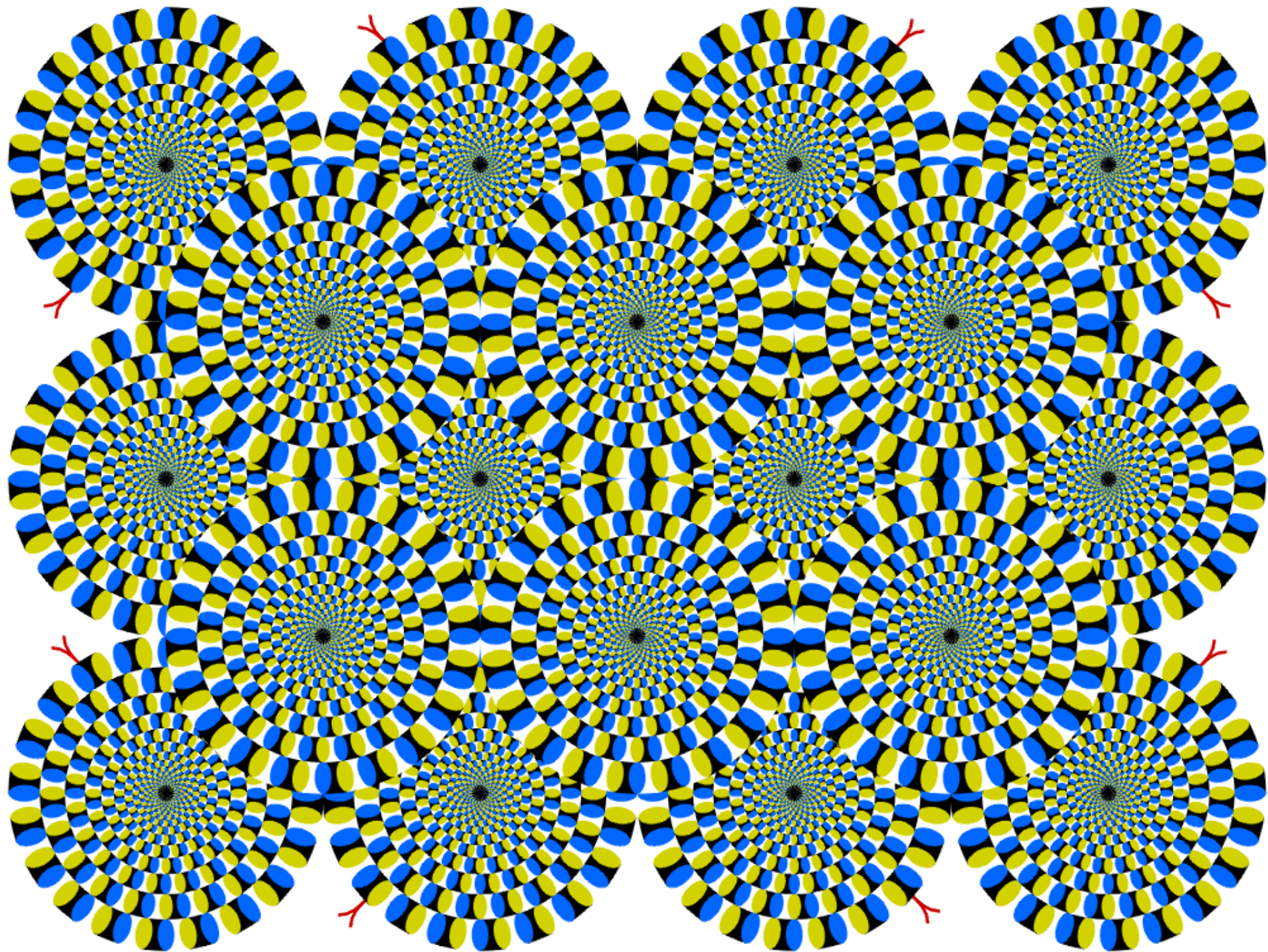
$$\mathbf{x}_2 = [x_1^{(2)}, \dots, x_d^{(2)}]$$

## 3) Matching:

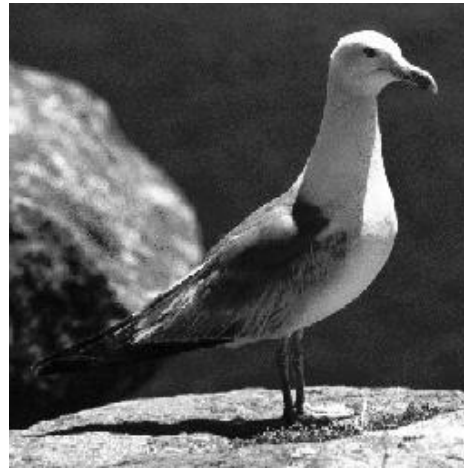
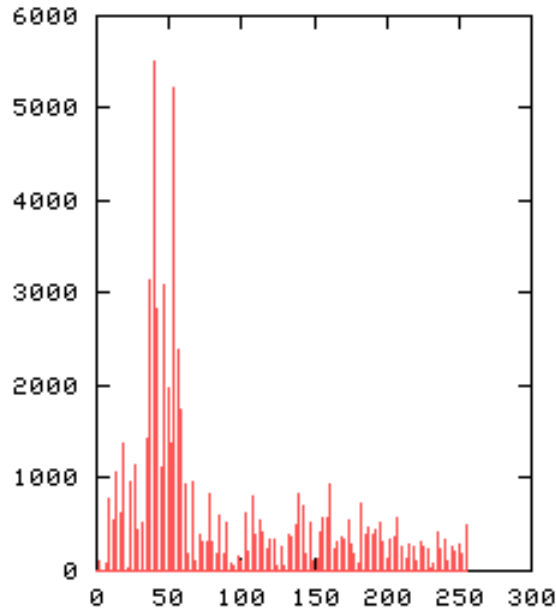
Compute distance between feature vectors to find correspondence.

$$d(\mathbf{x}_1, \mathbf{x}_2) < T$$





# Image Representations: Histograms



Global histogram to represent distribution of features

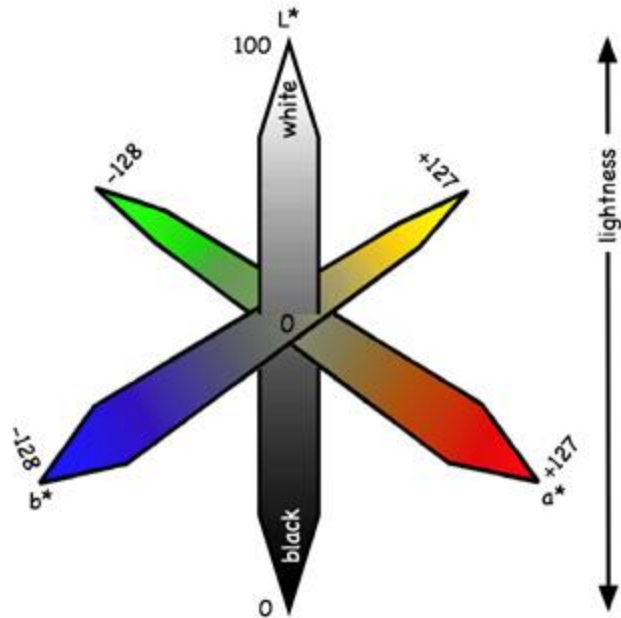
– Color, texture, depth, ...

Local histogram per detected point

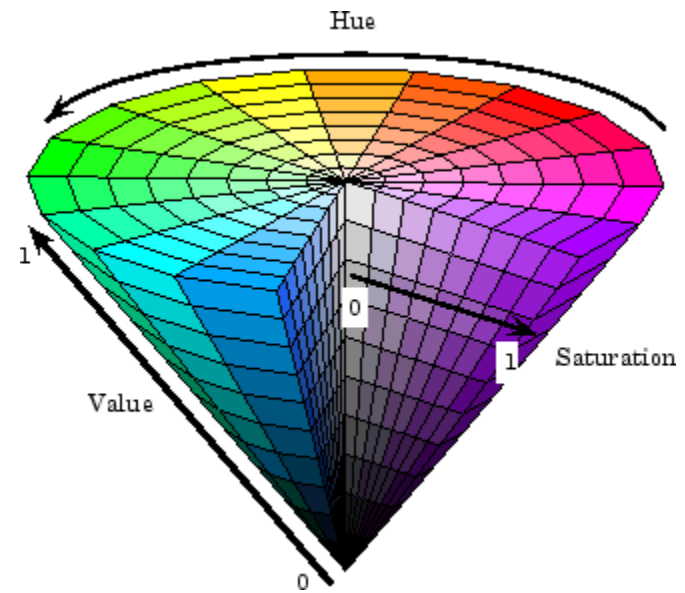


# For what things do we compute histograms?

- Color



$L^*a^*b^*$  color space

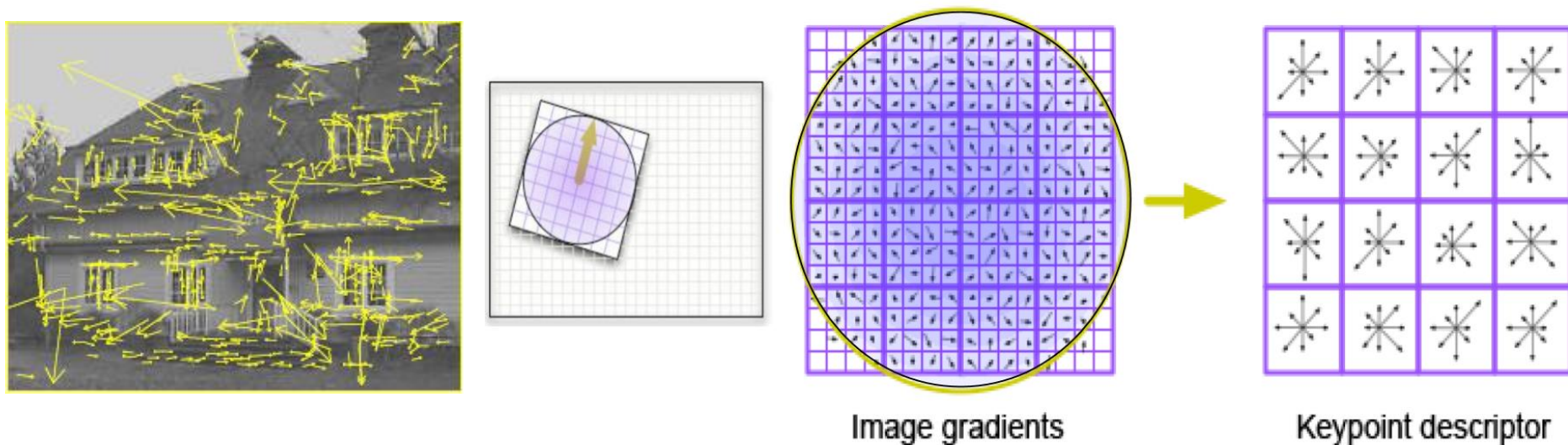


HSV color space

- Model local appearance

# For what things do we compute histograms?

- Texture
- Local histograms of oriented gradients
- SIFT: Scale Invariant Feature Transform
  - Extremely popular (40k citations)



SIFT – Lowe IJCV 2004

# SIFT

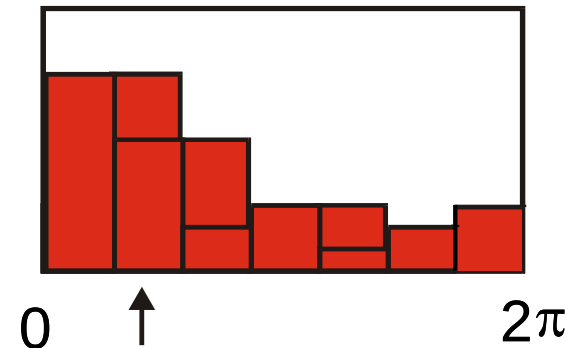
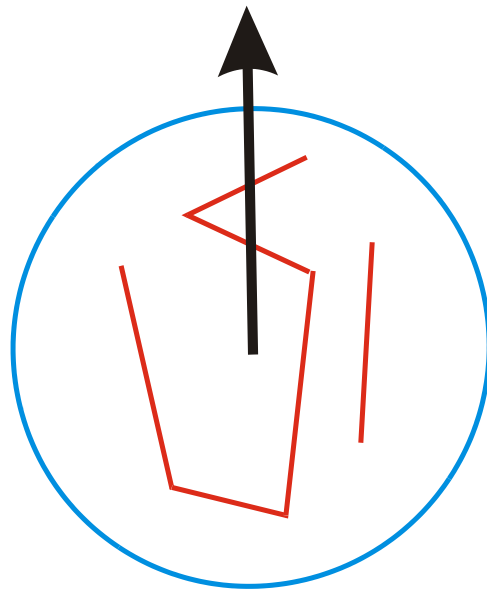
- Find Difference of Gaussian scale-space extrema
- Post-processing
  - Position interpolation
  - Discard low-contrast points
  - Eliminate points along edges

# SIFT

- Find Difference of Gaussian scale-space extrema
- Post-processing
  - Position interpolation
  - Discard low-contrast points
  - Eliminate points along edges
- Orientation estimation

# SIFT Orientation Normalization

- Compute orientation histogram
- Select dominant orientation  $\theta$
- Normalize: rotate to fixed orientation

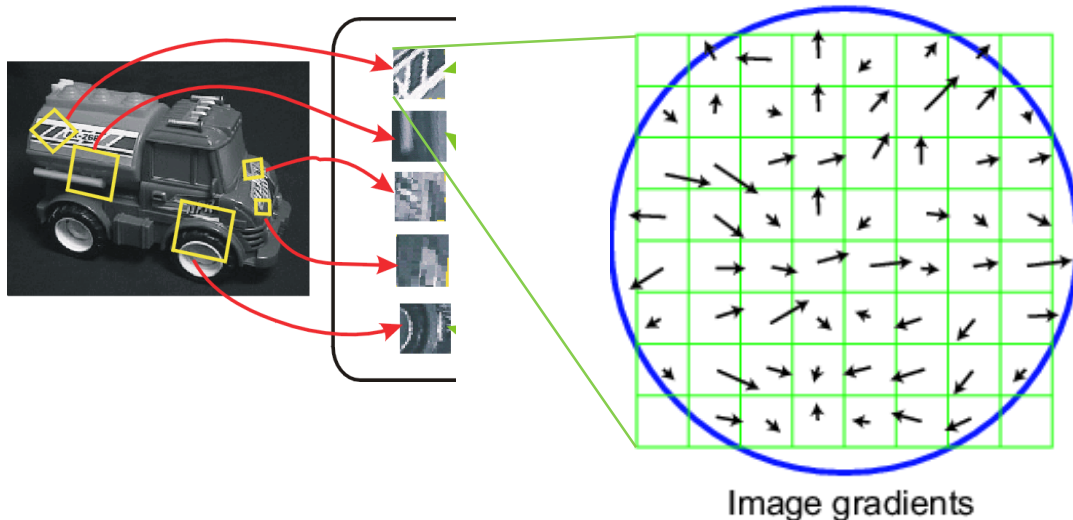


# SIFT

- Find Difference of Gaussian scale-space extrema
- Post-processing
  - Position interpolation
  - Discard low-contrast points
  - Eliminate points along edges
- Orientation estimation
- Descriptor extraction
  - Motivation: We want some sensitivity to spatial layout, but not too much, so blocks of histograms give us that.

# SIFT descriptor formation

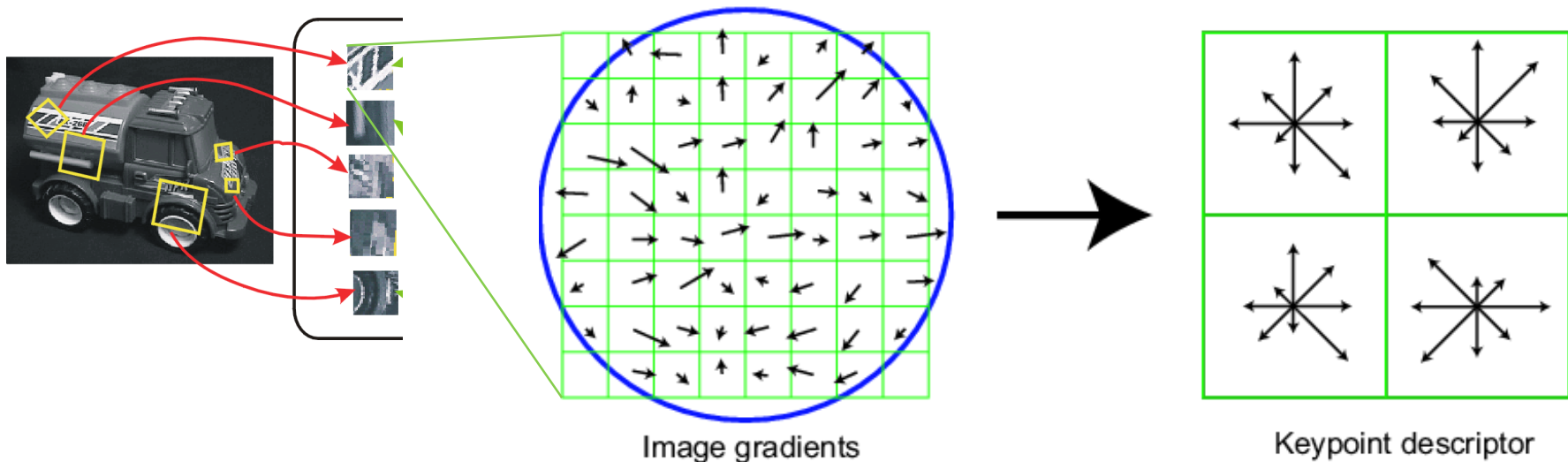
- Compute on local  $16 \times 16$  window around detection.
- Rotate and scale window according to discovered orientation  $\theta$  and scale  $\sigma$  (gain invariance).
- Compute gradients weighted by a Gaussian of variance half the window (for smooth falloff).



Actually  $16 \times 16$ , only showing  $8 \times 8$

# SIFT vector formation

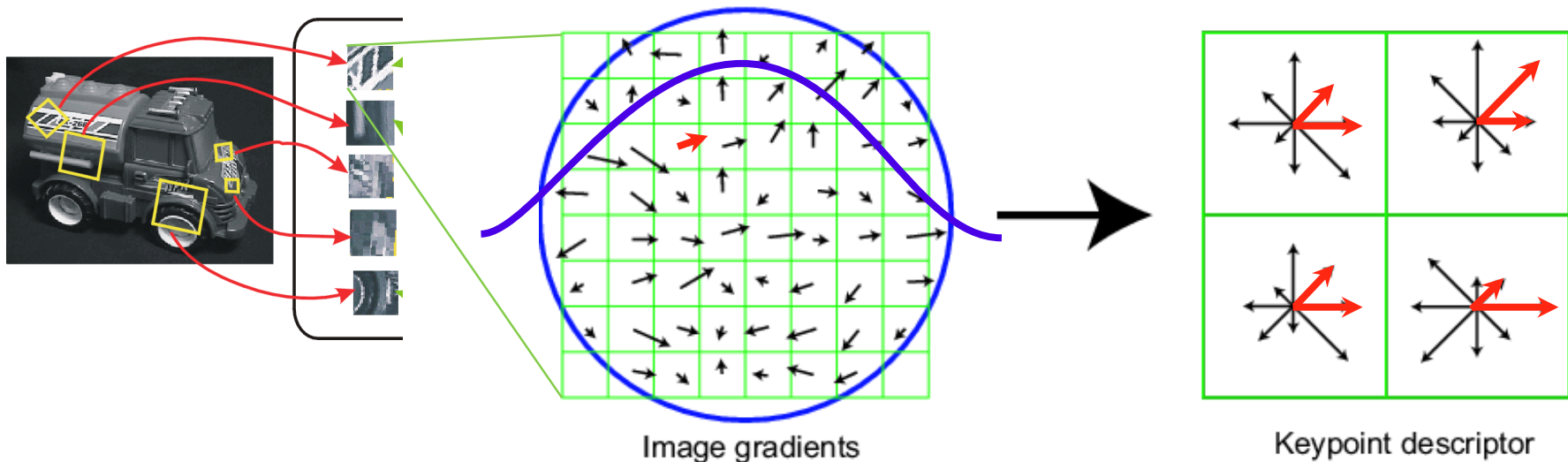
- 4x4 array of gradient orientation histograms weighted by gradient magnitude.
- Bin into 8 orientations x 4x4 array = 128 dimensions.



Showing only 2x2 here but is 4x4

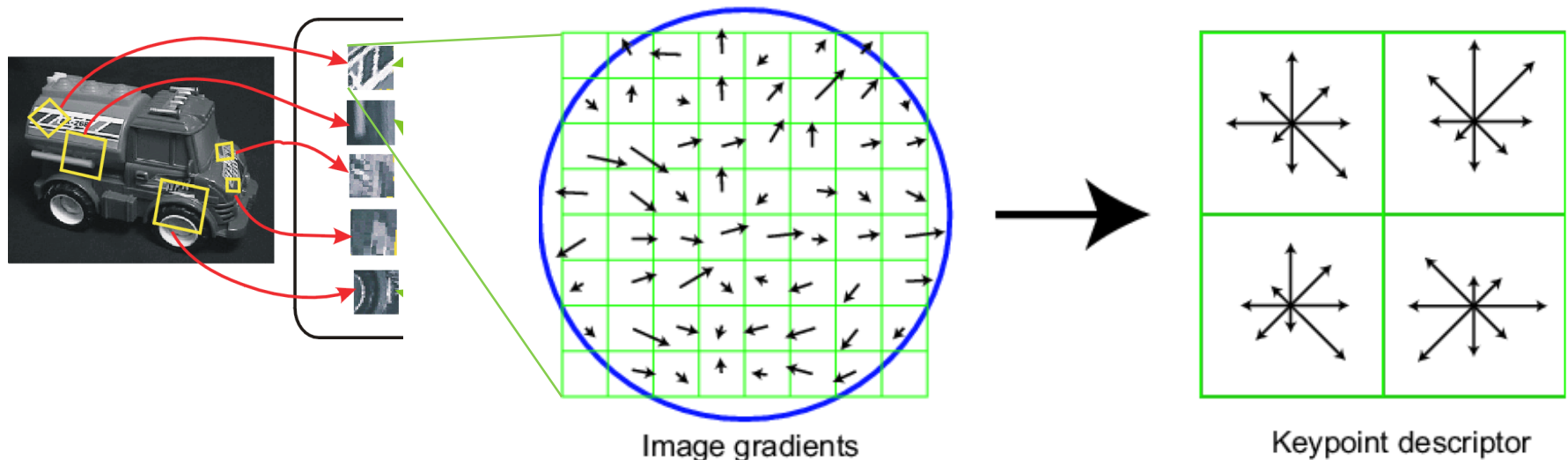
# Ensure smoothness

- Gaussian weight the magnitudes
- Trilinear interpolation
  - A given gradient contributes to 8 bins:  
4 in space x 2 in orientation



# Reduce effect of illumination

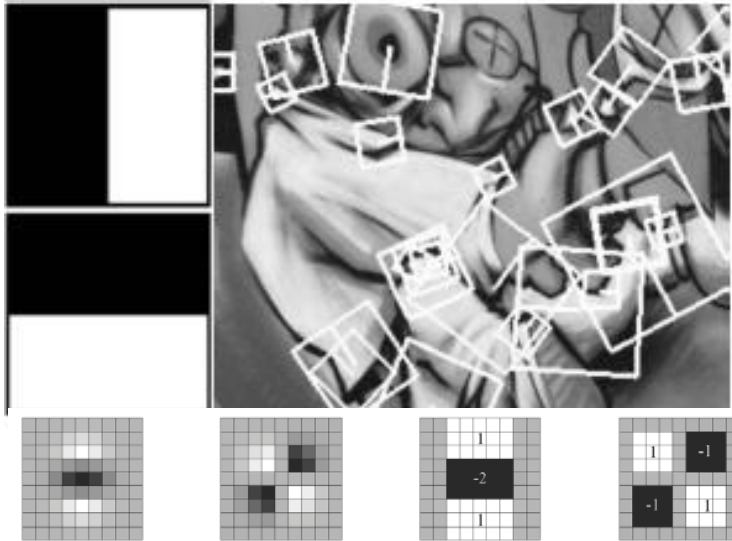
- 128-dim vector normalized to 1
- Threshold gradient magnitudes to avoid excessive influence of high gradients
  - After normalization, clamp gradients  $> 0.2$
  - Renormalize



# SIFT-like descriptor in Project 2

- SIFT is hand designed based on intuition
- You implement your own SIFT-like descriptor
- May be some trial and error
- Feel free to look at papers / resources for inspiration

# Local Descriptors: SURF



## Fast approximation of SIFT idea

Efficient computation by 2D box filters & integral images

⇒ 6 times faster than SIFT

Equivalent quality for object identification

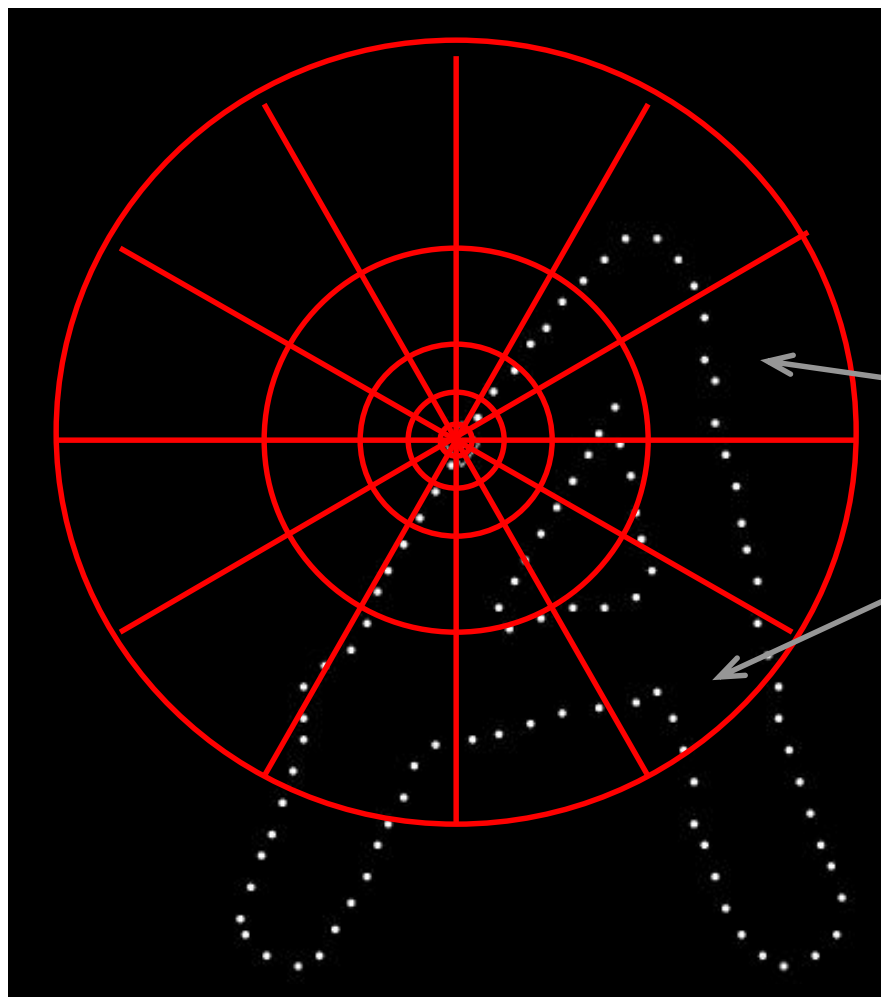
## GPU implementation available

Feature extraction @ 200Hz

(detector + descriptor, 640×480 img)

<http://www.vision.ee.ethz.ch/~surf>

# Local Descriptors: Shape Context



**Count the number of points  
inside each bin, e.g.:**

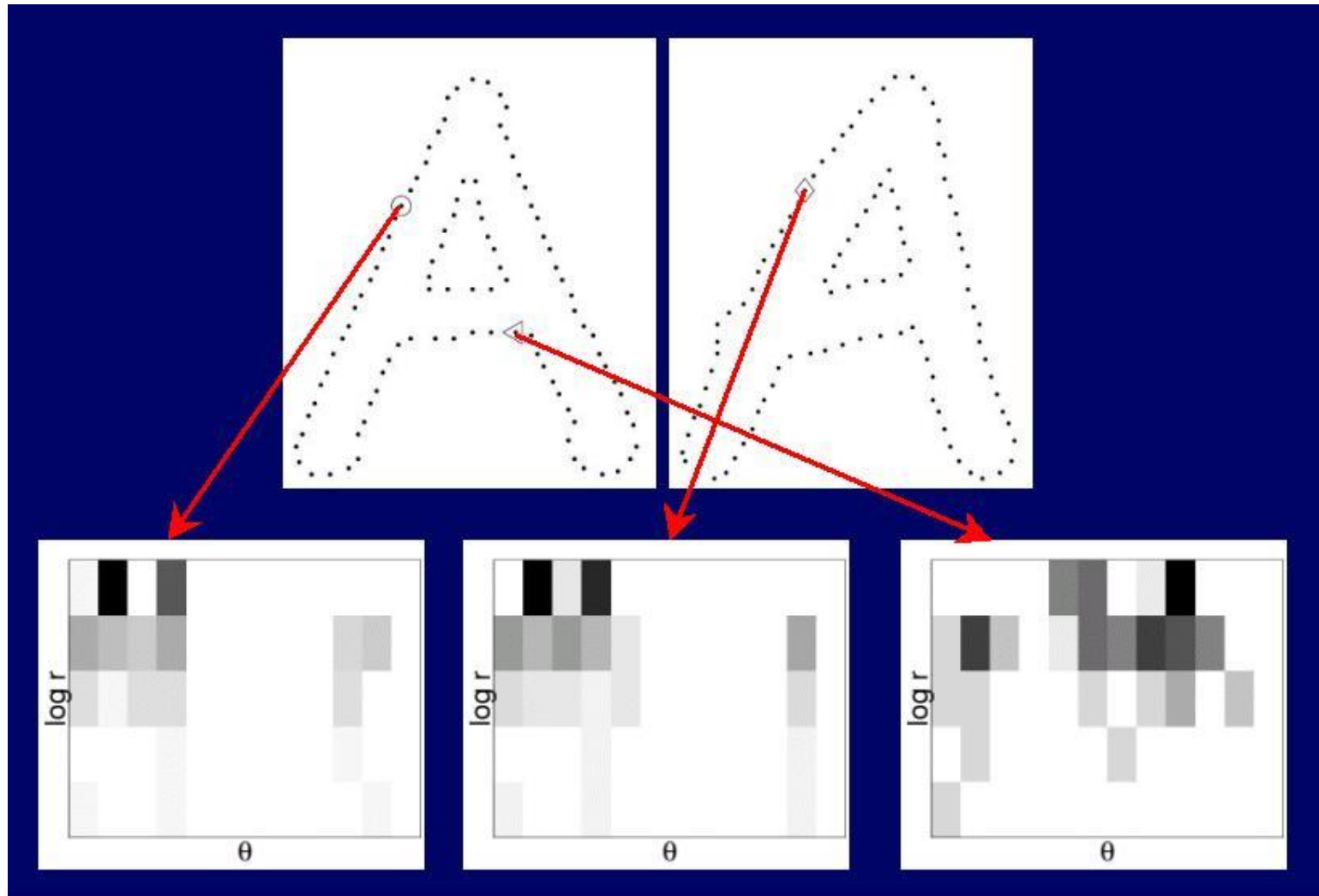
**Count = 4**

**⋮**

**Count = 10**

**Log-polar binning: more  
precision for nearby points,  
more flexibility for farther  
points.**

# Shape Context Descriptor



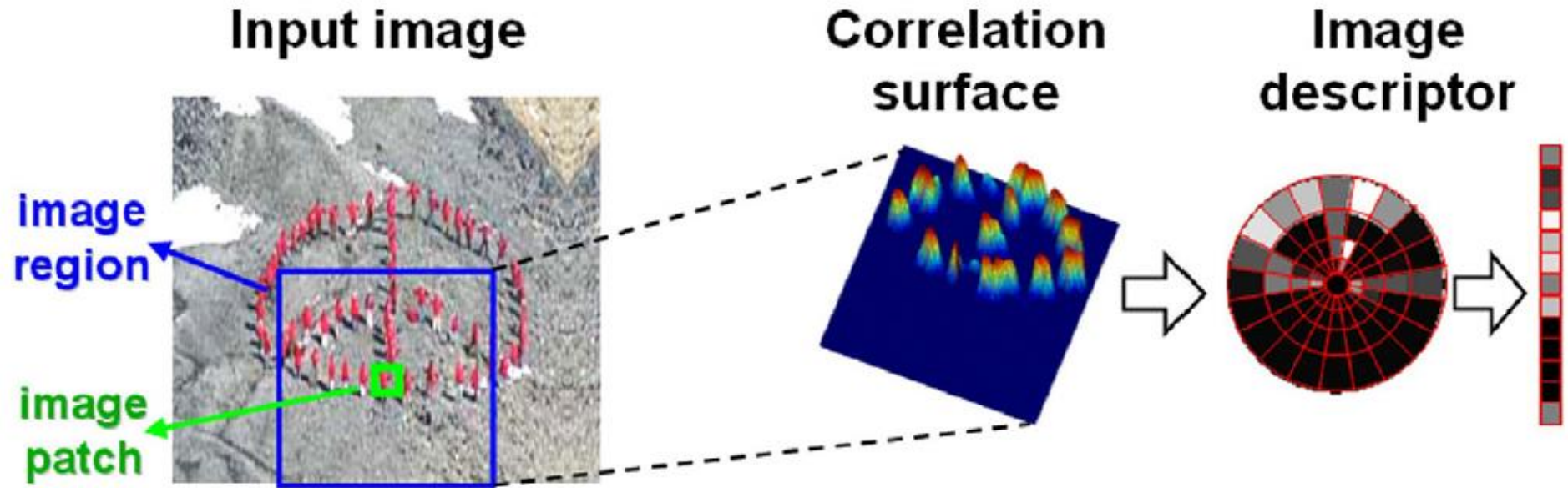
# Self-similarity Descriptor



Figure 1. *These images of the same object (a heart) do NOT share common image properties (colors, textures, edges), but DO share a similar geometric layout of local internal self-similarities.*

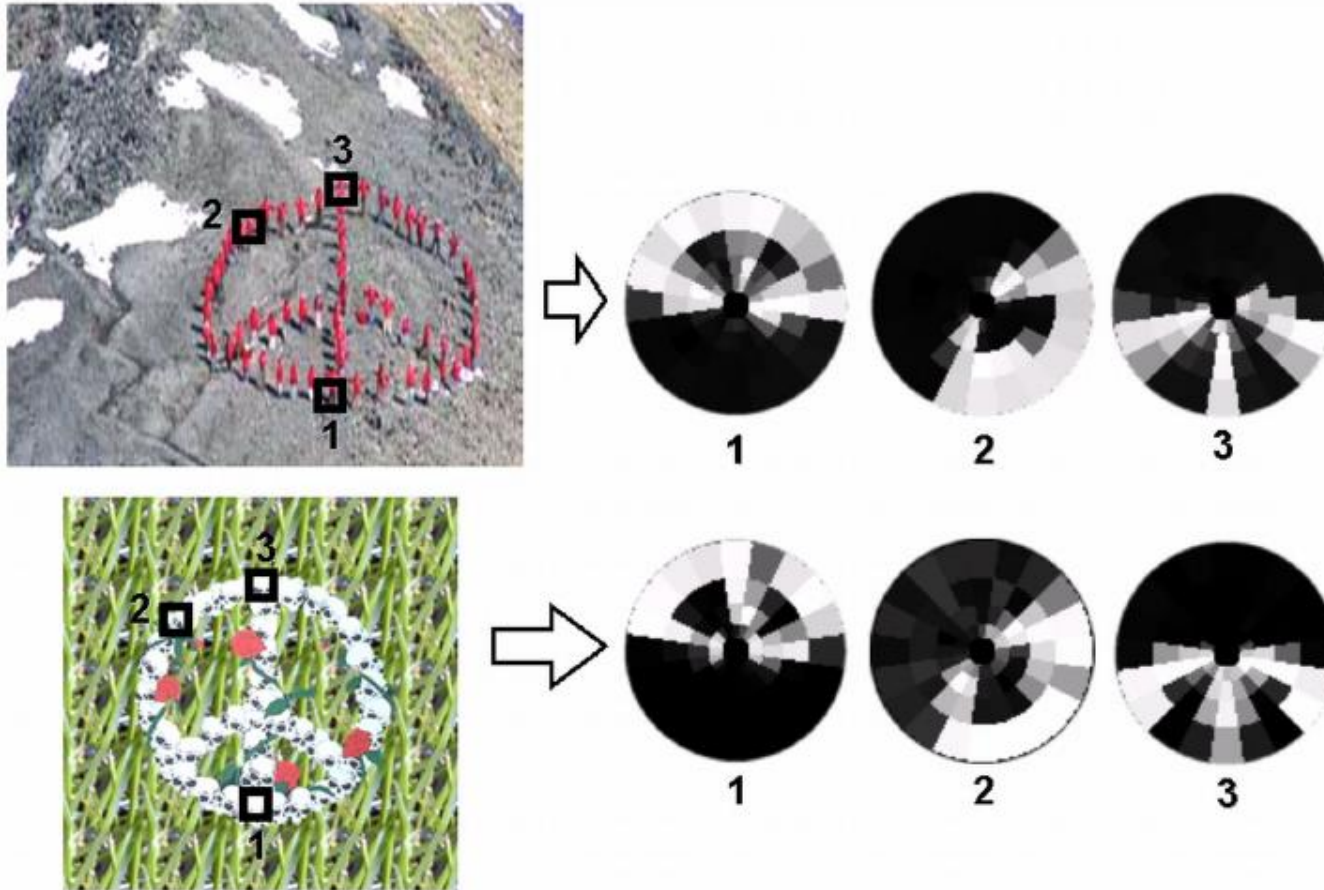
Matching Local Self-Similarities across Images  
and Videos, Shechtman and Irani, 2007

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Matching Local Self-Similarities across Images and Videos, Shechtman and Irani, 2007

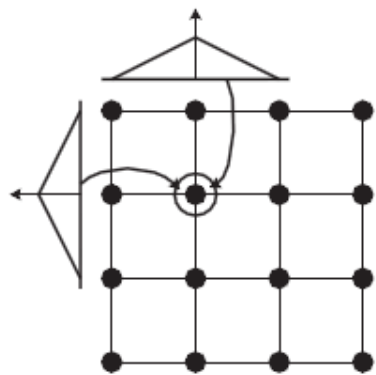
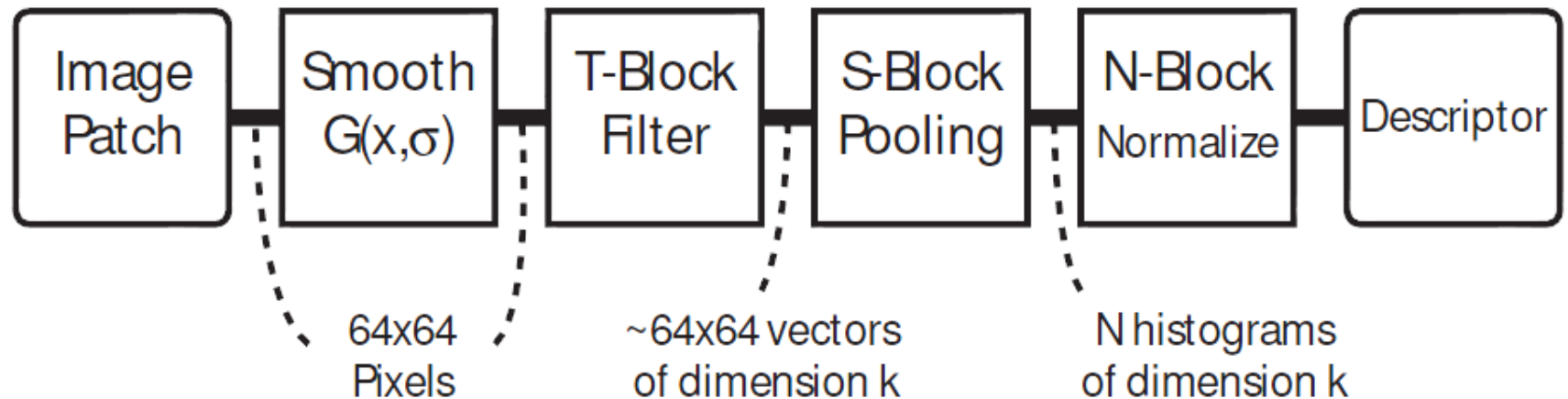
# Self-similarity Descriptor



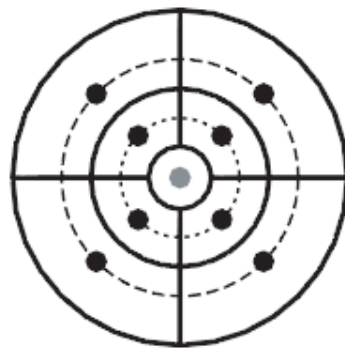
Matching Local Self-Similarities across Images  
and Videos, Shechtman and Irani, 2007

# Learning Local Image Descriptors

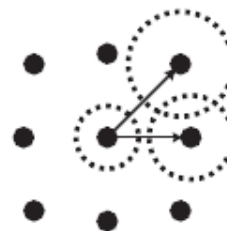
Winder and Brown, 2007



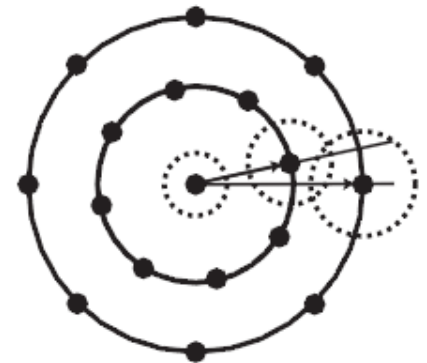
S1: SIFT grid with bilinear weights



S2: GLOH polar grid with bilinear radial and angular weights



S3: 3x3 grid with Gaussian weights



S4: 17 polar samples with Gaussian weights

# Local Descriptors

- Most features can be thought of as templates, histograms (counts), or combinations
- The ideal descriptor should be
  - Robust
  - Distinctive
  - Compact
  - Efficient
- Most available descriptors focus on edge/gradient information
  - Capture texture information
  - Color rarely used

# Available at a web site near you...

- Many local feature detectors have executables available online:
  - <http://www.robots.ox.ac.uk/~vgg/research/affine>
  - <http://www.cs.ubc.ca/~lowe/keypoints/>
  - <http://www.vision.ee.ethz.ch/~surf>

# Next time

- Feature matching, Hough Transform