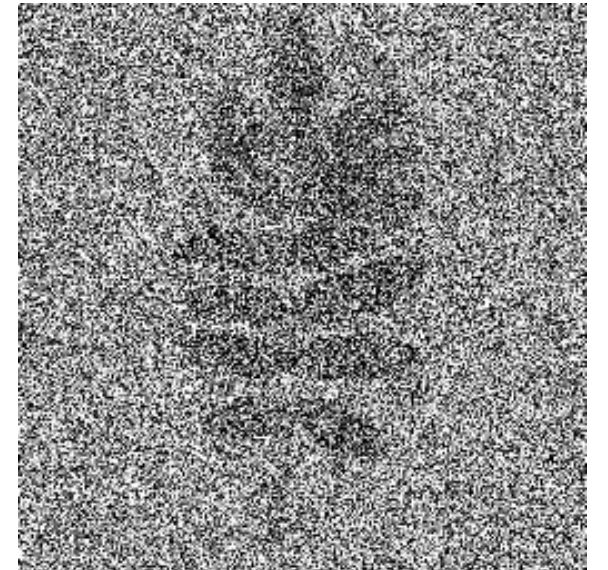
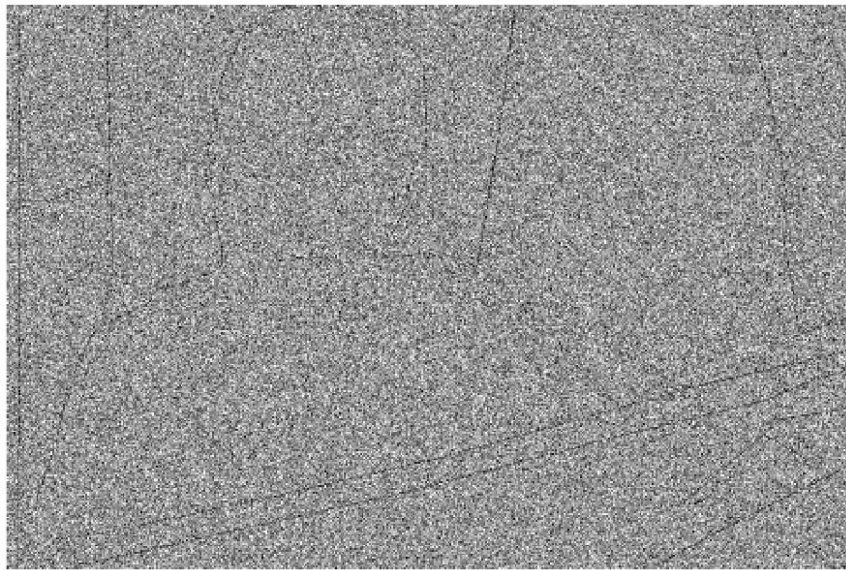


# Probabilistic Scene Grammars: A General-Purpose Framework for Scene Understanding

Jeroen Chua

Advisor: Pedro Felzenszwalb



# Why a general-purpose framework?

- Improvements can boost performance on many scene understanding tasks simultaneously
- Less engineering/research work for future scene understanding tasks
- Scene understanding tasks inform each other
- Scientifically interesting: can all (most) of scene understanding be understood as the same fundamental problem?

# This thesis

- **Motivation** for a general scene understanding framework
- **Background/related work**
- • **Representation** for general scene understanding tasks
- • Efficient **approximate inference algorithm**
  - **Notes** on other possible inference algorithms
  - **Connections** to related work
- • **Learning algorithm** to estimate model parameters
- • **Experimental evaluation**
- • **Extensions** for larger/more complex tasks
  - **Directions** for future research

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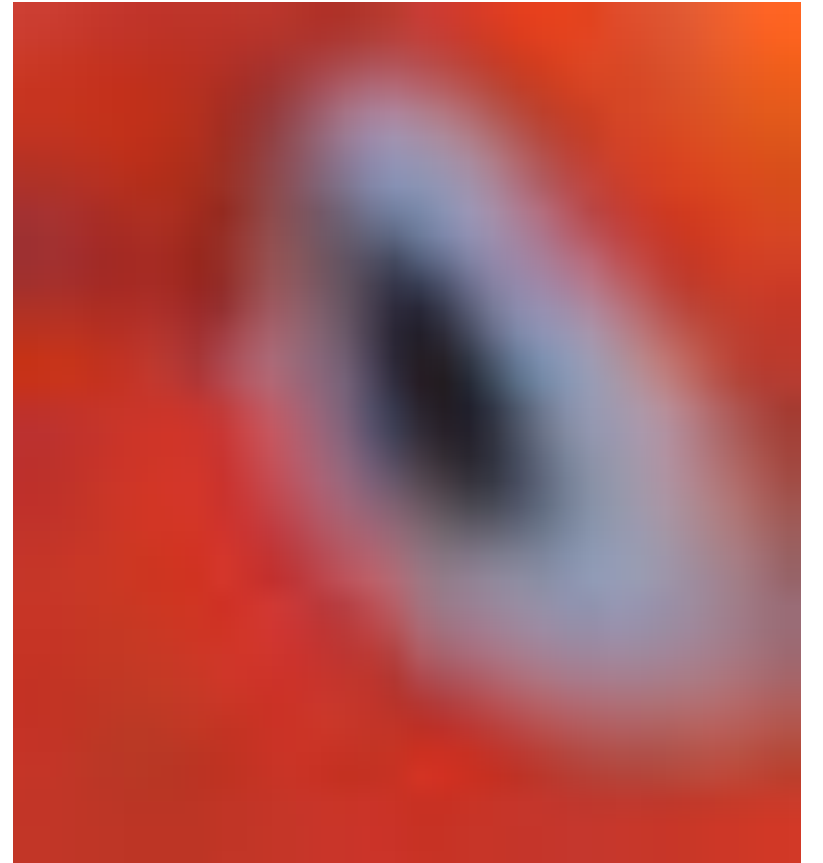
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Contextual information is often useful

Context helps for \_\_\_\_\_



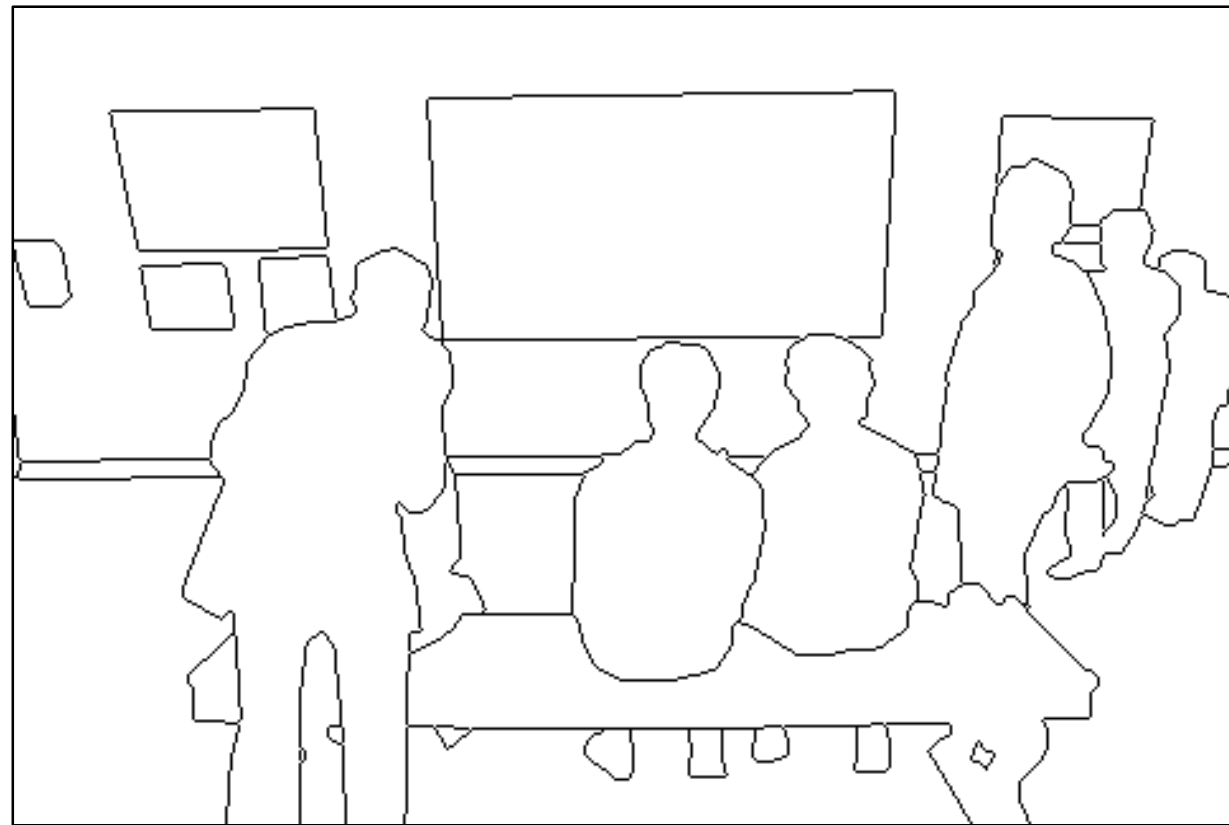
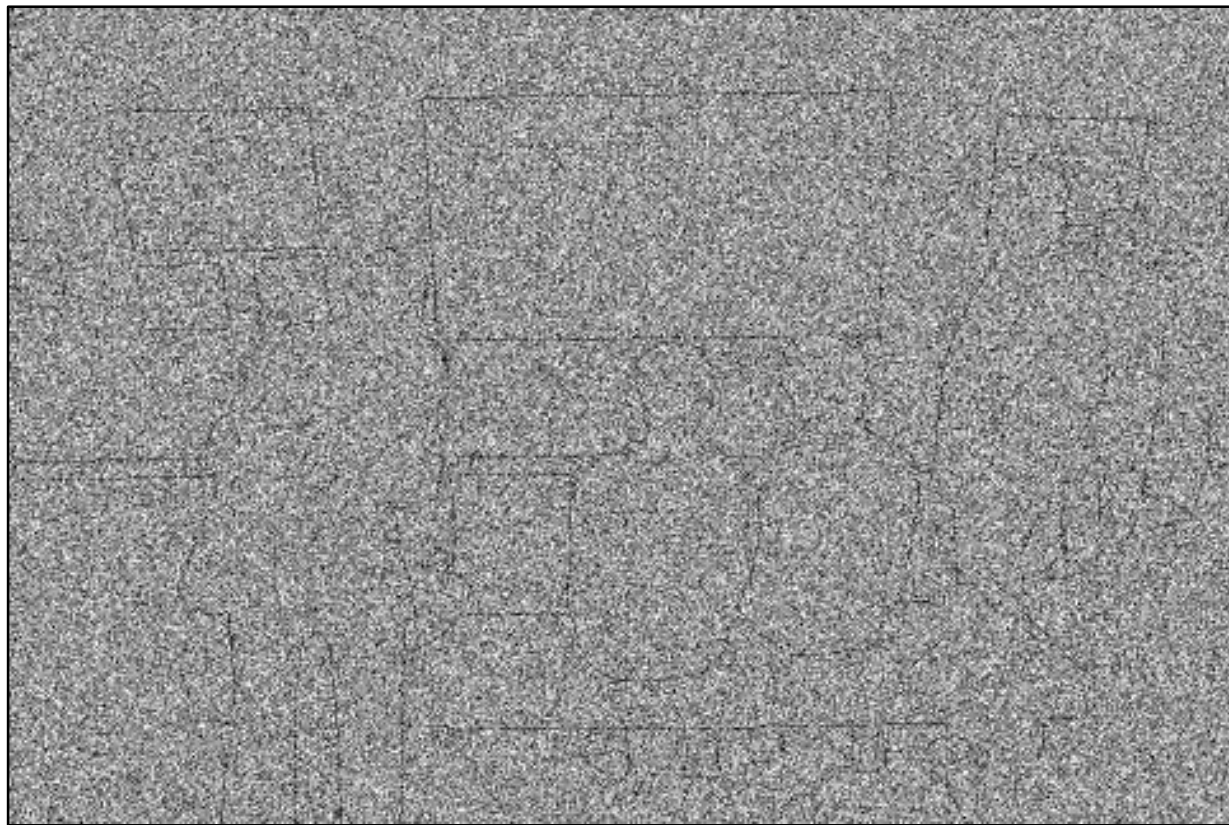
# Context helps for object recognition



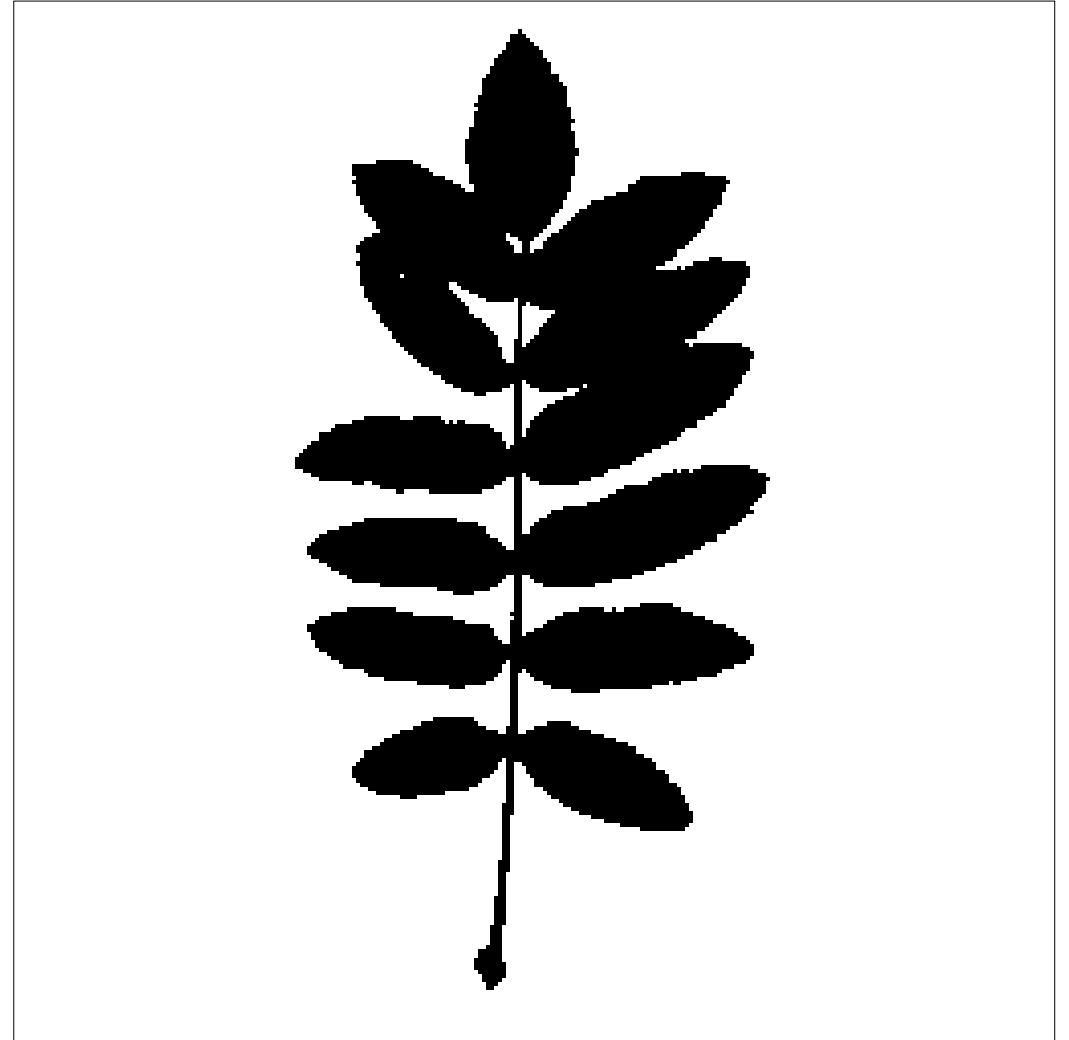
# Context helps for object recognition



# Context helps for **contour detection**



# Context helps for image segmentation



# Related work

- Contextual information
  - Oliva and Torralba[1,2], Efros [3]
  - Empirical studies [4]
  - Gestalt Theory [5]
- Motivation
  - Probabilistic Programming Languages [6,7,8]
- Modelling
  - Pictorial Structures [8]
  - DPM [9]
  - “Markov backbone” model [10]
- Probabilistic inference for compositional models
  - Markov-chain Monte Carlo
  - Heuristics

[1] “Modelling the shape of the scene: a holistic representation of the spatial envelope”, IJCV 2001

[2] “The role of context in object recognition”, Trends in Cognitive Sciences, 2007

[3] “Unsupervised visual representation learning by context prediction”, ICCV 2015

[4] “An empirical study of context in object detection”, CVPR 2009

[5] Vision science: Photons to phenomenology, volume 1. MIT press, 1999

[6] “Picture: A probabilistic programming language for scene perception”, CVPR 2015

[7] “Edward: A library for probabilistic modeling, inference, and criticism”, arXiv 2016

[8] “The design and Implementation of Probabilistic Programming Languages”, <http://dippl.org> 2014

[9] “Pictorial Structures for object recognition”, IJCV 2005

[10] “Object detection with grammar models”, NIPS 2011

[11] “Context and hierarchy in a probabilistic image model”, CVPR 2006

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**PSG**

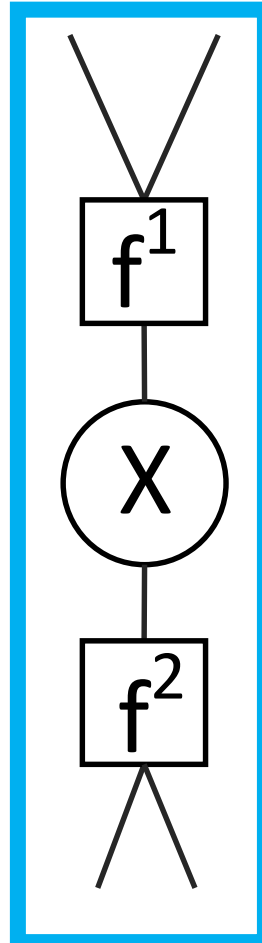


# The Probabilistic Scene Grammar Framework

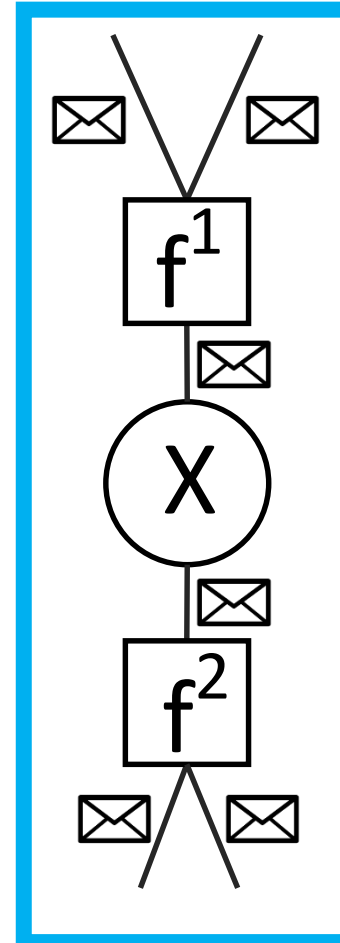
Probabilistic Scene Grammar



Factor graph



Inference



Learning



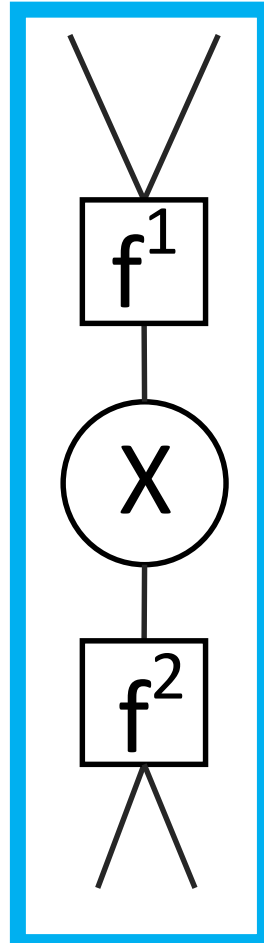


# The Probabilistic Scene Grammar Framework

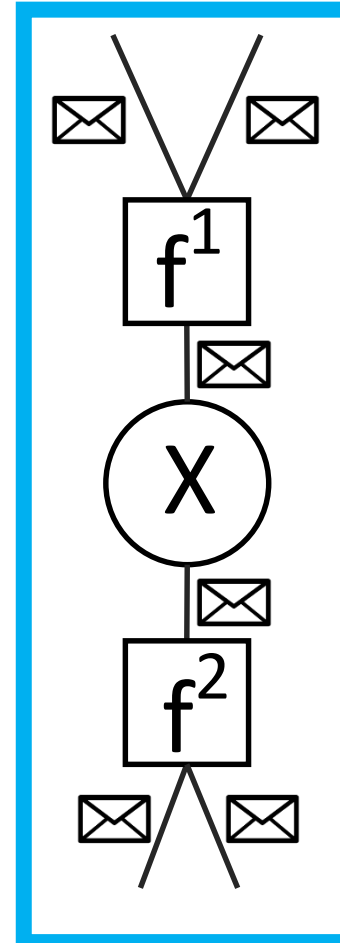
Probabilistic Scene Grammar



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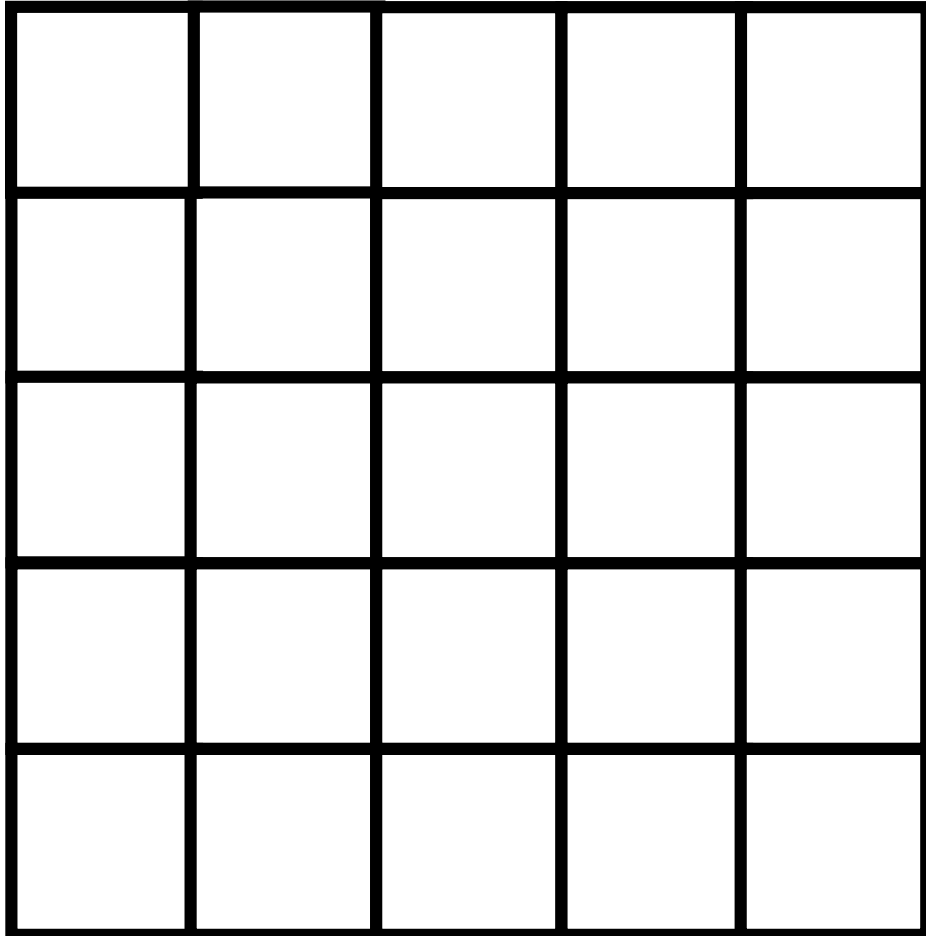


# Probabilistic Scene Grammars

- Context-free stochastic grammar
  - Symbols, *eg. {Face, eye, conversation}*
  - Pose space, *eg. {location, orientation, scale}*
  - Production rules, *eg. Face  $\rightarrow$  {Eye, Eye, Nose, Mouth}*
  - Production rule probabilities
- Geometric relationships between objects/parts
- “Self-rooting” parameter

# Generative example: Faces

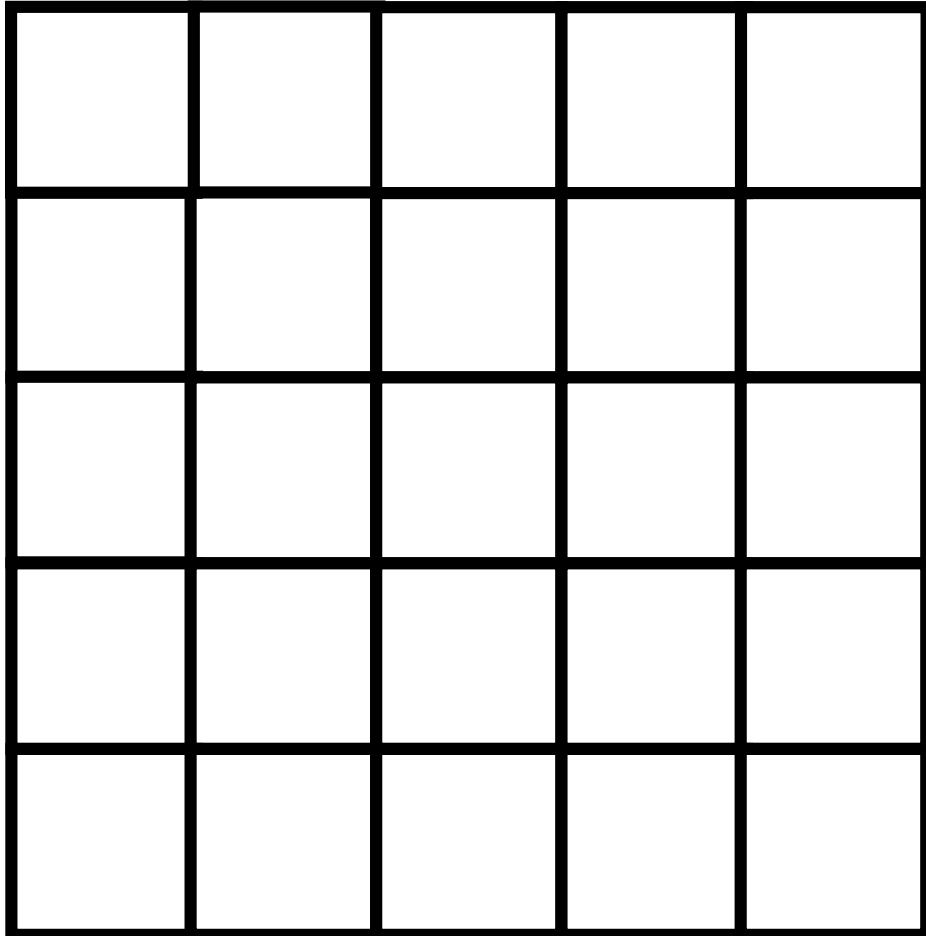
Symbols: Face (F), Eye (E), Nose (N), Mouth (M), Eyelashes (L)



Rule	P(rule)	Spatial distribution type
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# Generative example: Faces

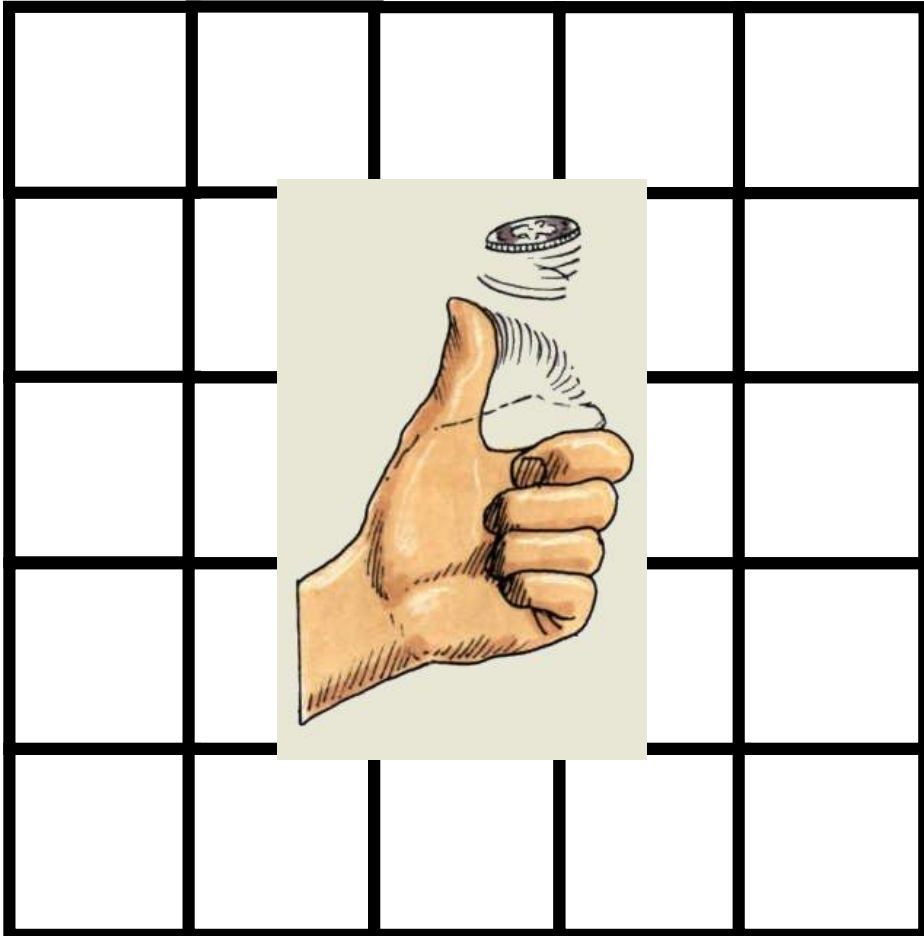
Symbols: **Face (F)**, Eye (E), Nose (N), Mouth (M), Eyelashes (L)



Rule	P(rule)	Spatial distribution type
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# Generative example: Faces

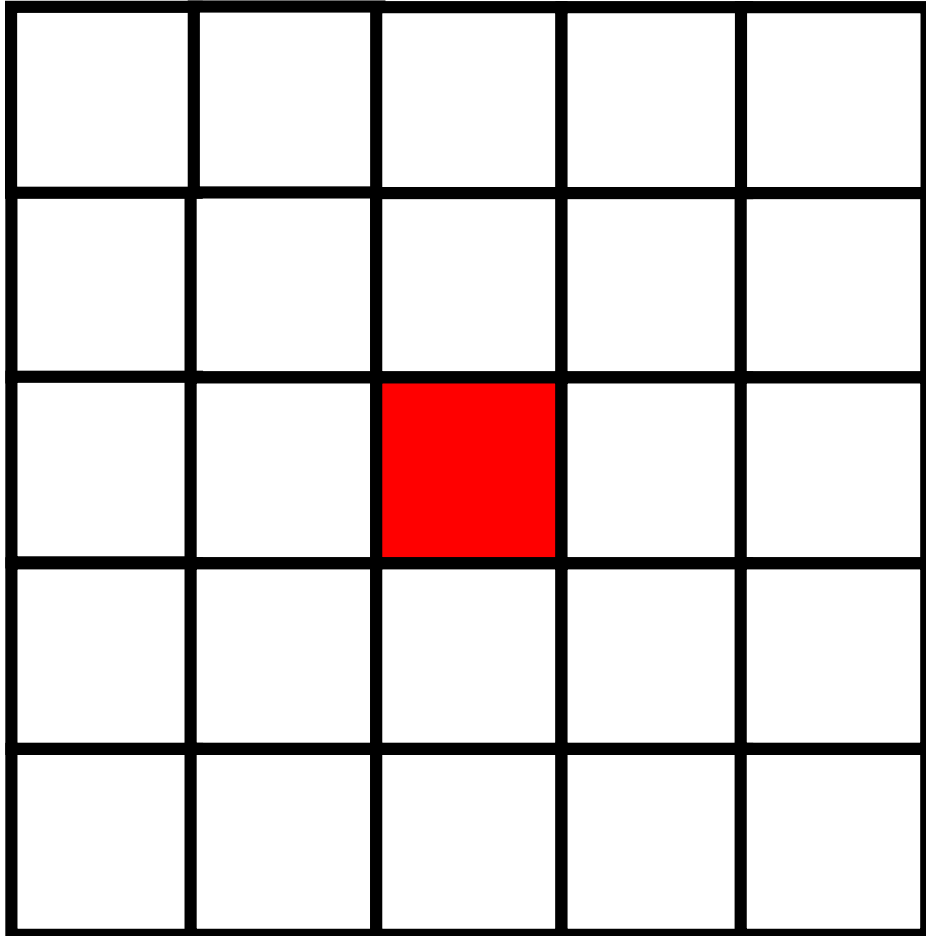
Symbols: **Face (F)**, Eye (E), Nose (N), Mouth (M), Eyelashes (L)



Rule	P(rule)	Spatial distribution type
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# Generative example: Faces

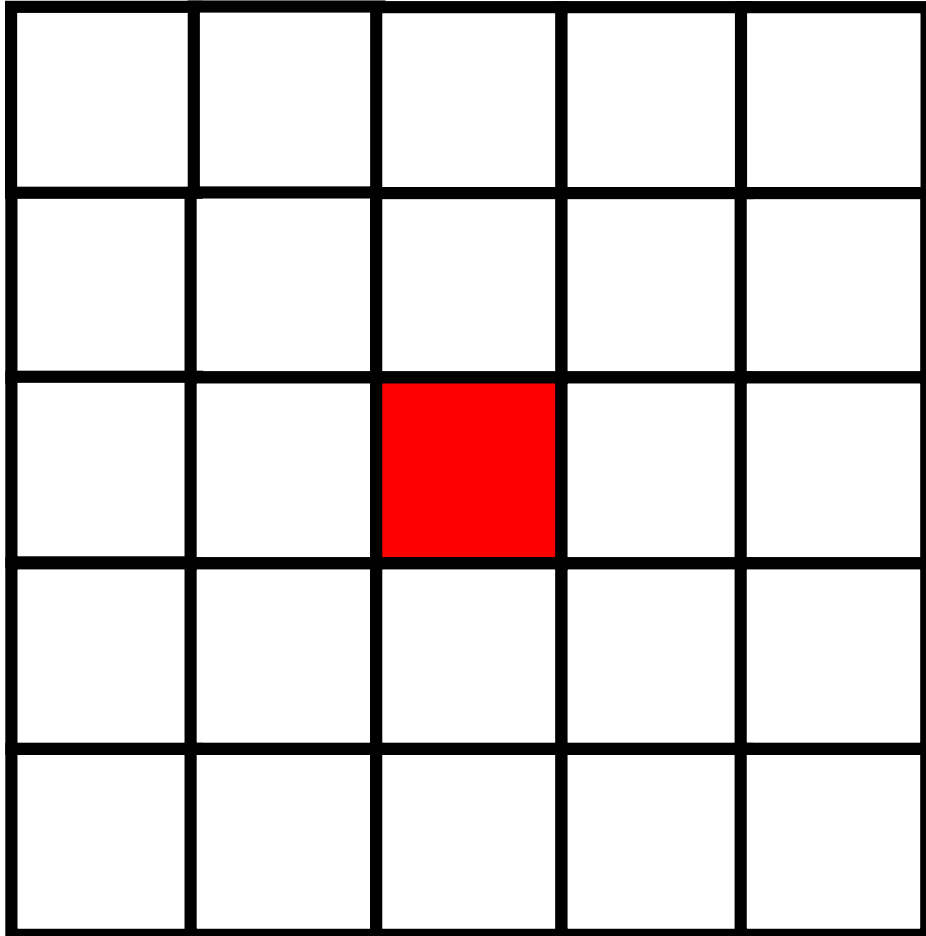
Symbols: Face (F), Eye (E), Nose (N), Mouth (M), Eyelashes (L)



Rule	P(rule)	Spatial distribution type
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# Generative example: Faces

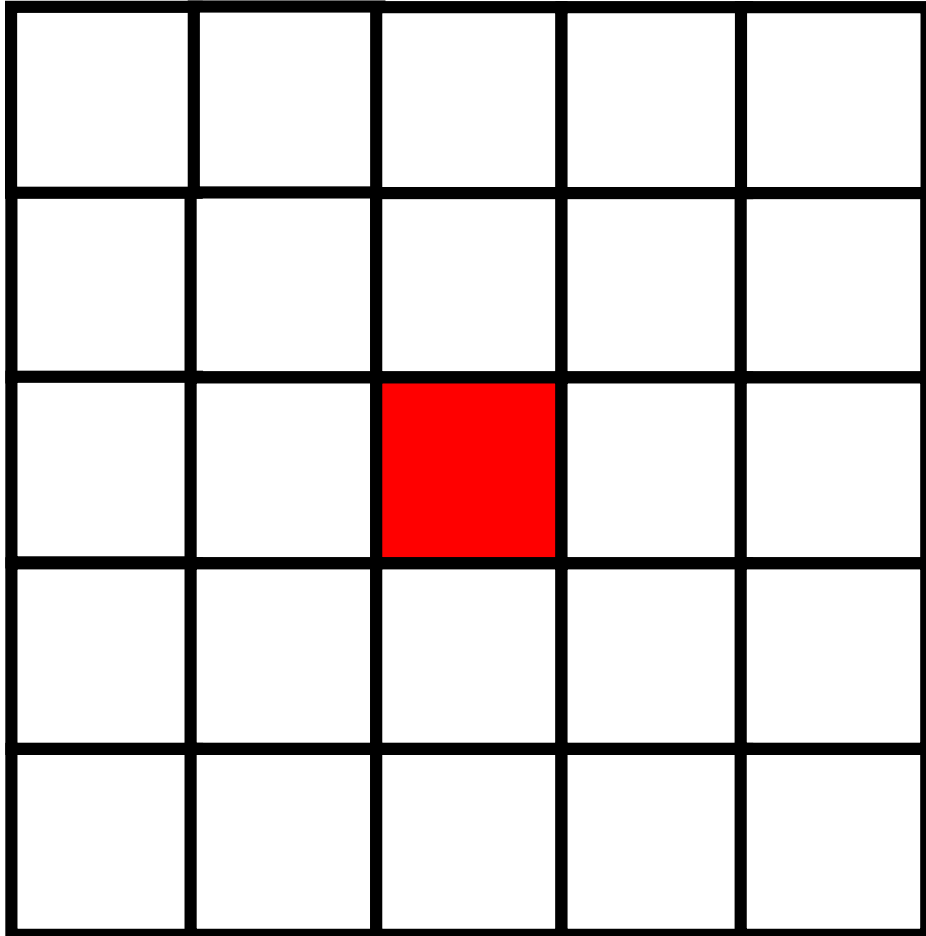
Symbols: **Face (F)**, Eye (E), Nose (N), Mouth (M), Eyelashes (L)



Rule	P(rule)	Spatial distribution type
$F \rightarrow E, E, N, M$	1.0	Uniform

# Generative example: Faces

Symbols: **Face (F)**, Eye (E), Nose (N), Mouth (M), Eyelashes (L)

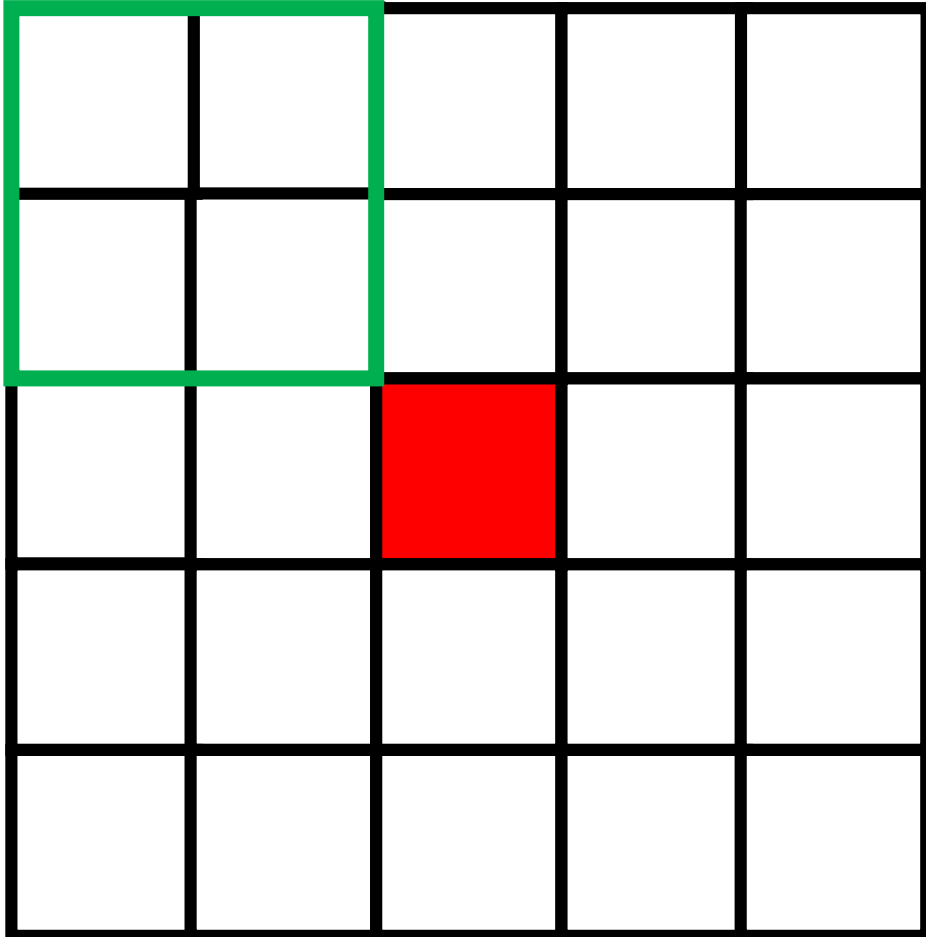


Rule	P(rule)	Spatial distribution type
$F \rightarrow E, E, N, M$	1.0	Uniform



# Generative example: Faces

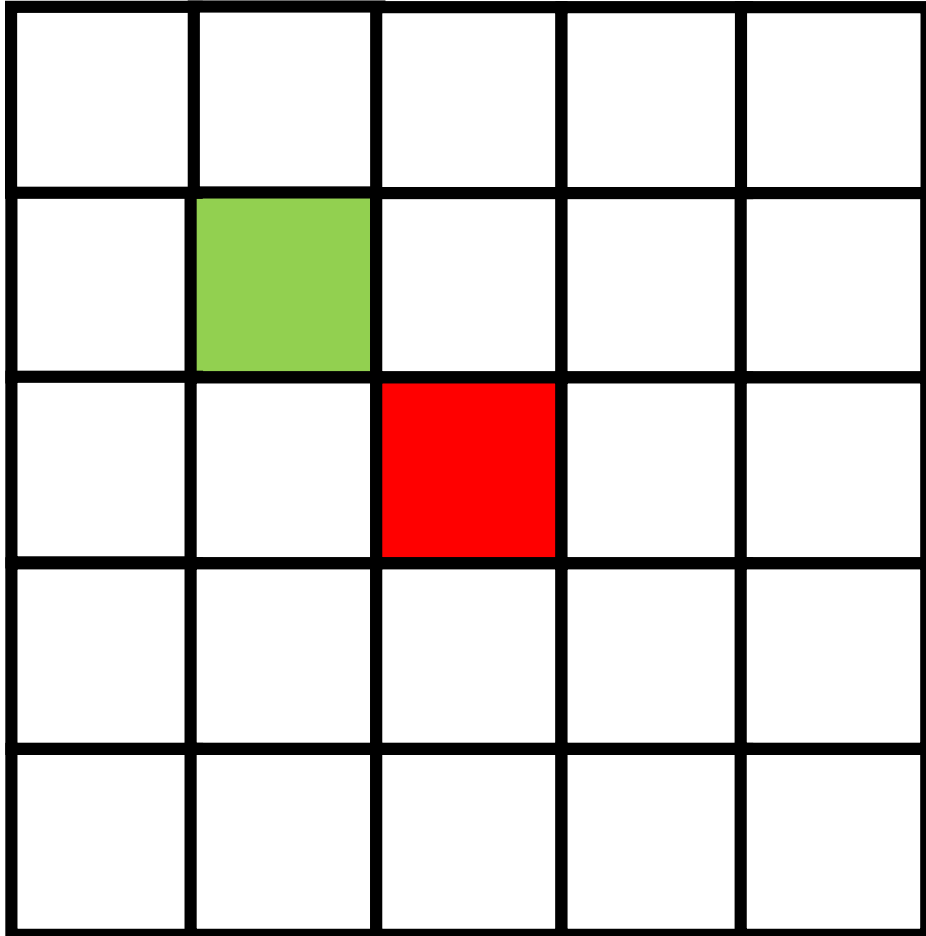
Symbols: **Face (F)**, Eye (E), Nose (N), Mouth (M), Eyelashes (L)



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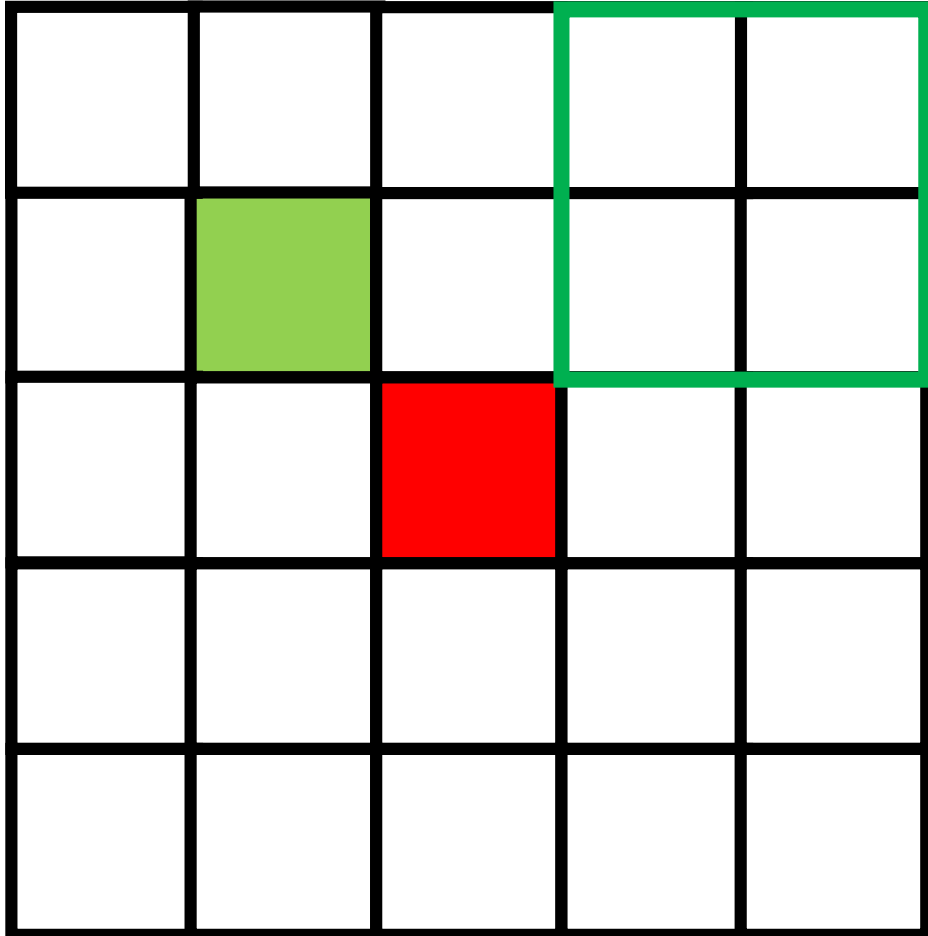
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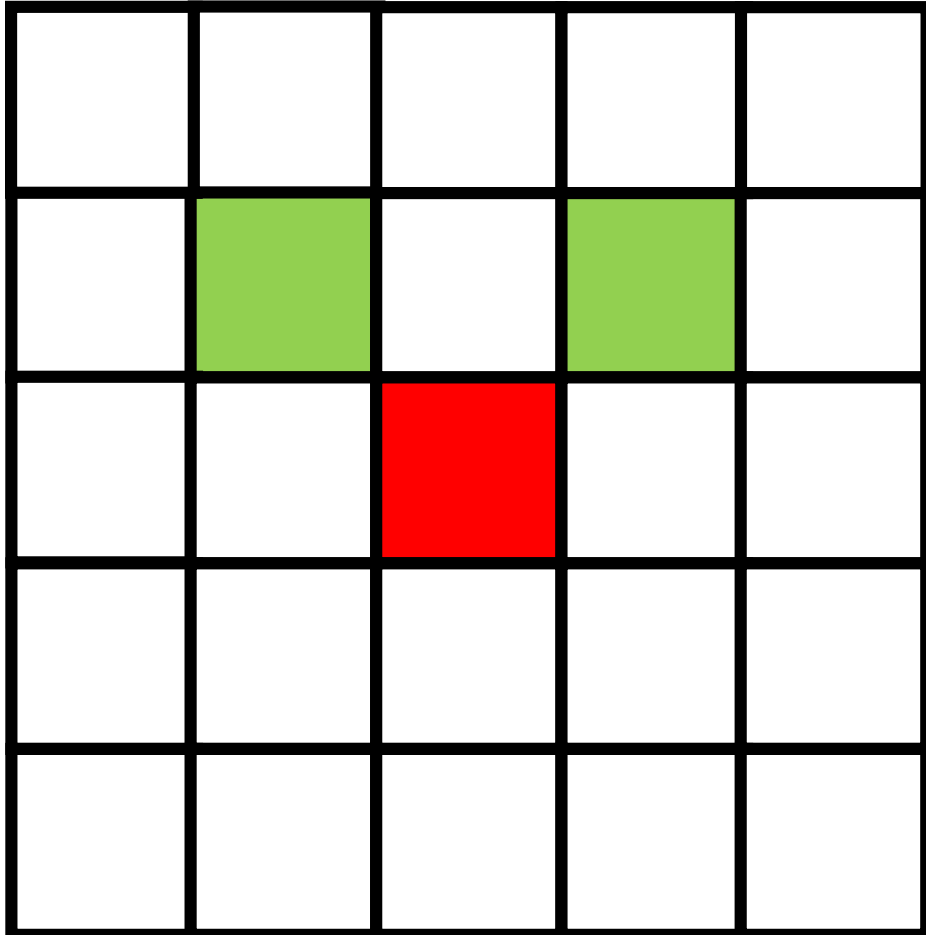
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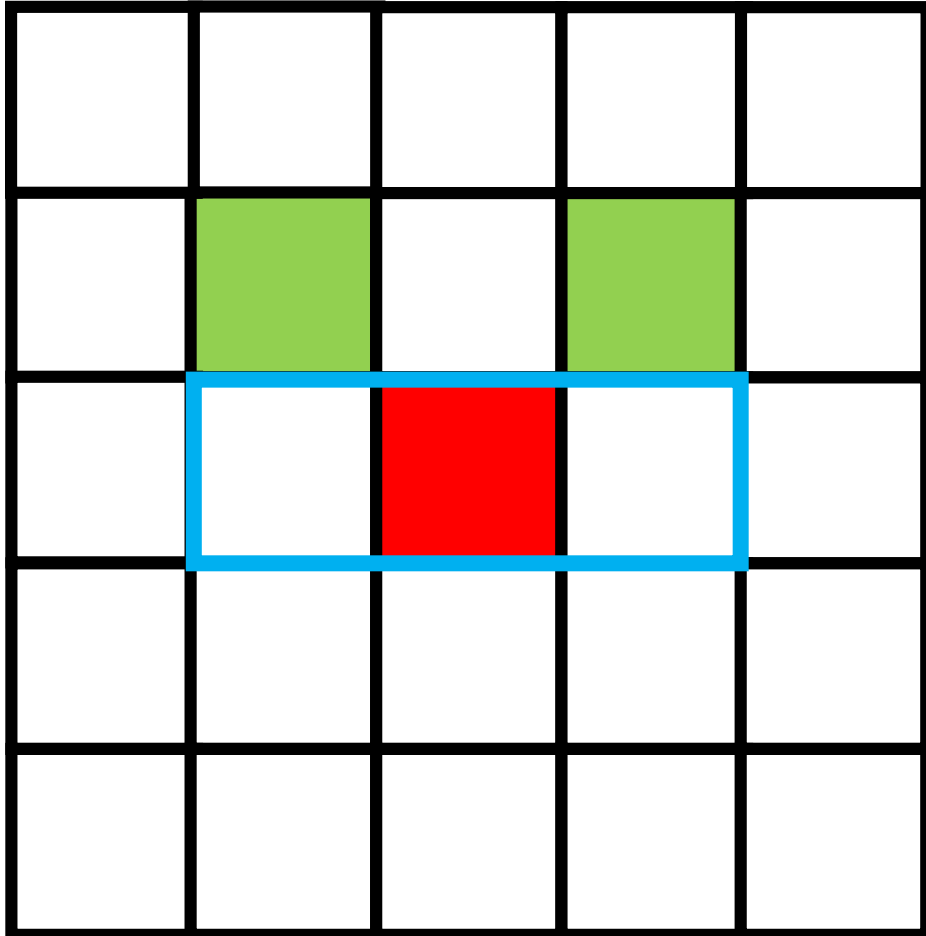
Symbols: Face (F), Eye (E), Nose (N), Mouth (M), Eyelashes (L)



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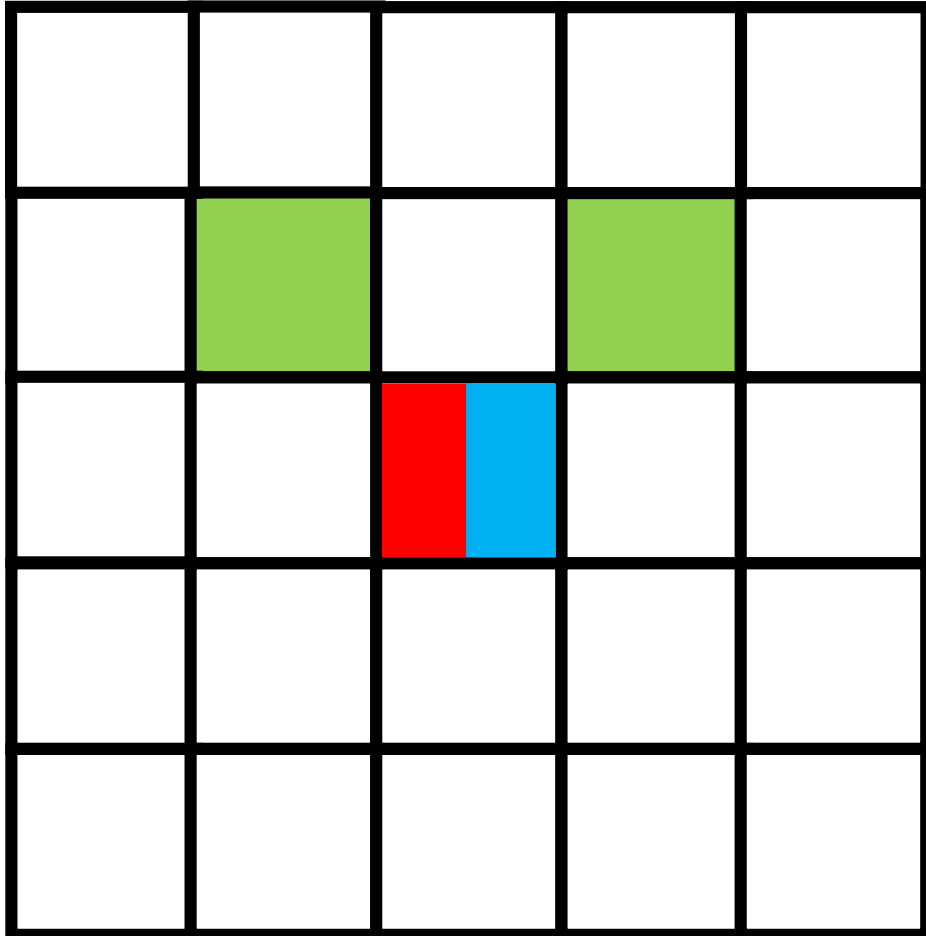
Symbols: Face (F), Eye (E), Nose (N), Mouth (M), Eyelashes (L)



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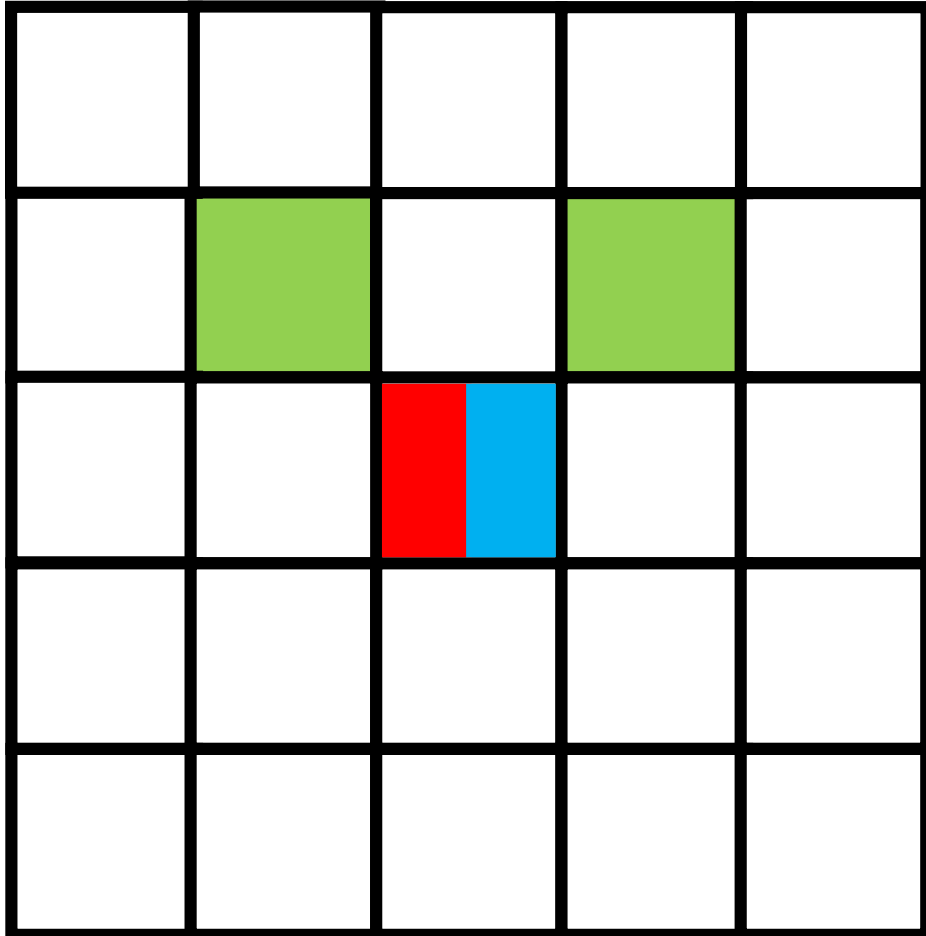
Symbols: Face (F), Eye (E), Nose (N), Mouth (M), Eyelashes (L)



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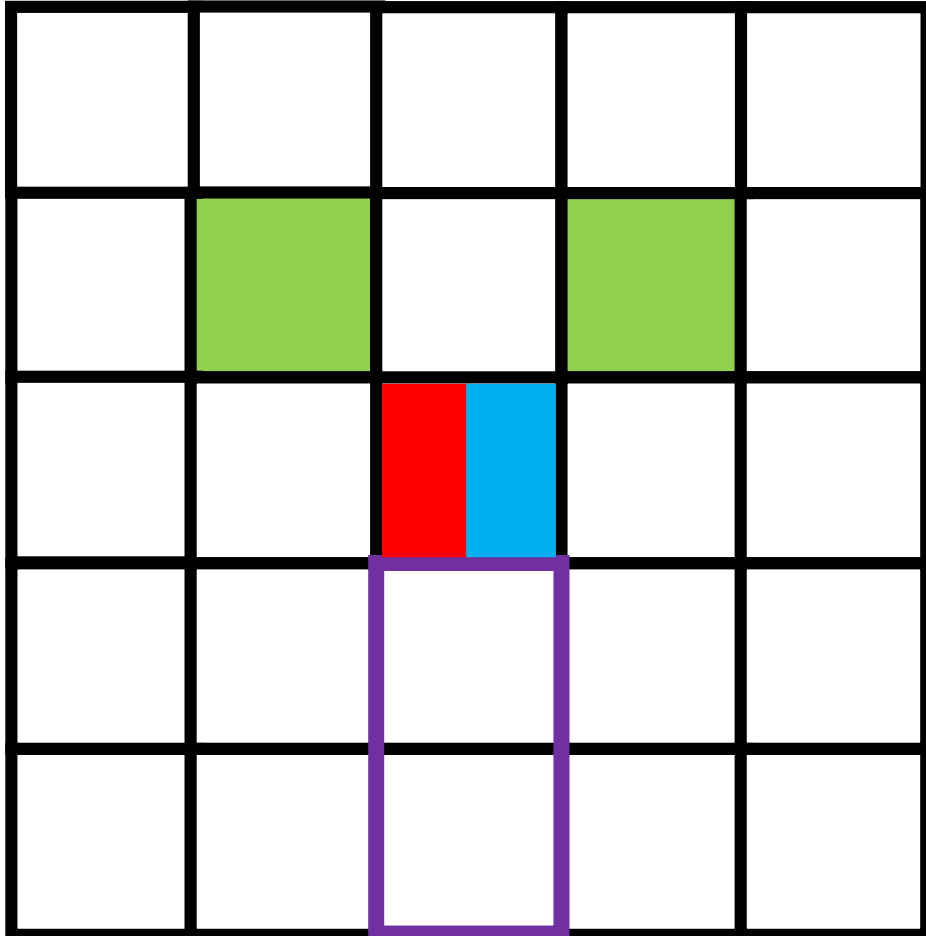
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Symbols: Face (F), Eye (E), Nose (N), Mouth (M), Eyelashes (L)

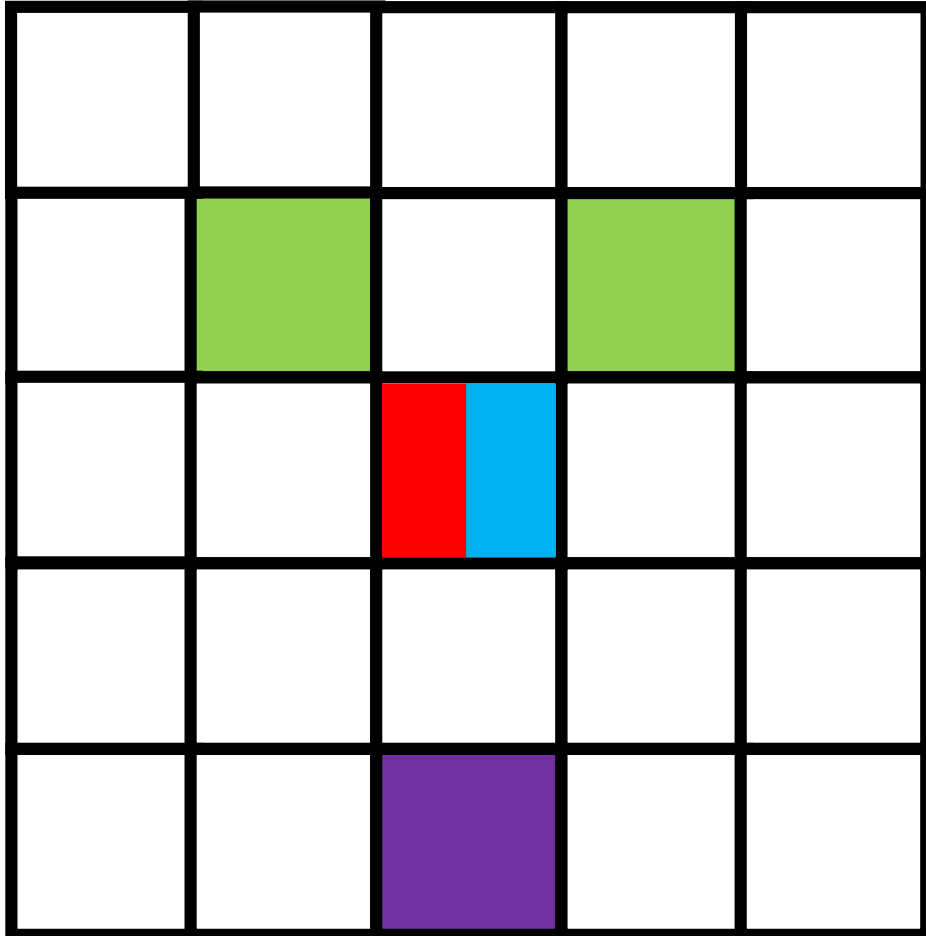


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# Generative example: Faces

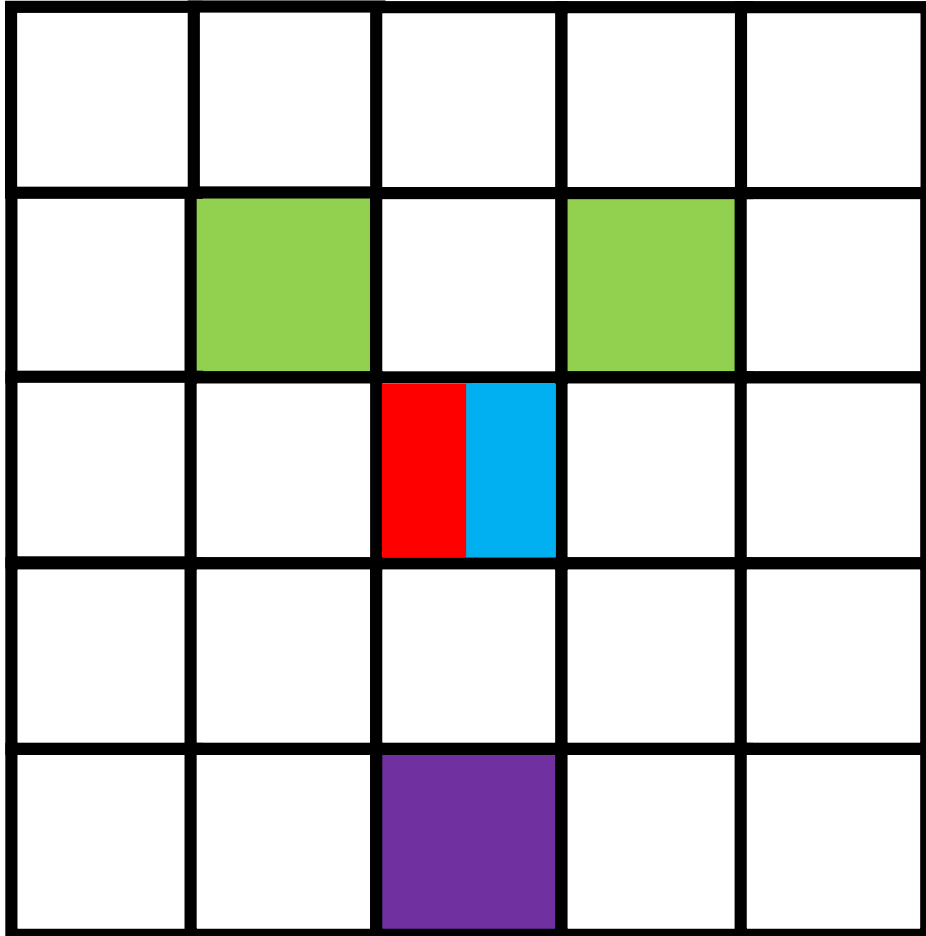
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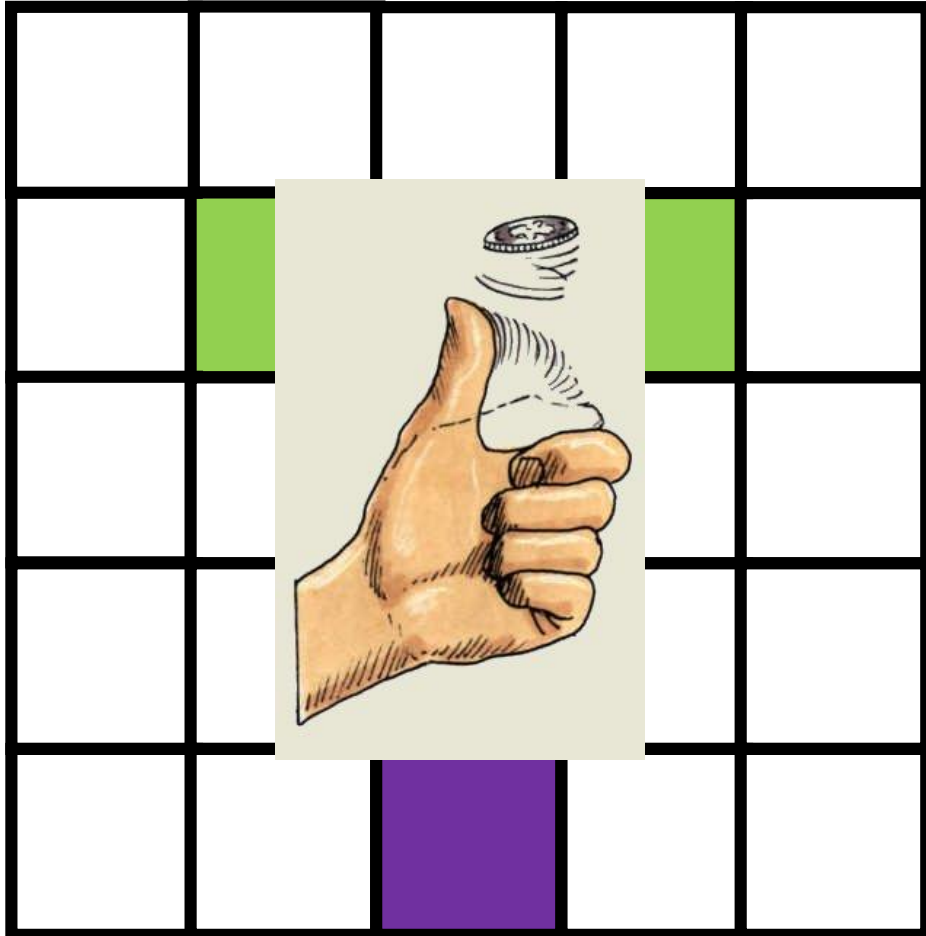
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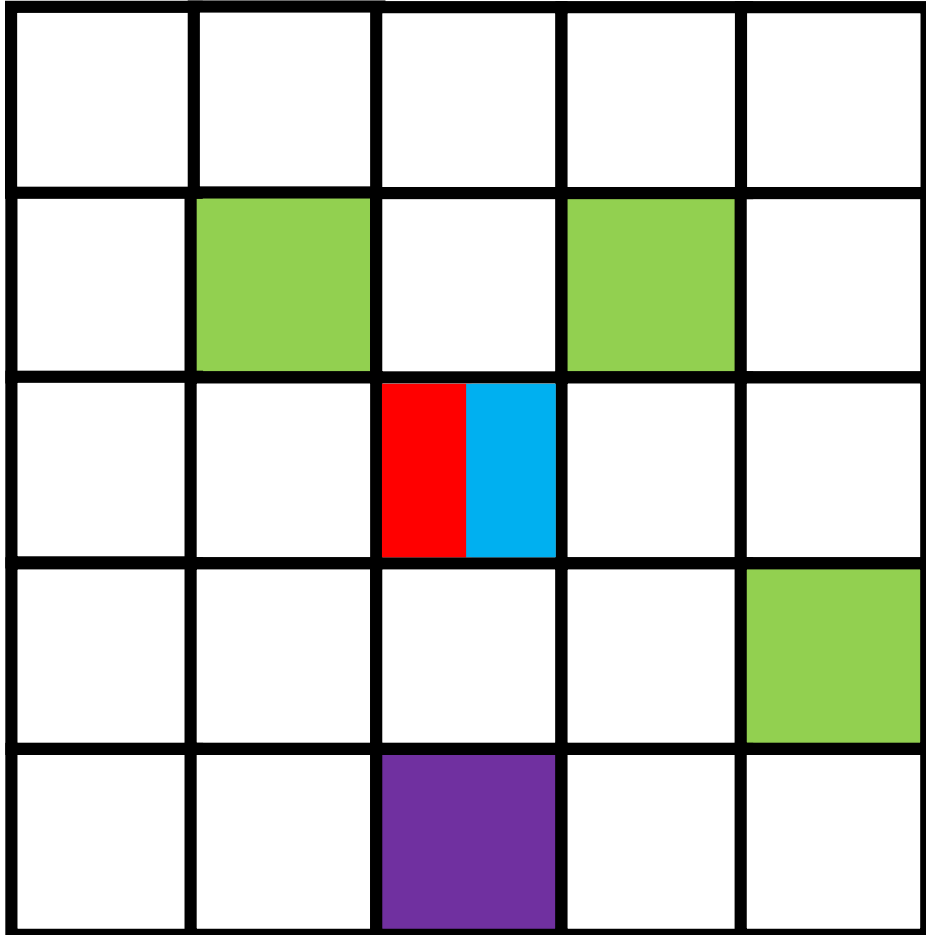
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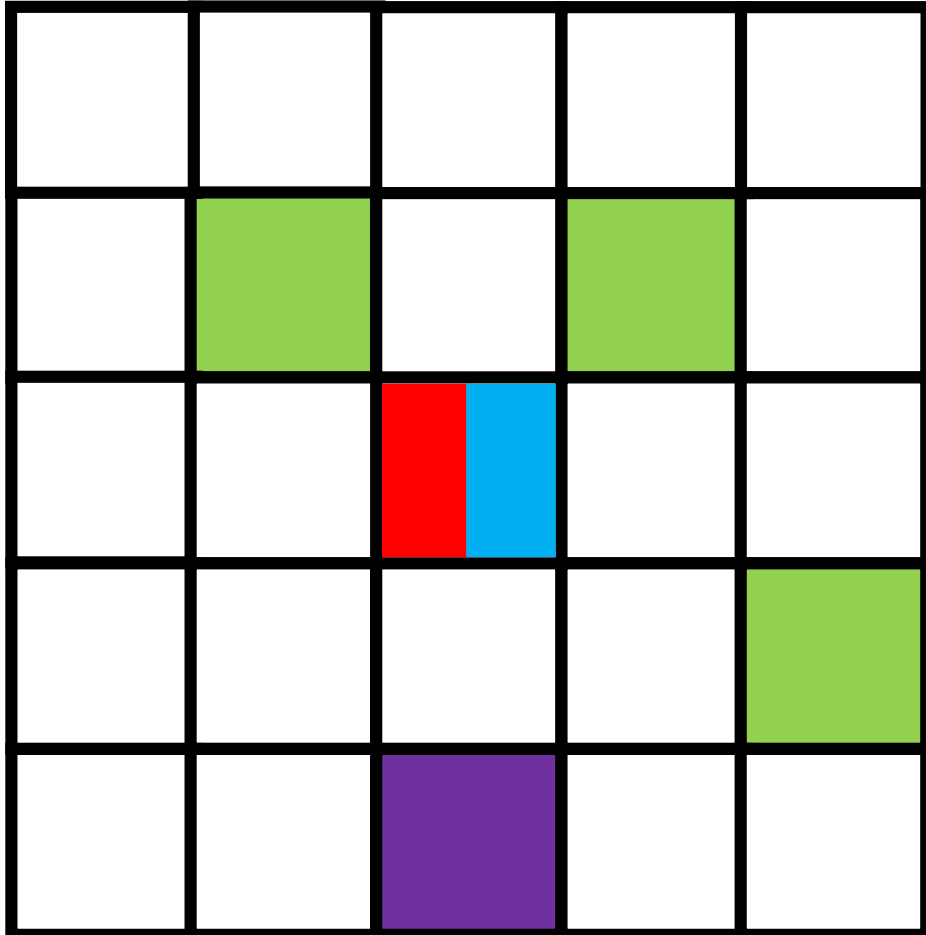
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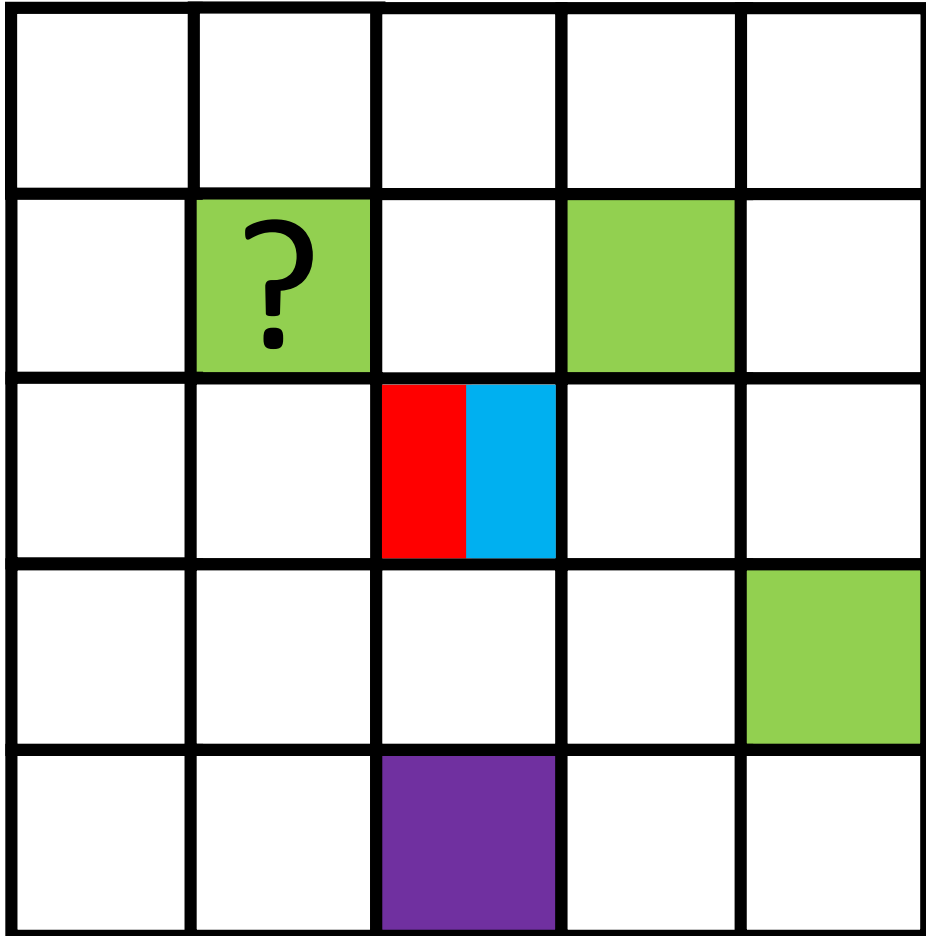
Symbols: Face (F), Eye (E), Nose (N), Mouth (M), Eyelashes (L)



Rule	P(rule)	Spatial distribution type
$F \rightarrow E, E, N, M$	1.0	Uniform
$E \rightarrow L$	0.5	
$E \rightarrow \emptyset$	0.5	-

# Generative example: Faces

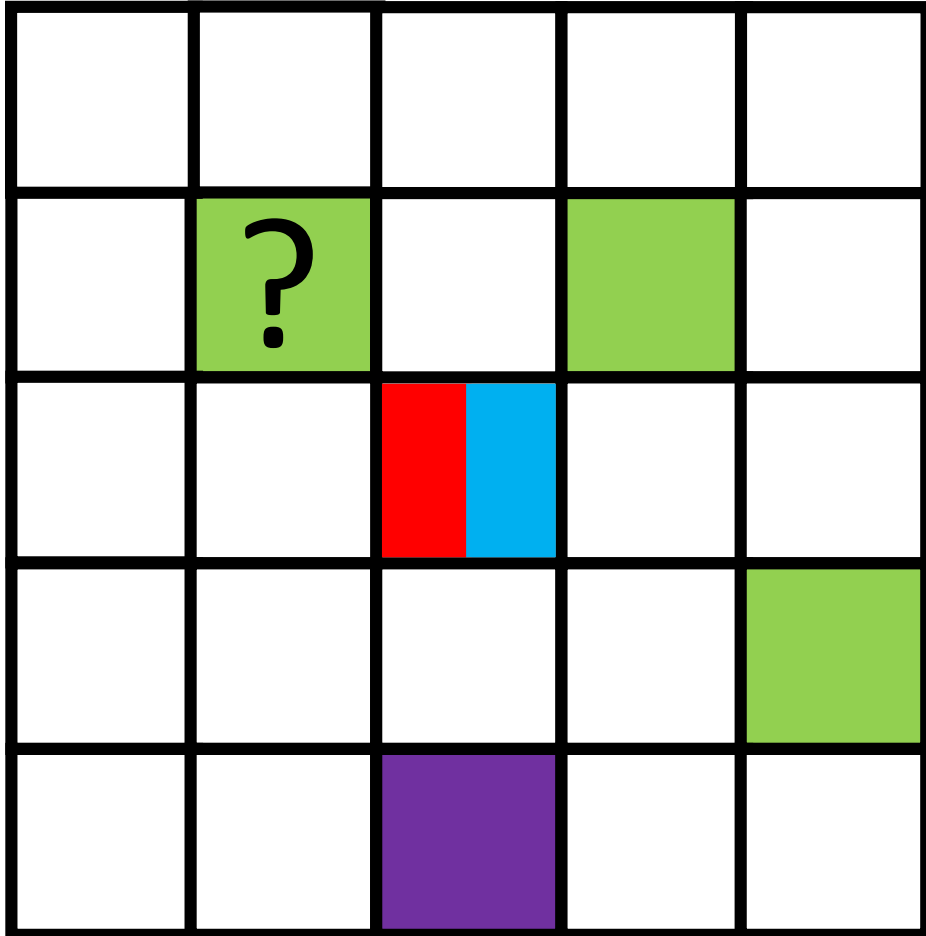
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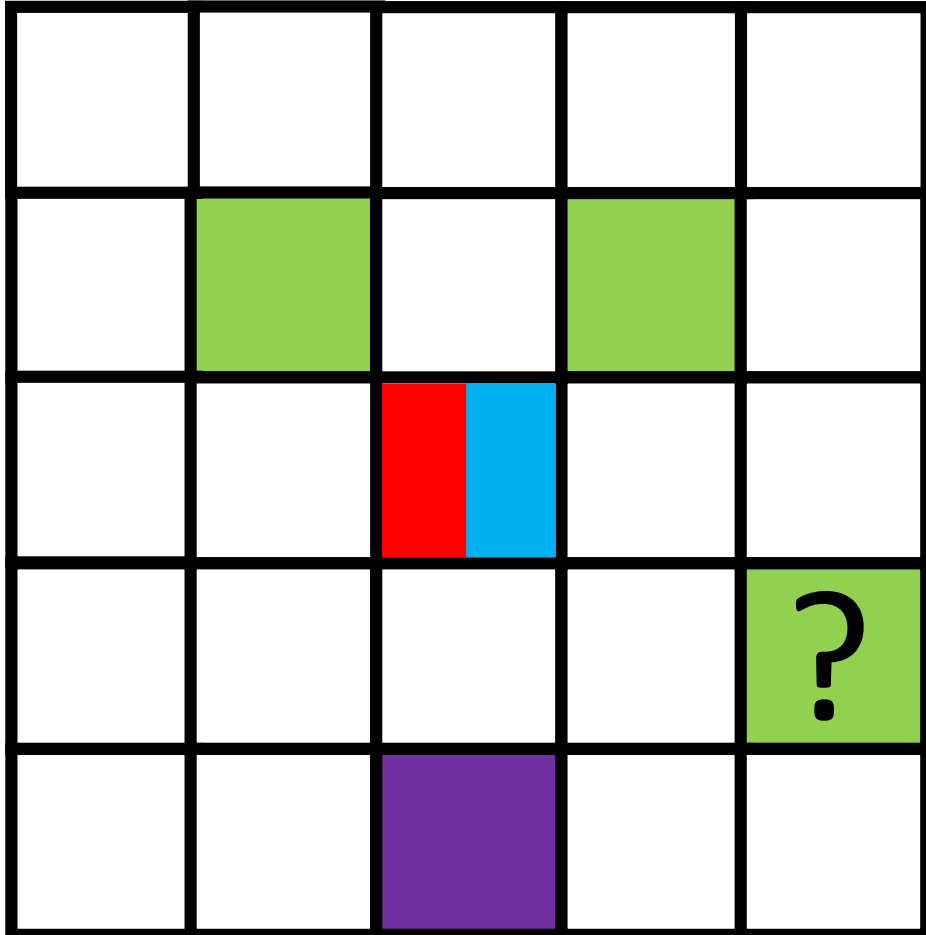
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Symbols: Face (F), Eye (E), Nose (N), Mouth (M), Eyelashes (L)

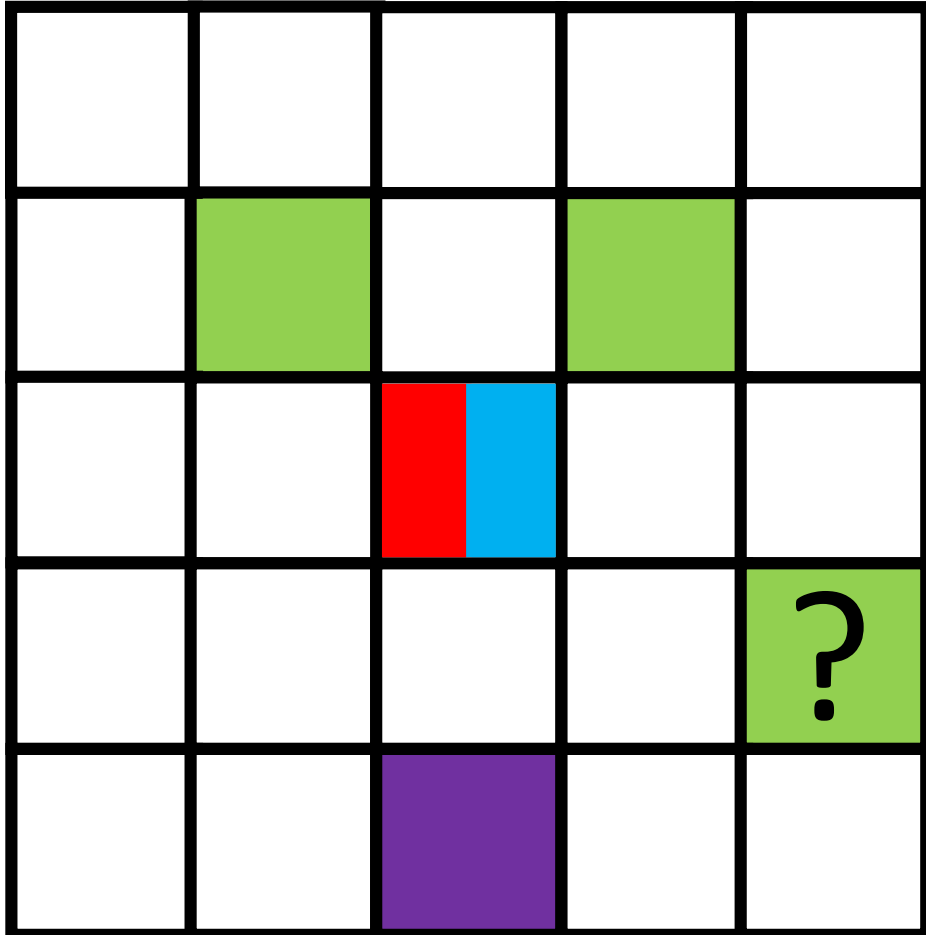


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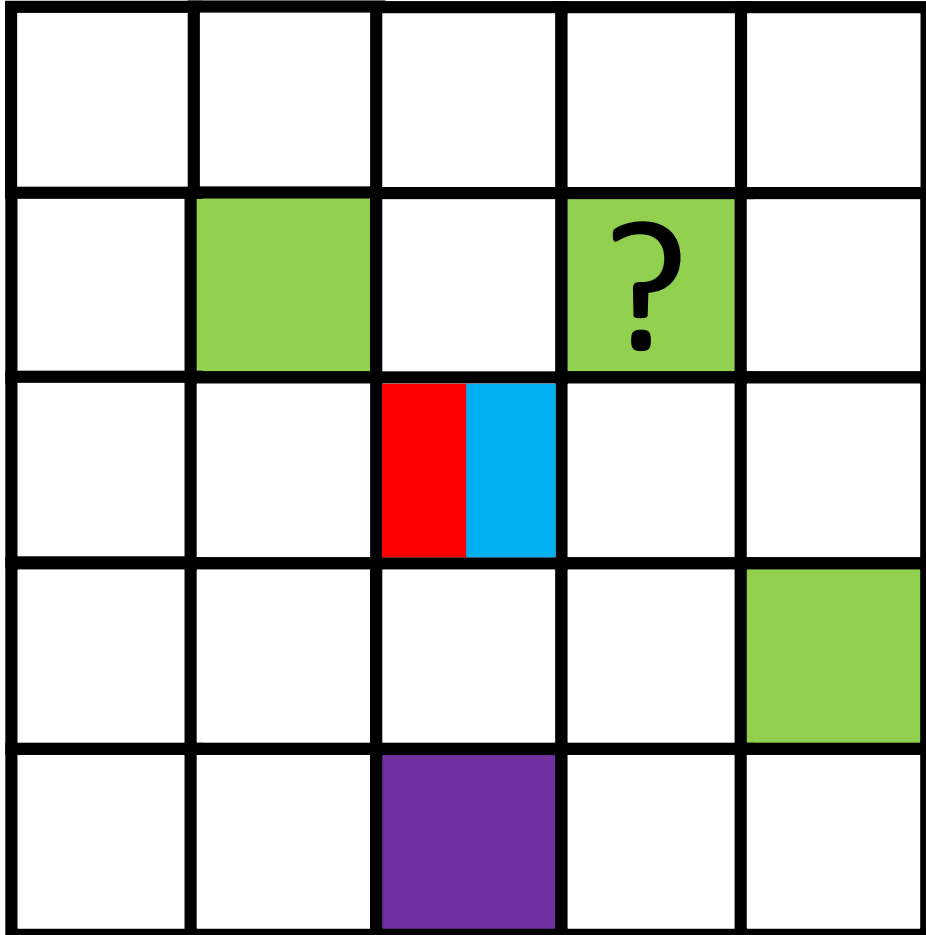
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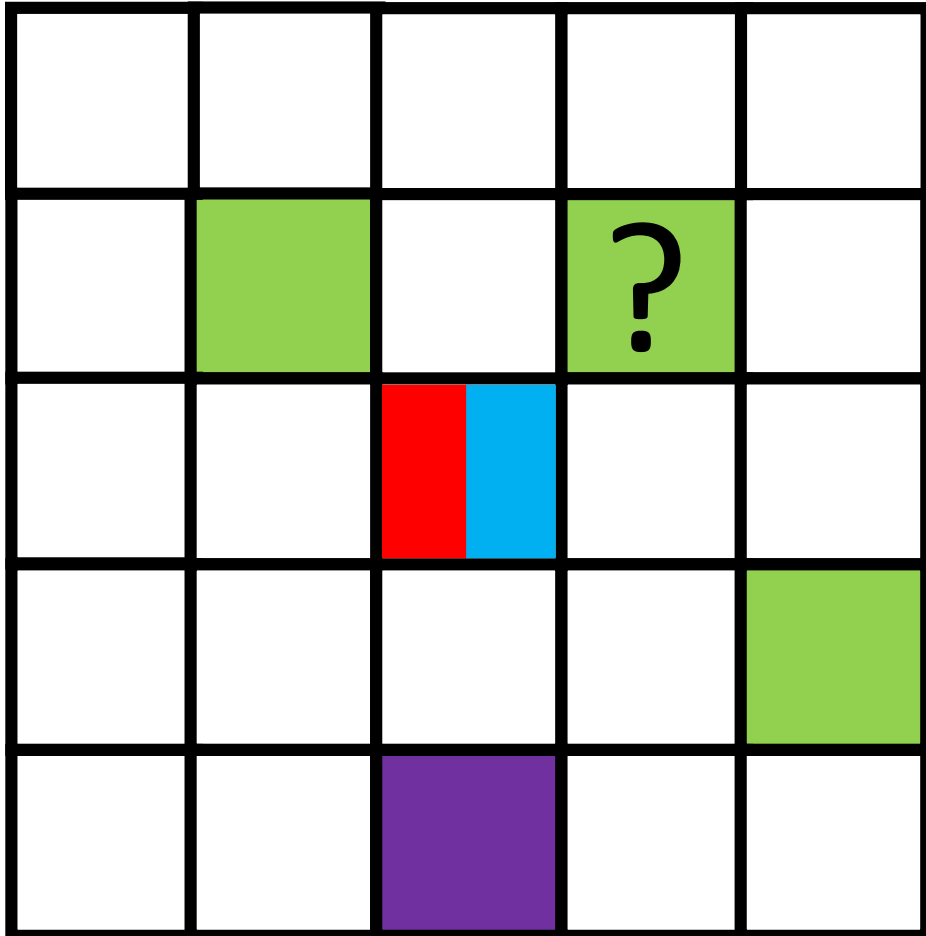
Symbols: Face (F), Eye (E), Nose (N), Mouth (M), Eyelashes (L)



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# Generative example: Faces

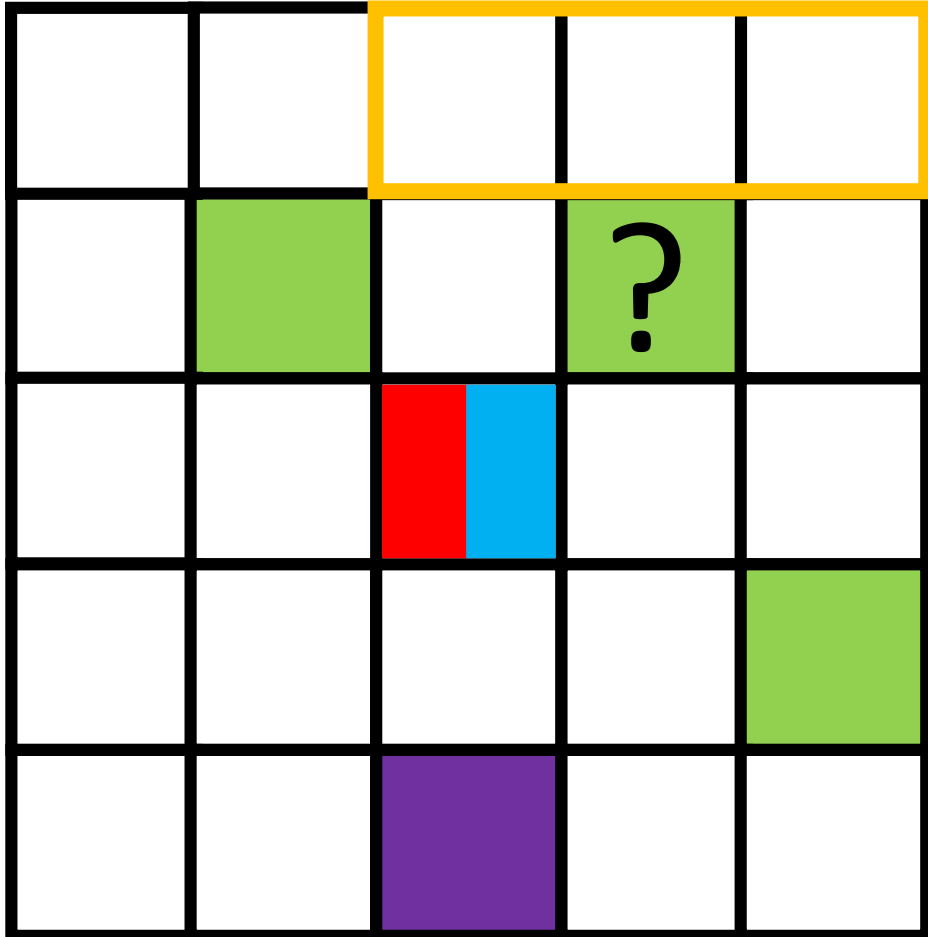
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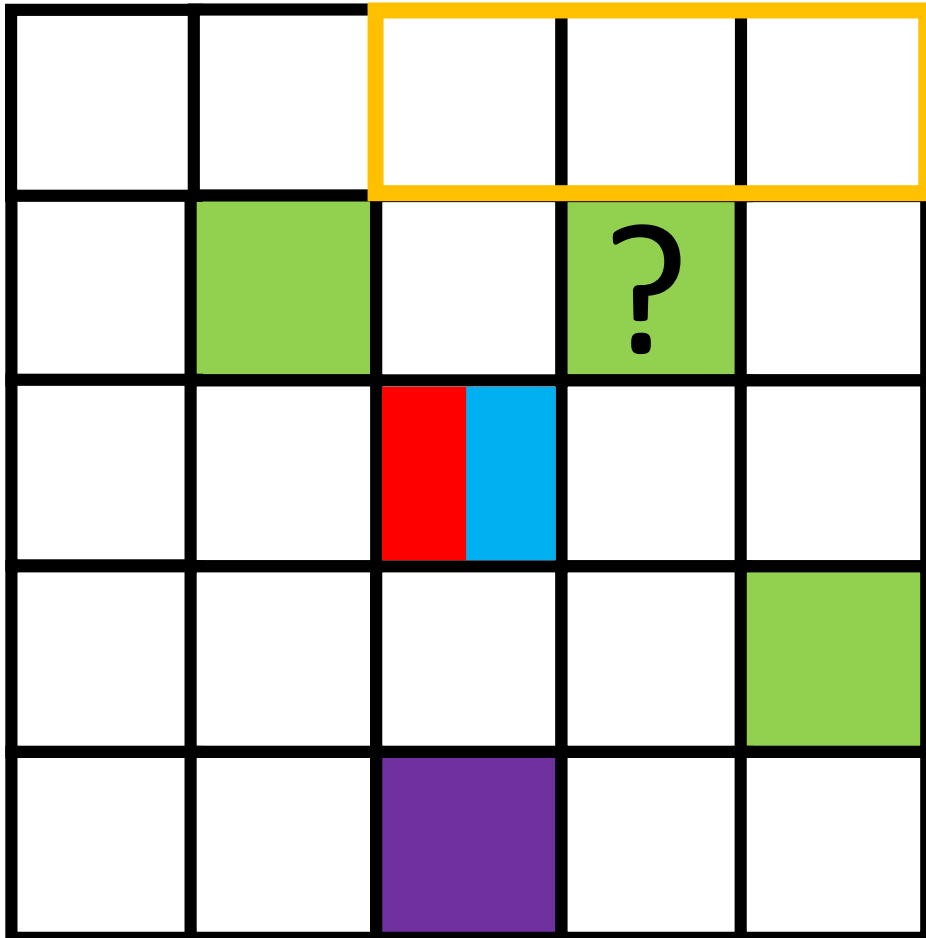
Symbols: Face (F), Eye (E), Nose (N), Mouth (M), Eyelashes (L)



Rule	P(rule)	Spatial distribution type
$F \rightarrow E, E, N, M$	1.0	Uniform
$E \rightarrow L$	0.5	
$E \rightarrow \emptyset$	0.5	-

# Generative example: Faces

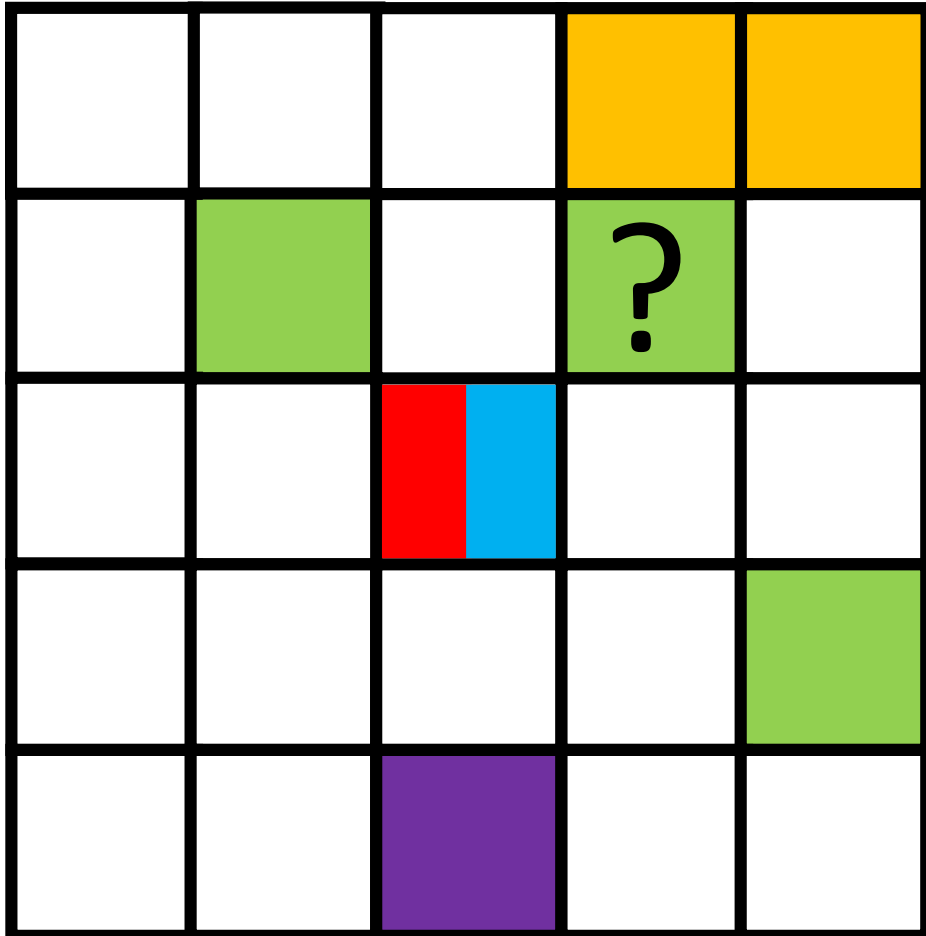
Symbols: Face (F), Eye (E), Nose (N), Mouth (M), Eyelashes (L)



Rule	P(rule)	Spatial distribution type
$F \rightarrow E, E, N, M$	1.0	Uniform
$E \rightarrow L$	0.5	Indep. Bernoullis, 50%
$E \rightarrow \emptyset$	0.5	-

# Generative example: Faces

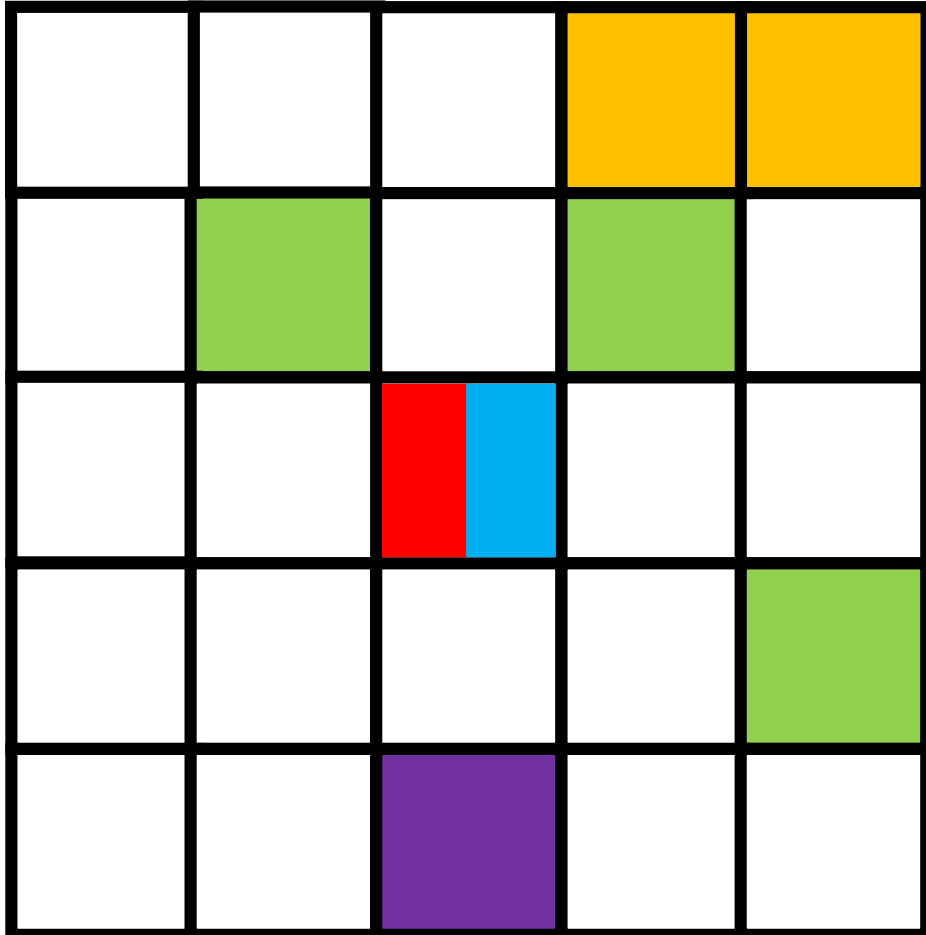
Symbols: Face (F), Eye (E), Nose (N), Mouth (M), Eyelashes (L)



Rule	P(rule)	Spatial distribution type
$F \rightarrow E, E, N, M$	1.0	Uniform
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# Generative example: Faces

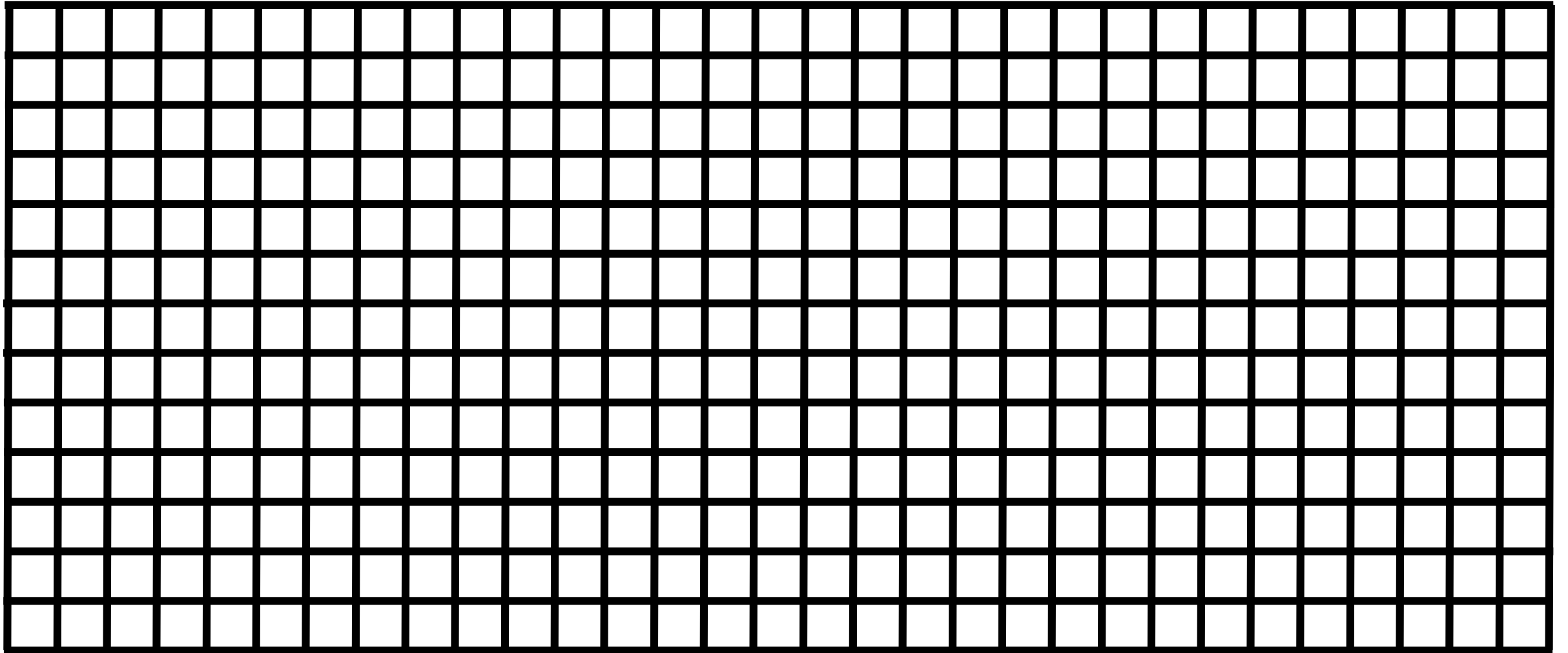
Symbols: Face (F), Eye (E), Nose (N), Mouth (M), Eyelashes (L)



Rule	P(rule)	Spatial distribution type
$F \rightarrow E, E, N, M$	1.0	Uniform
$E \rightarrow L$	0.5	Indep. Bernoullis, 50%
$E \rightarrow \emptyset$	0.5	-
$N \rightarrow \emptyset$	1.0	-
$M \rightarrow \emptyset$	1.0	-
$L \rightarrow \emptyset$	1.0	-

# Generative example: Faces

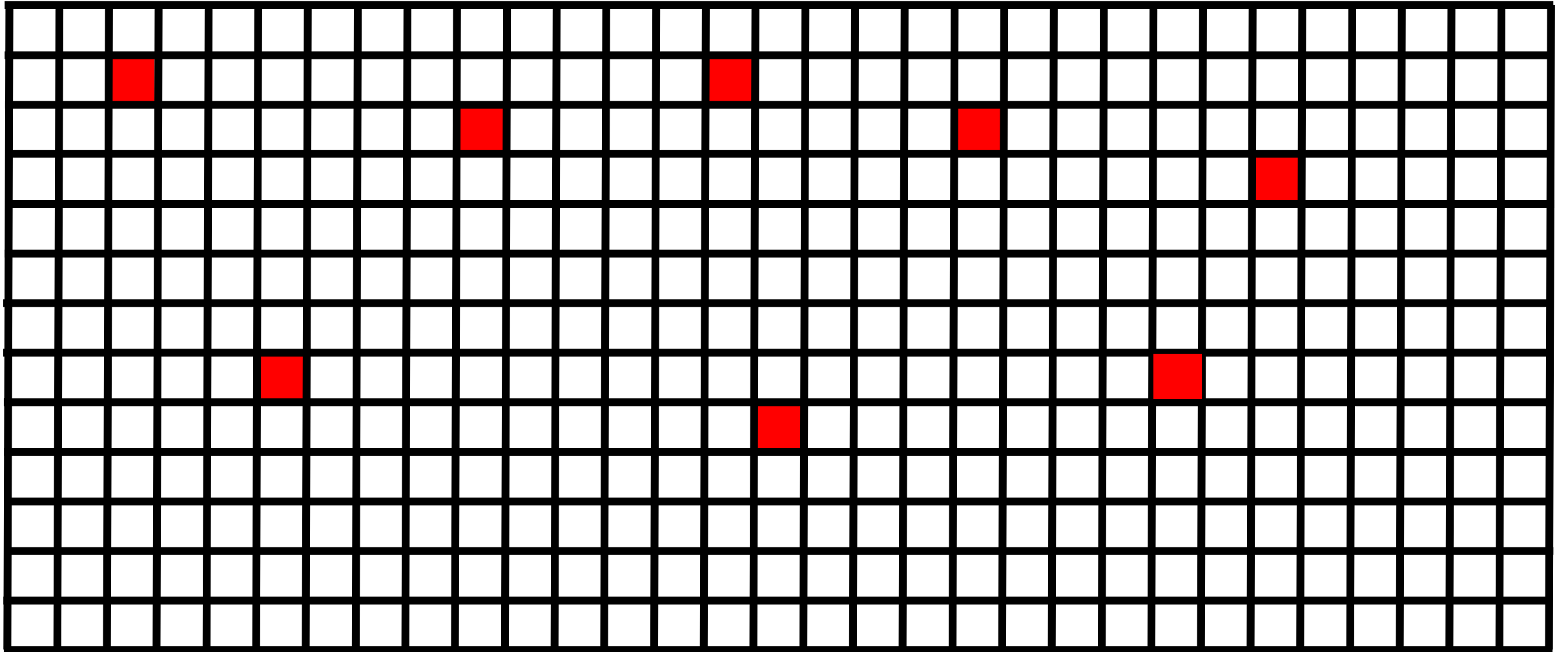
Symbols: Face (F), eye (E), nose (N), mouth (M), eyelashes (L)





# Generative example: Faces

Symbols: Face (F), eye (E), nose (N), mouth (M), eyelashes (L)



# Probabilistic Scene Grammar Specification

## Face localization grammar

$\Sigma = \{\text{FACE, EYE, NOSE, MOUTH}\}.$

$\forall A \in \Sigma, \Omega_A = [N] \times [M].$

*Rules:*

1.0, (FACE,  $\omega$ )  $\rightarrow$  (EYE, UniformRect( $\omega + a_1, \omega + b_1$ )),  
(EYE, UniformRect( $\omega + a_2, \omega + b_2$ )),  
(NOSE, UniformRect( $\omega + a_3, \omega + b_3$ )),  
(MOUTH, UniformRect( $\omega + a_4, \omega + b_4$ ))

1.0, (EYE,  $\omega$ )  $\rightarrow \emptyset$

1.0, (NOSE,  $\omega$ )  $\rightarrow \emptyset$

1.0, (MOUTH,  $\omega$ )  $\rightarrow \emptyset$

$\epsilon_{\text{FACE}} = 10^{-4},$

$\epsilon_{\text{EYE}} = \epsilon_{\text{NOSE}} = \epsilon_{\text{MOUTH}} = 10^{-5}.$

## Contour detection grammar

$\Sigma = \{\text{CURVE, INK}\}.$

$\Omega_{\text{CURVE}} = [N] \times [M] \times [8].$

$\Omega_{\text{INK}} = [N] \times [M].$

*Rules:*

0.65, (CURVE,  $(x, y, \theta)$ )  $\rightarrow$  (INK,  $\delta((x, y))$ ), (CURVE,  $\delta(((x, y) + \text{Round}(T_\theta(1, 0)), \theta))$ )

0.10, (CURVE,  $(x, y, \theta)$ )  $\rightarrow$  (INK,  $\delta((x, y))$ ), (CURVE,  $\delta(((x, y) + \text{Round}(T_\theta(1, -1)), \theta))$ )

0.10, (CURVE,  $(x, y, \theta)$ )  $\rightarrow$  (INK,  $\delta((x, y))$ ), (CURVE,  $\delta(((x, y) + \text{Round}(T_\theta(1, +1)), \theta))$ )

0.05, (CURVE,  $(x, y, \theta)$ )  $\rightarrow$  (CURVE,  $\delta((x, y, \theta + 1))$ )

0.05, (CURVE,  $(x, y, \theta)$ )  $\rightarrow$  (CURVE,  $\delta((x, y, \theta - 1))$ )

0.05, (CURVE,  $(x, y, \theta)$ )  $\rightarrow$  (INK,  $\delta((x, y))$ ),

1.00, (INK,  $(x, y)$ )  $\rightarrow \emptyset$

$\epsilon_{\text{CURVE}} = \epsilon_{\text{INK}} = 10^{-4}.$

## Binary image segmentation grammar

$\Sigma = \{\text{SEED, FG}\}.$

$\Omega_{\text{SEED}} = [1] \times [1].$

$\Omega_{\text{FG}} = [N] \times [M].$

*Rules:*

1.0, (SEED,  $\omega$ )  $\rightarrow$  (FG, UniformRect( $(1, 1), (N, M)$ ))

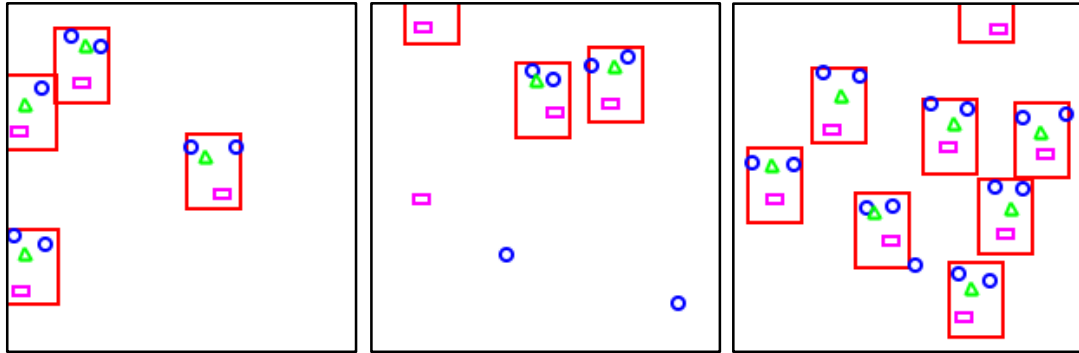
1.0, (FG,  $\omega$ )  $\rightarrow$  (FG, UniformBern(Rect( $\omega - (1, 1), \omega + (1, 1)$ ) \  $\omega$ , 0.25))

$\epsilon_{\text{SEED}} = 1,$

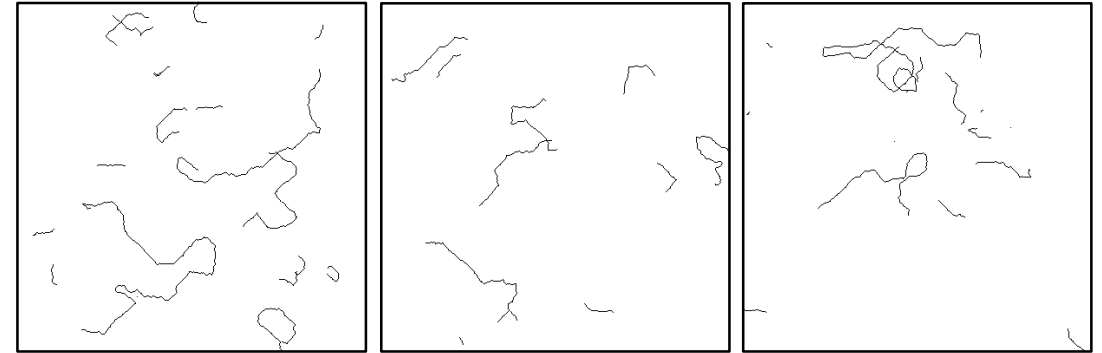
$\epsilon_{\text{FG}} = 0.$

# Probabilistic Scene Grammar Samples

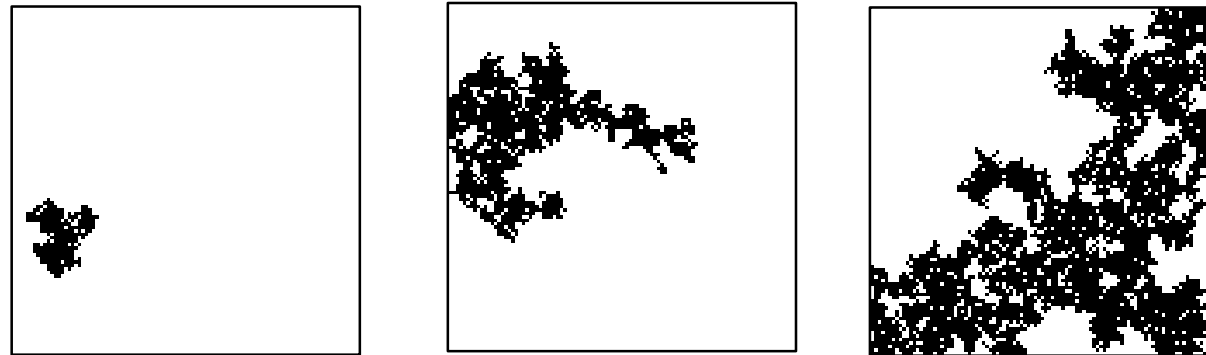
Face localization grammar



Contour detection grammar



Binary image segmentation grammar

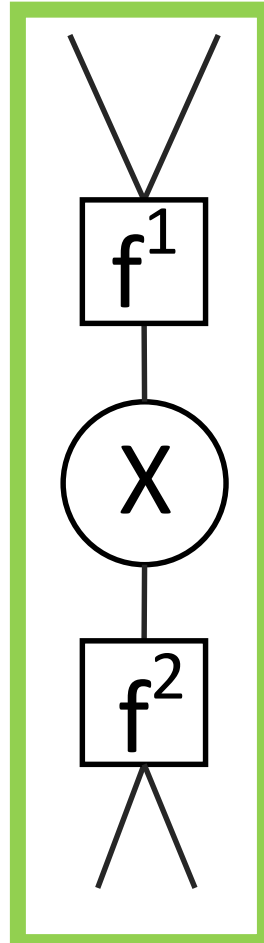


# The Probabilistic Scene Grammar Framework

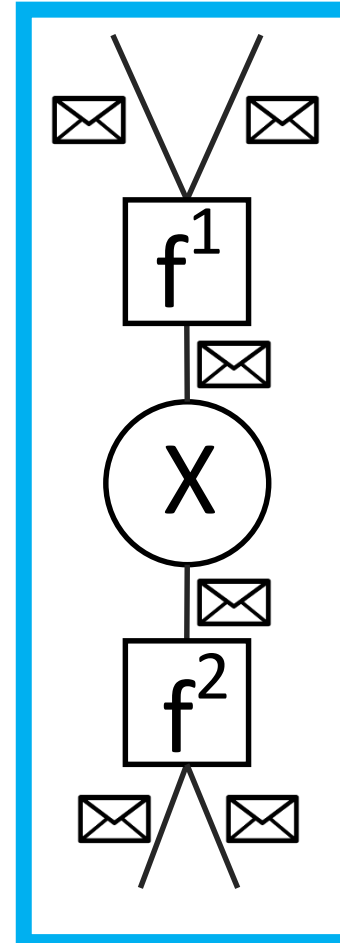
Probabilistic Scene Grammar



Factor graph



Inference

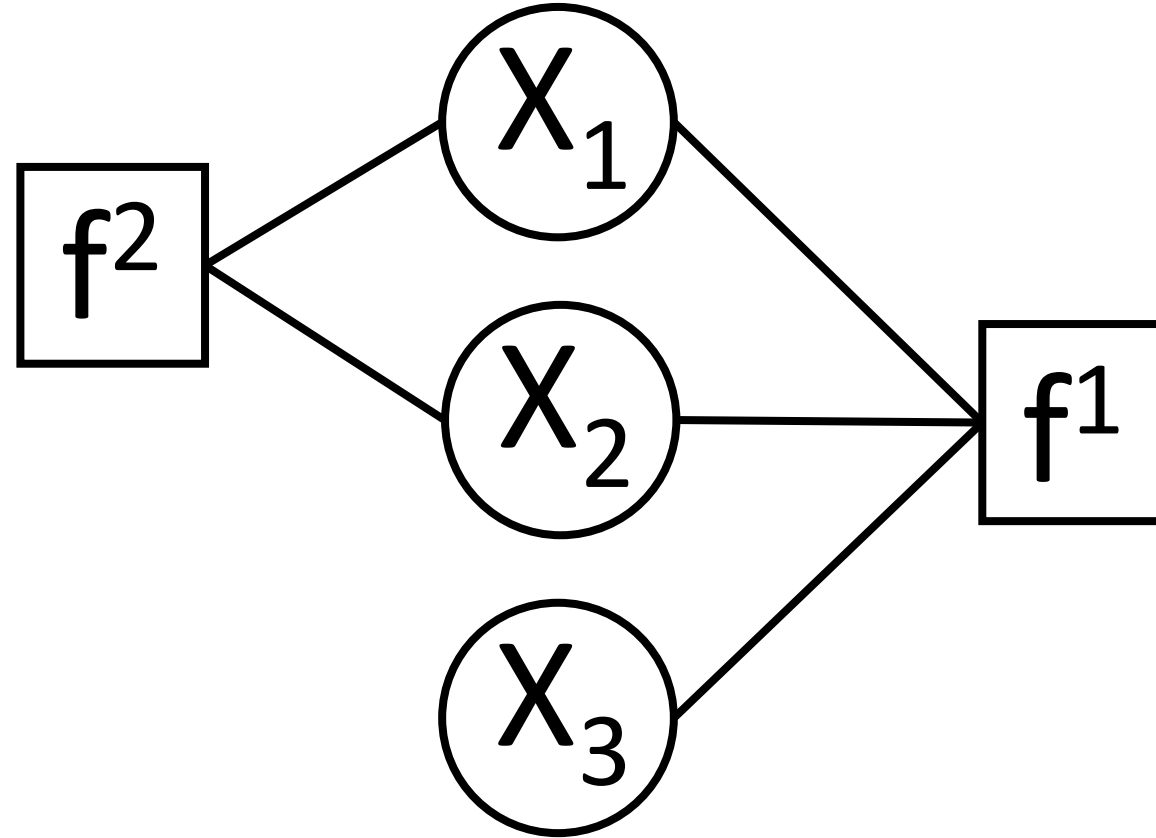


Learning



Approximate EM Algorithm

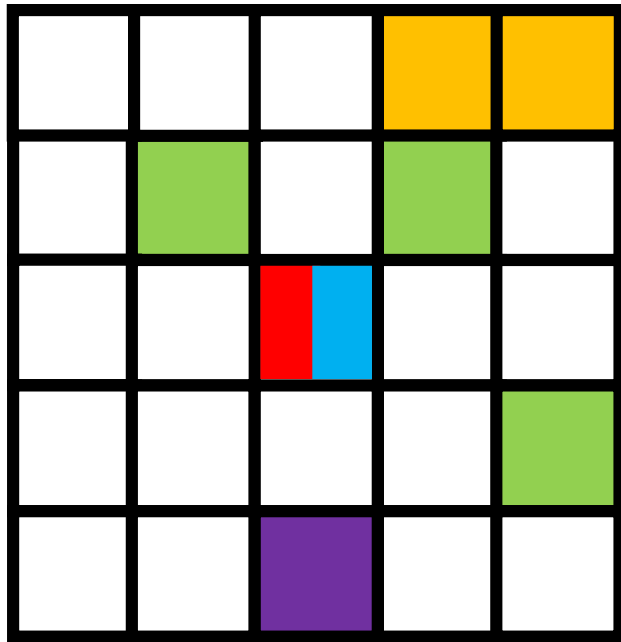
# Factor Graphs



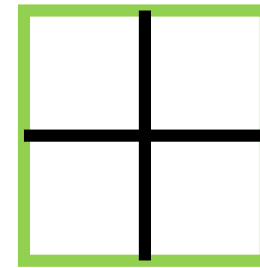
Encodes a distribution over random variables

# Distributions of the PSG

Three types of distributions: 1) Categorical



Which child to choose ?

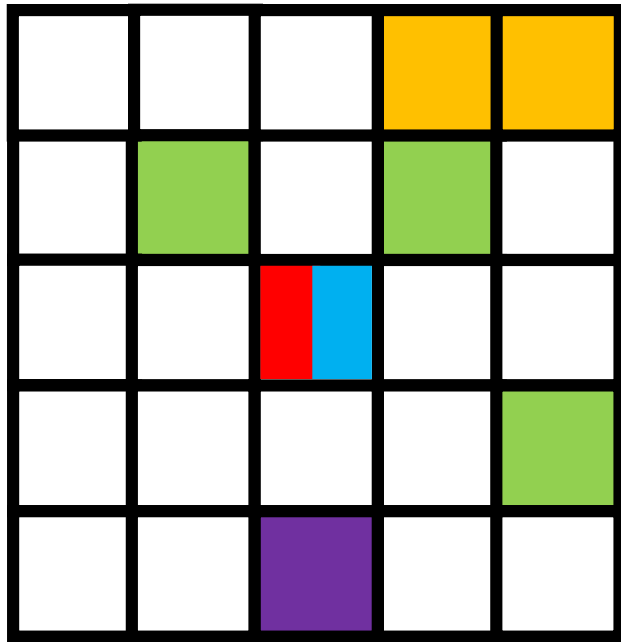


Which production rule?

$E \rightarrow L$	0.5	-
$E \rightarrow \emptyset$	0.5	-

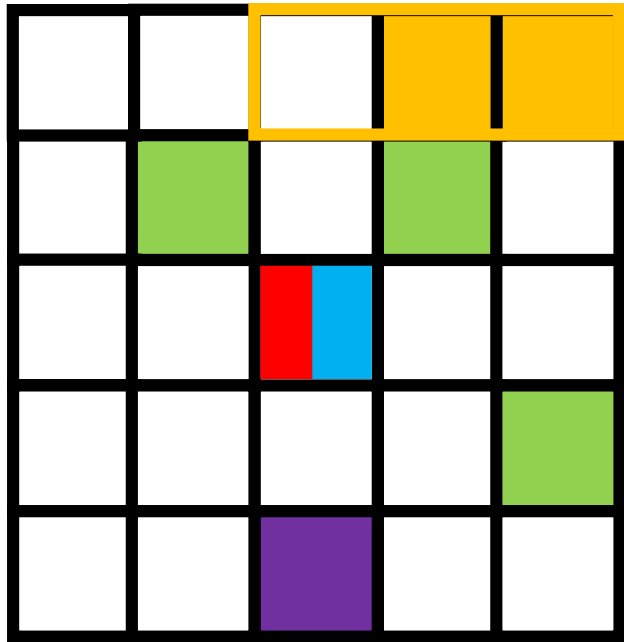
# Distributions of the PSG

Three types of distributions: 2) Independent Bernoullis



# Distributions of the PSG

Three types of distributions: 2) Independent Bernoullis



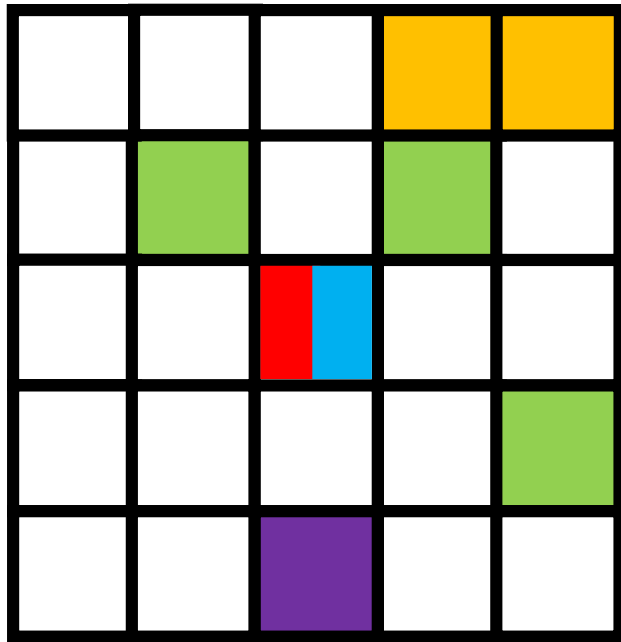
Which children to choose ?





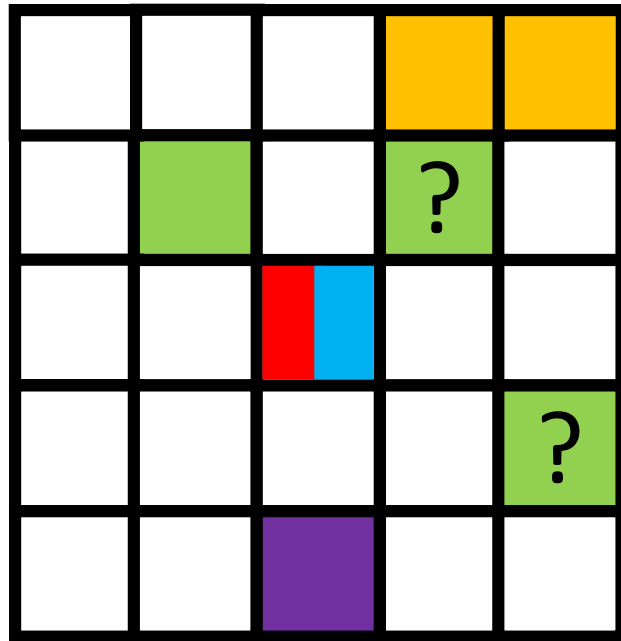
# Distributions of the PSG

Three types of distributions: 3) Leaky-or



# Distributions of the PSG

Three types of distributions: 3) Leaky-or

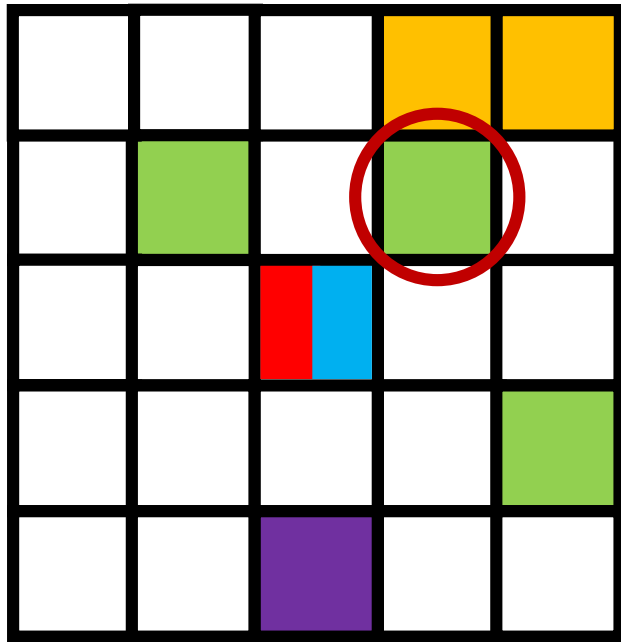


Object present?



# Distributions of the PSG

Three types of distributions: 3) Leaky-or



Object present?



# Framework: As a Factor Graph



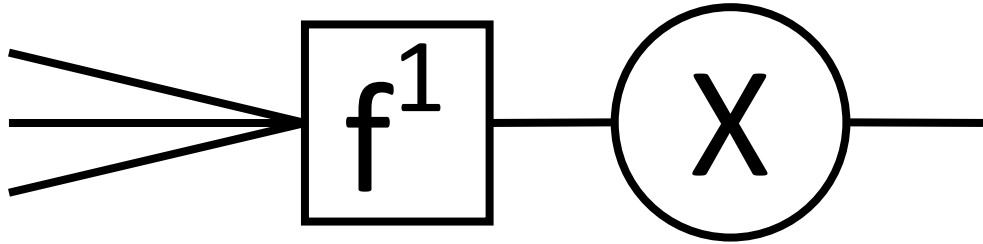
**Binary random variables:**

**Factors:**

# Framework: As a Factor Graph



=



Connections with super-parts

**Binary random variables:**

$X$ : Presence/absence of object

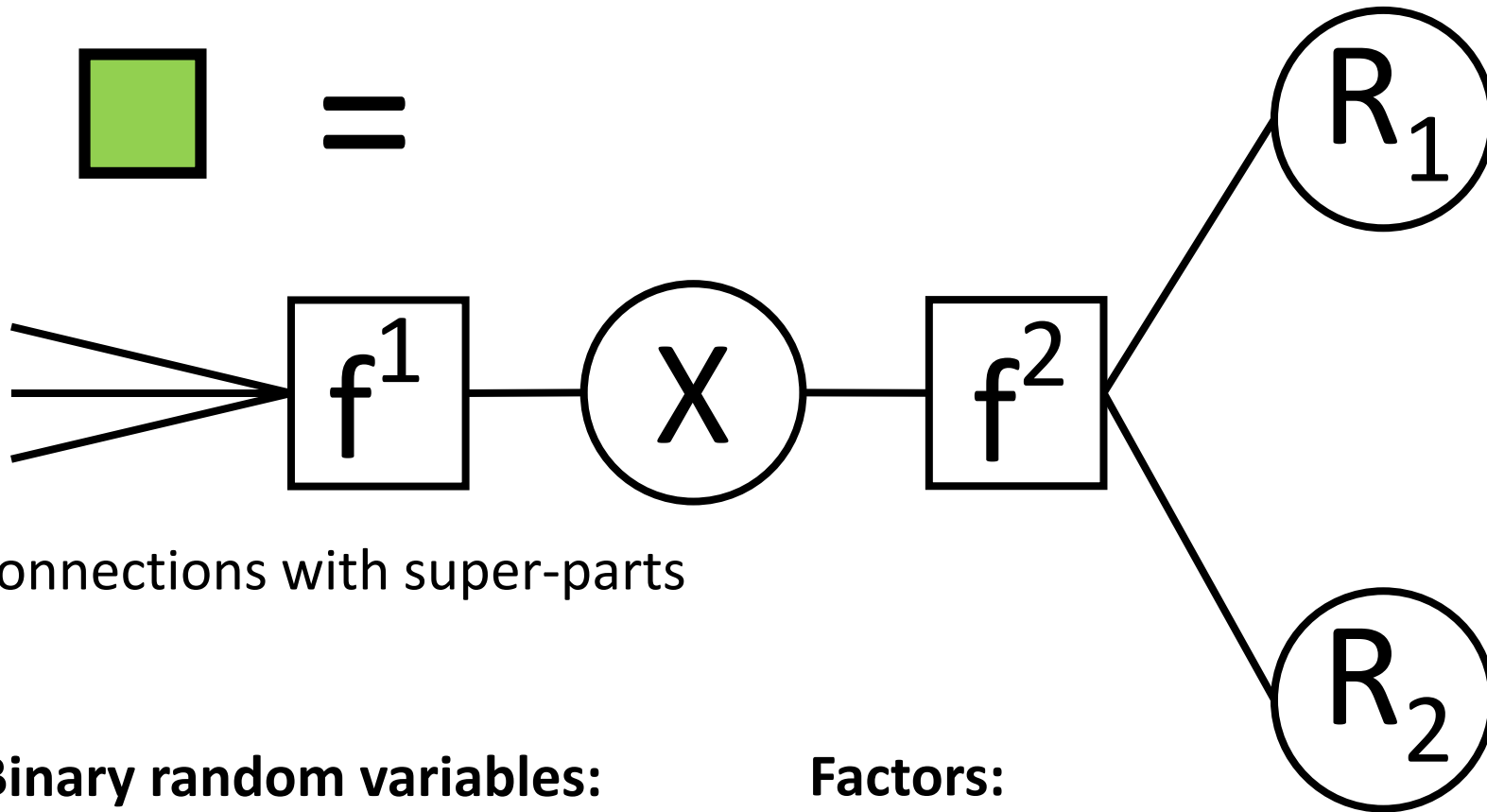
**Factors:**

$f^1$ : Leaky-or factor

# Framework: As a Factor Graph



=



Connections with super-parts

## Binary random variables:

$X$ : Presence/absence of object

$R_i$ : Choose rule  $i$

## Factors:

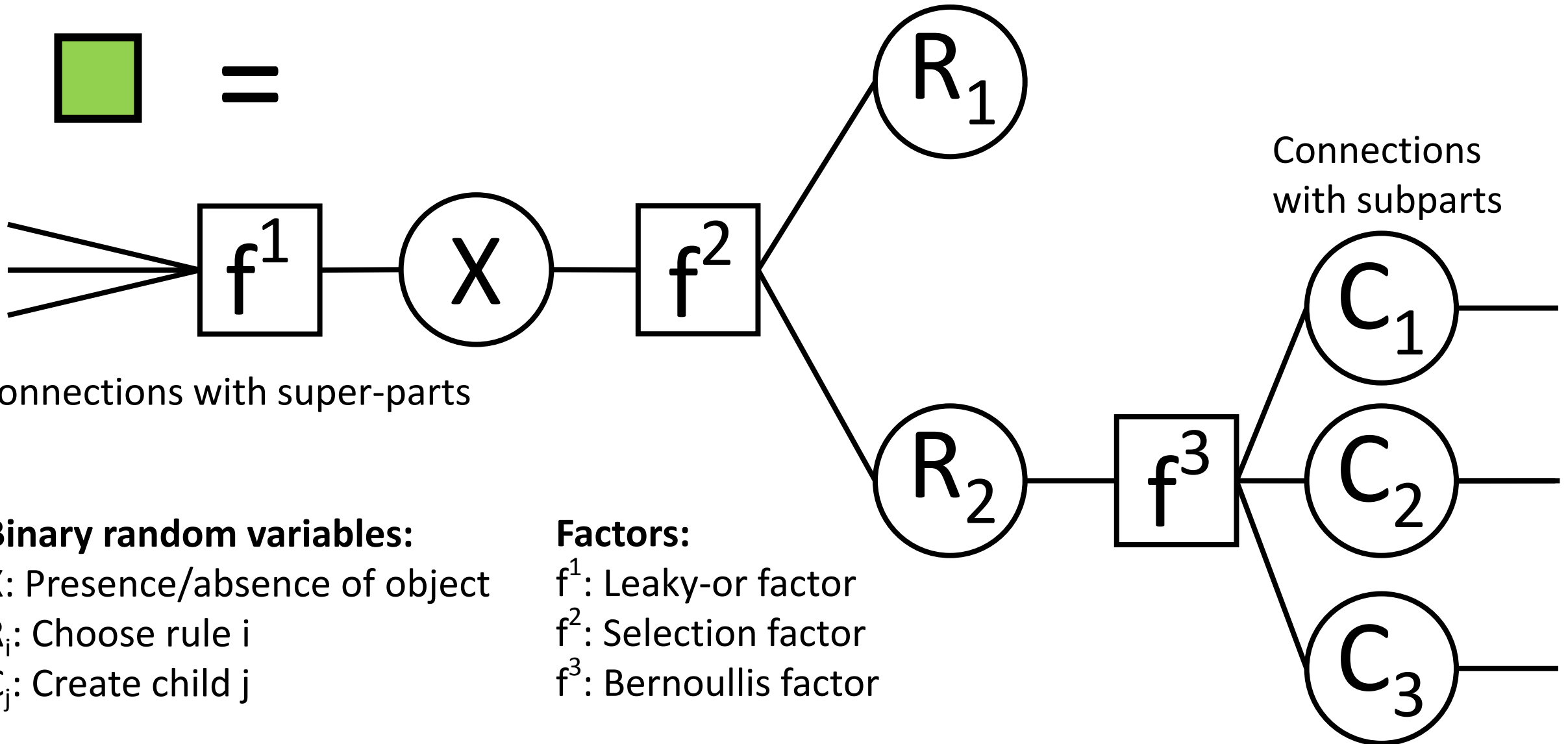
$f^1$ : Leaky-or factor

$f^2$ : Selection factor

# Framework: As a Factor Graph



=



Connections with super-parts

Connections with subparts

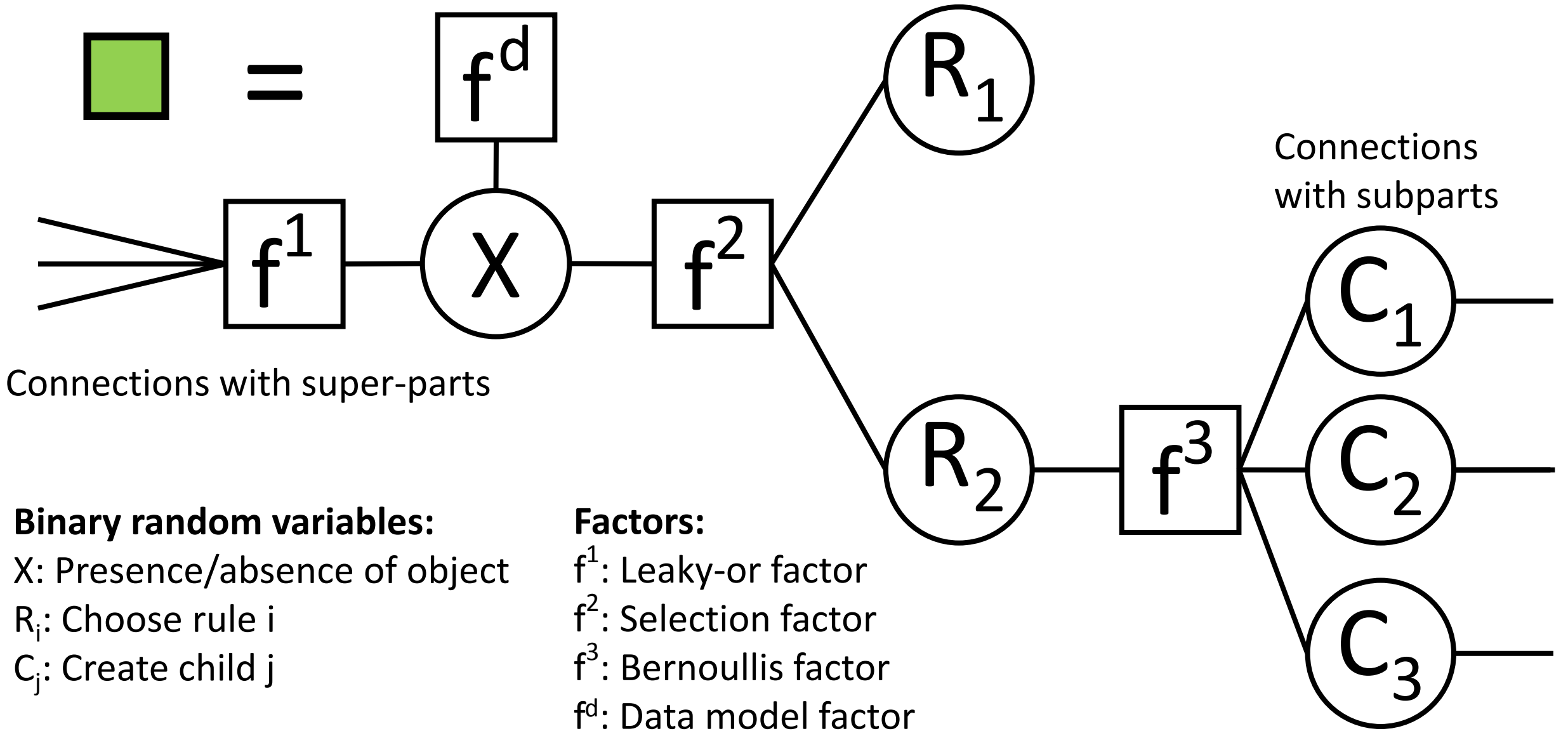
## Binary random variables:

- $X$ : Presence/absence of object
- $R_i$ : Choose rule  $i$
- $C_j$ : Create child  $j$

## Factors:

- $f^1$ : Leaky-or factor
- $f^2$ : Selection factor
- $f^3$ : Bernoullis factor

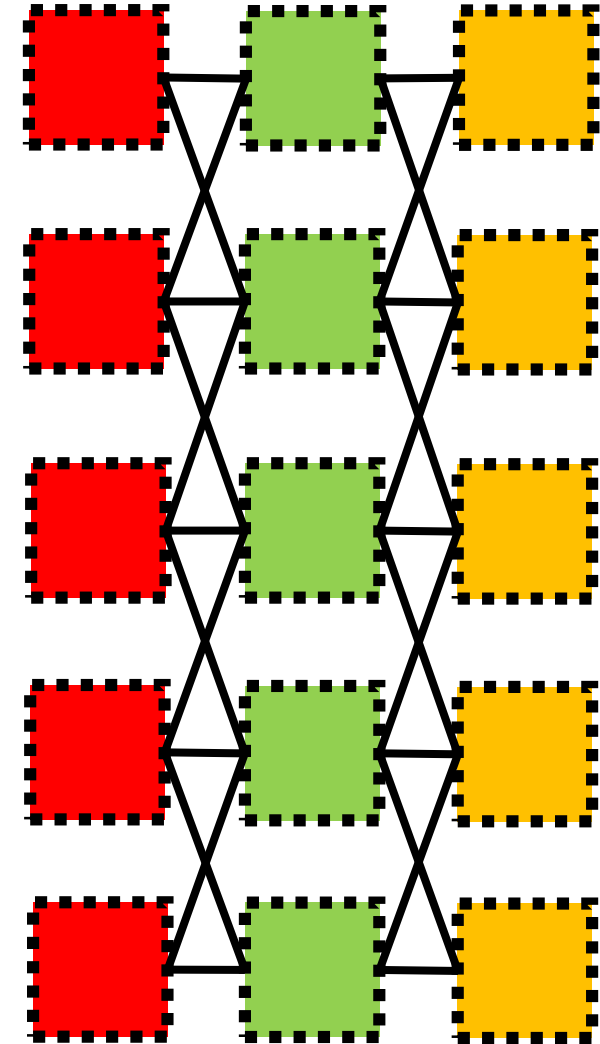
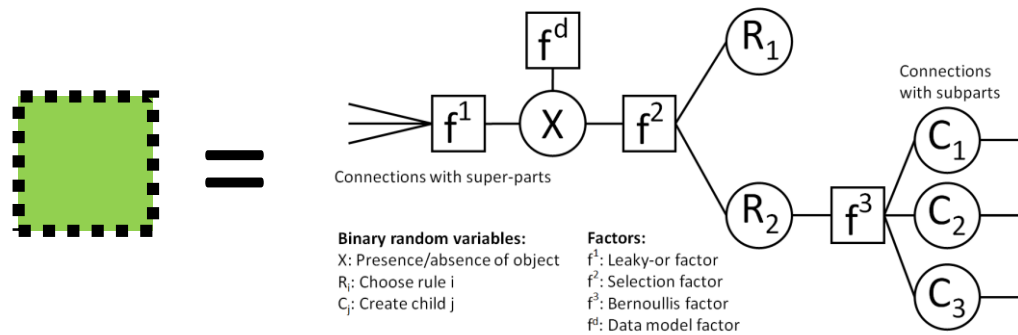
# Framework: As a Factor Graph





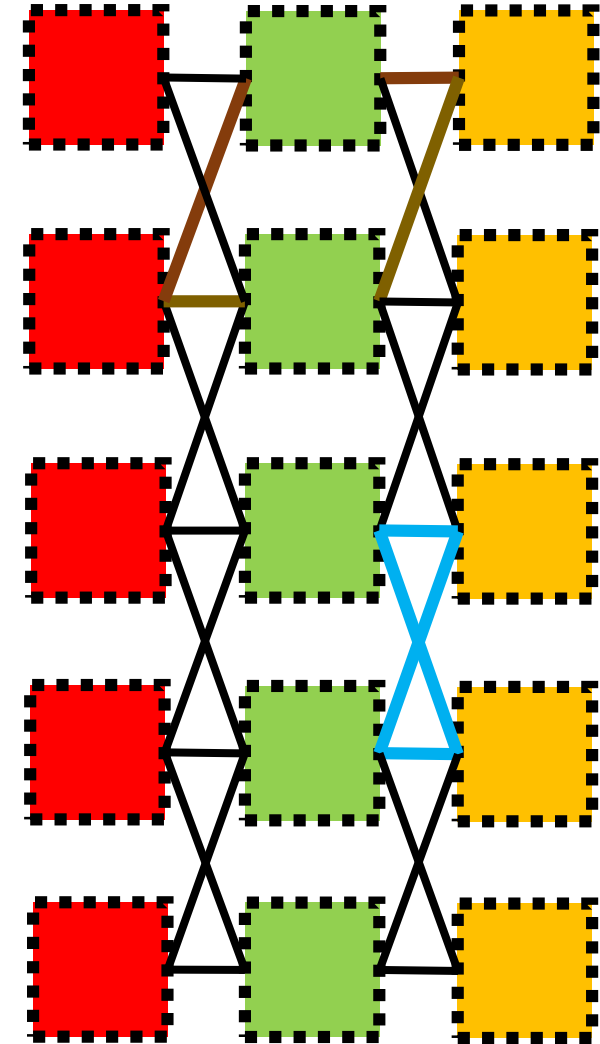
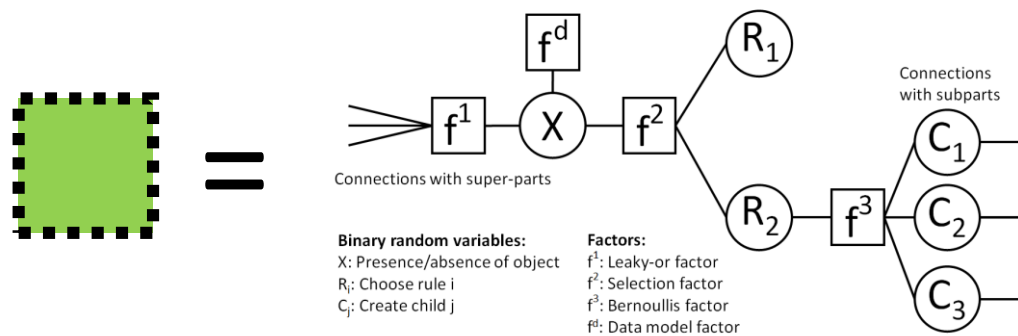
# Framework: As a Factor Graph

- Symbols: **Face**, **Eye**, **Eyelashes**
- 1D pose spaces
- Spatial neighbourhoods:
  - **Face**( $y$ )  $\rightarrow$  **Eye**( $y'$ ),  $y' = \{y-1, y, y+1\}$
  - **Eye**( $y$ )  $\rightarrow$  **EyeLashes**( $y'$ ),  $y' = \{y-1, y, y+1\}$



# Framework: As a Factor Graph

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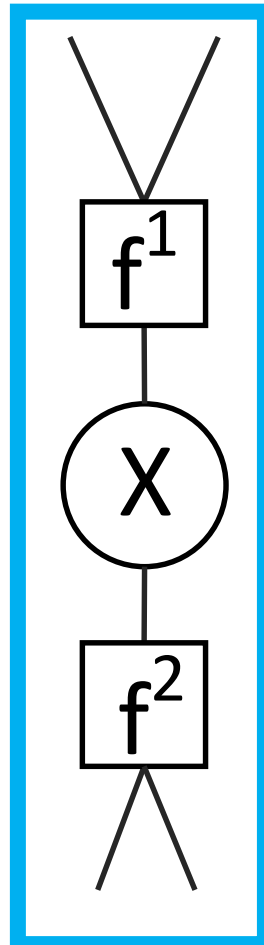


# The Probabilistic Scene Grammar Framework

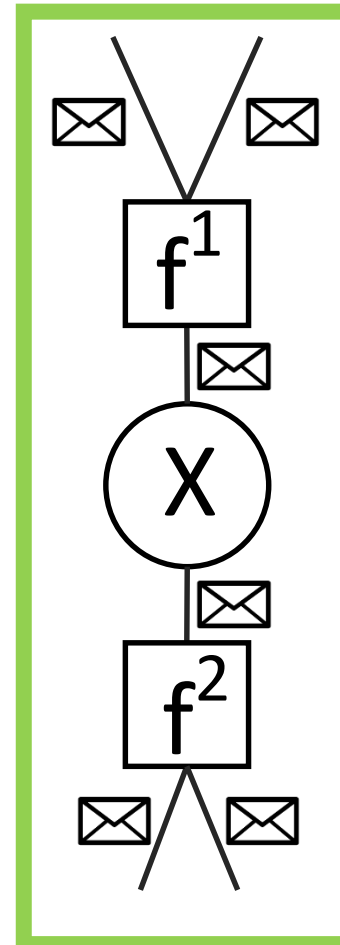
Probabilistic Scene Grammar



Factor graph



Inference

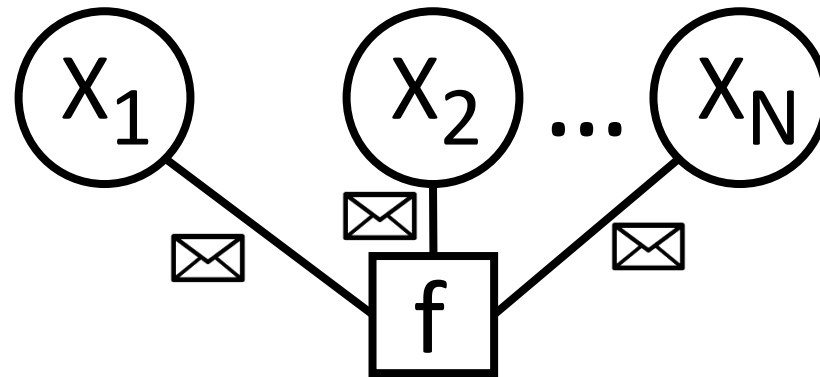


Learning



# Approximate Inference

- Given an image, what objects are in the image and what are their parts?
- Run Loopy Belief Propagation on the factor graph
  - Compute (approximate) posterior quantities,  $\hat{p}(\cdot | \text{Image})$



$$\mu_{f \rightarrow x_i}(x_i) = \sum_{x_1} \cdots \sum_{x_{i-1}} \sum_{x_{i+1}} \cdots \sum_{x_N} f(x_1, \dots, x_N) \prod_{j \neq i} \mu_{x_j \rightarrow f}(x_j)$$

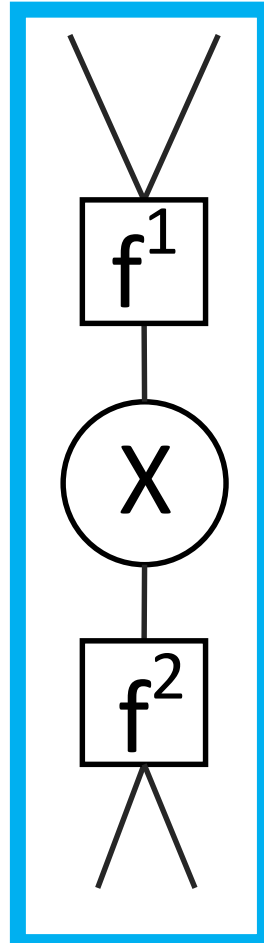
- In general: **exponential** time. Our case: **linear** time.

# The Probabilistic Scene Grammar Framework

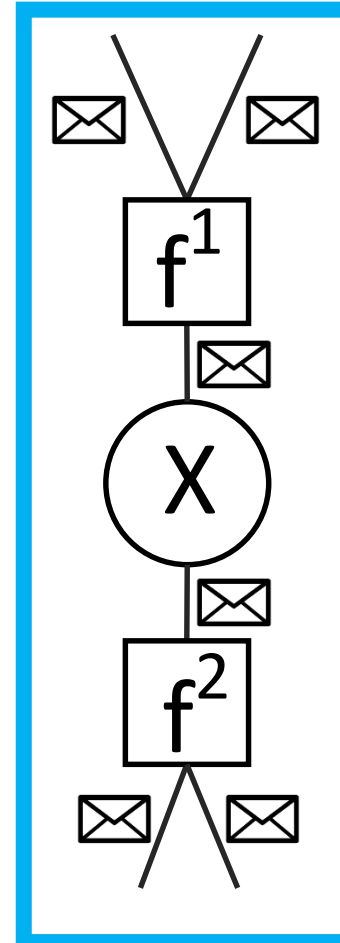
Probabilistic Scene Grammar



Factor graph



Inference



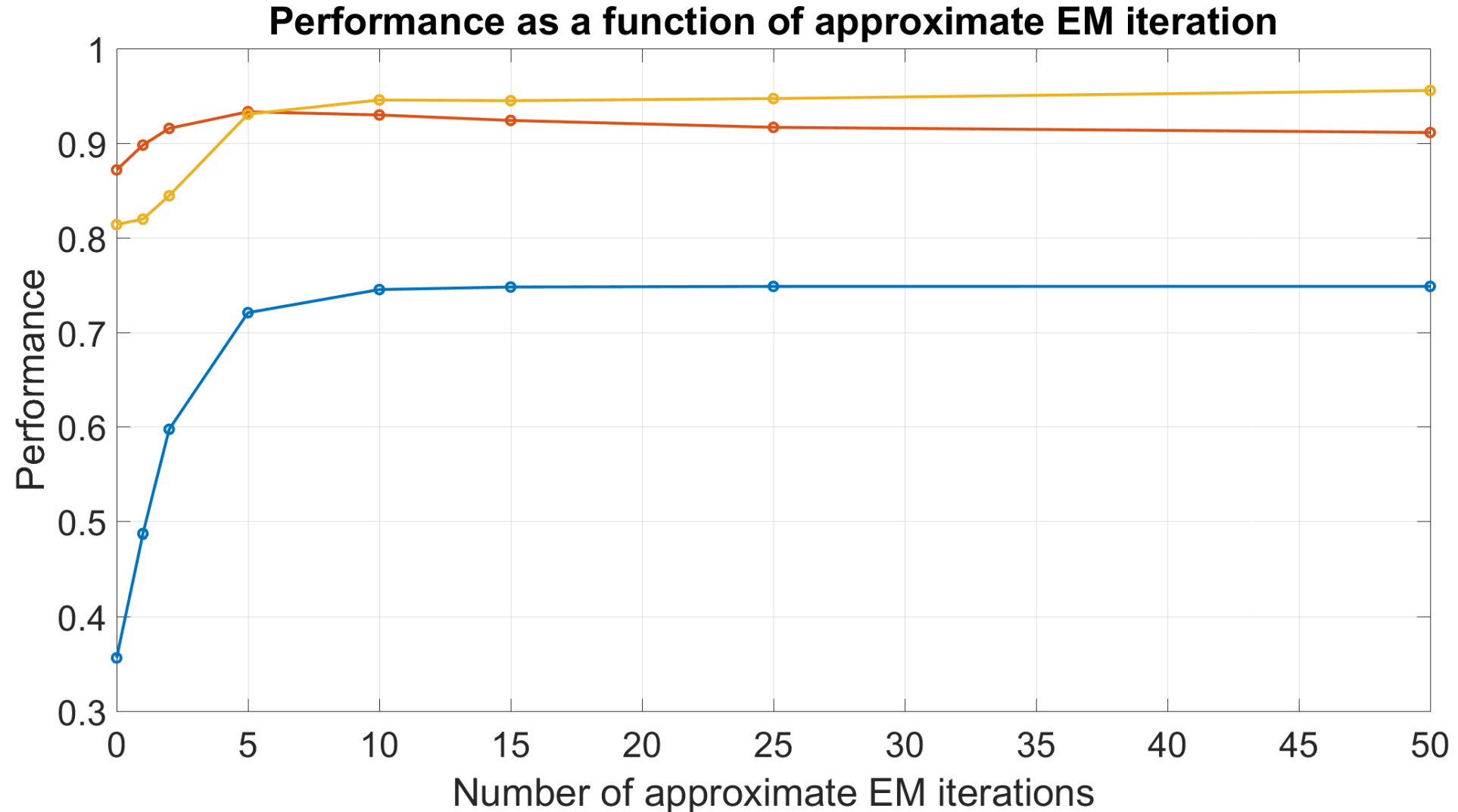
Learning



# Learning: Approximate EM algorithm

- Goal: Estimate model parameters
  - Rule probabilities
  - Geometric relationships
  - Leaky-or parameter
- **Maximization-step**: sums involving posterior quantities
- Exact posterior quantities are intractable to compute
- **Expectation-step**: use approximate posteriors computed by Loopy Belief Propagation

# Learning: Approximate EM algorithm



# This talk

- **Motivation** for a general scene understanding framework
- **Background/related work**
- **Representation** for general scene understanding tasks
- Efficient **approximate inference algorithm**
- **Learning algorithm** to estimate model parameters
- **Experimental evaluation**
- **Extensions** for larger/more complex tasks
- **Directions** for future research

**PSG**



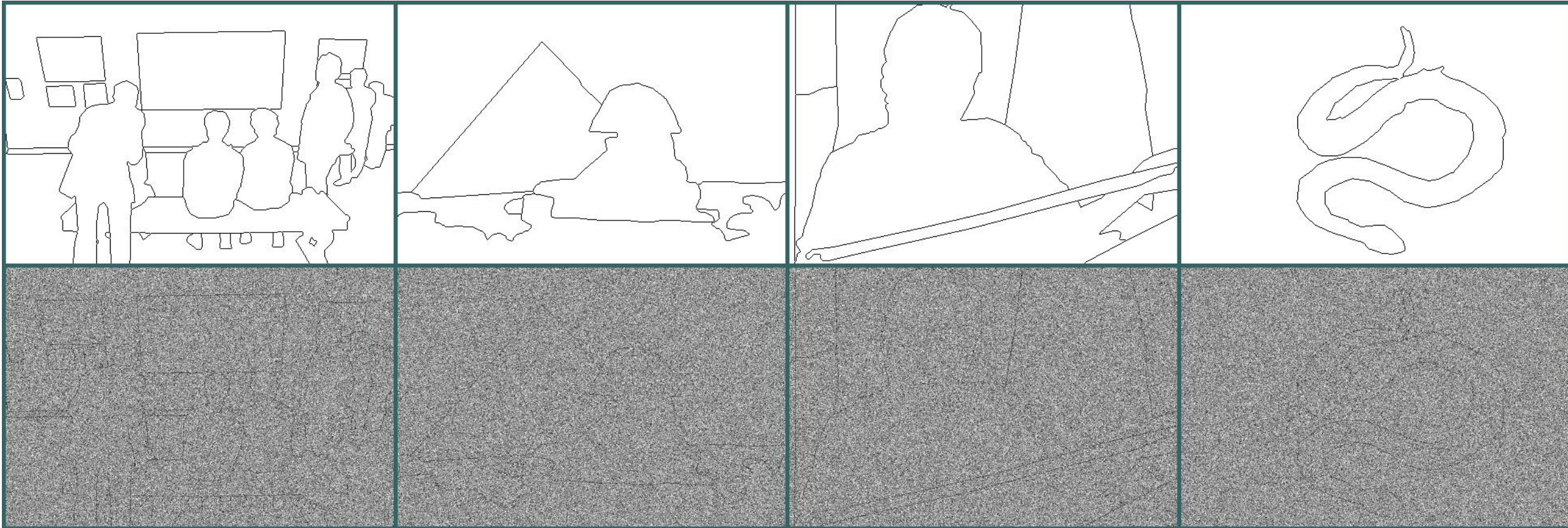


# This talk

- **Motivation** for a general scene understanding framework
- **Background/related work**
- **Representation** for general scene understanding tasks
- Efficient **approximate inference algorithm**
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- • **Experimental evaluation**
- **Extensions** for larger/more complex tasks
- **Directions** for future research

PSG framework is competitive with  
some specialized frameworks

# Application: contour detection



# Application: contour detection

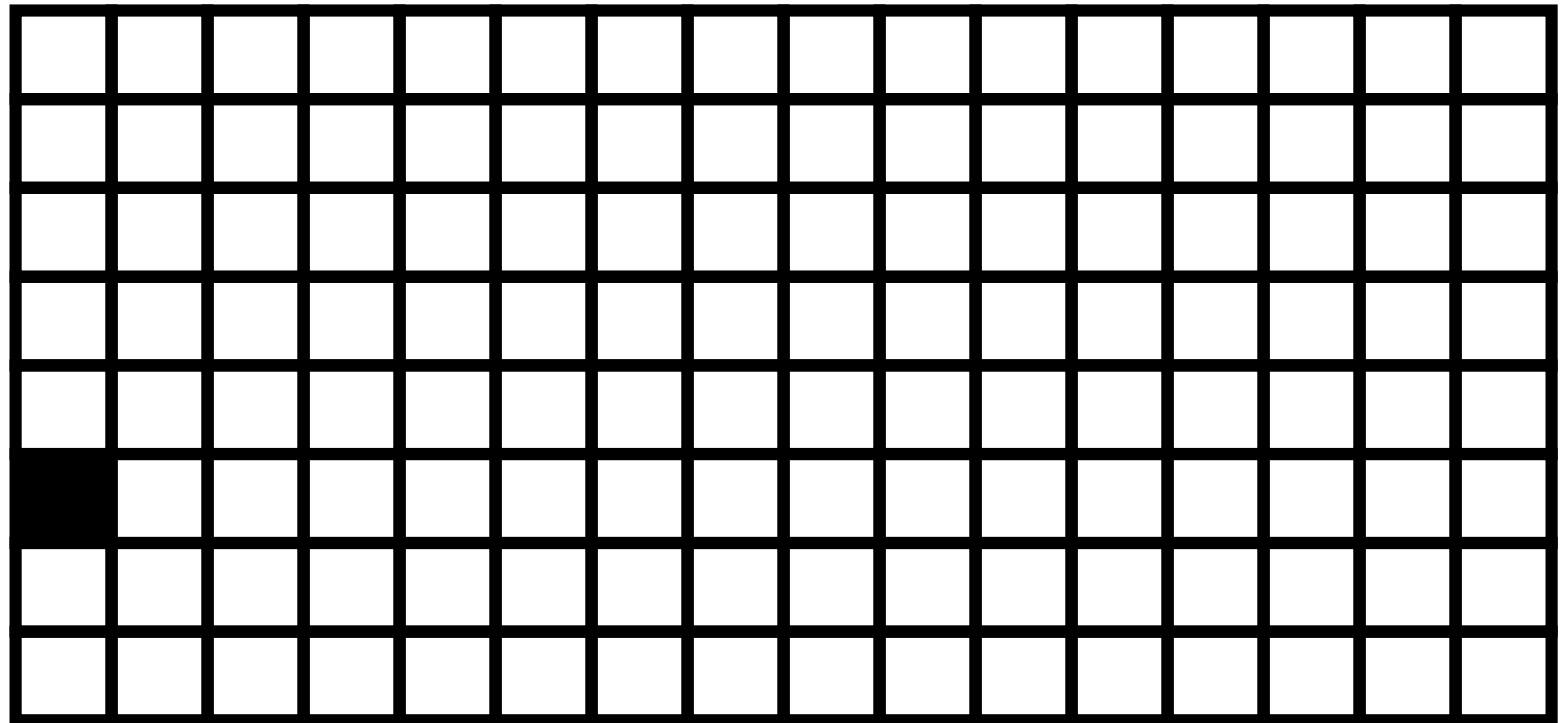
- Dataset:
  - Ground truth: human-drawn object boundary contours from Berkeley Segmentation Dataset [1]
  - $B(x,y)$ : Binary value of whether this pixel belongs to a contour
  - $D(x,y)$ : Pixel intensity
  - Data-model:  $D(x,y) \sim N(\mu_{B(x,y)}, \sigma)$

[1] Arbelaez, Maire, Fowlkes, Malik. "Contour Detection and hierarchical image segmentation", PAMI 2011.

# Application: contour detection

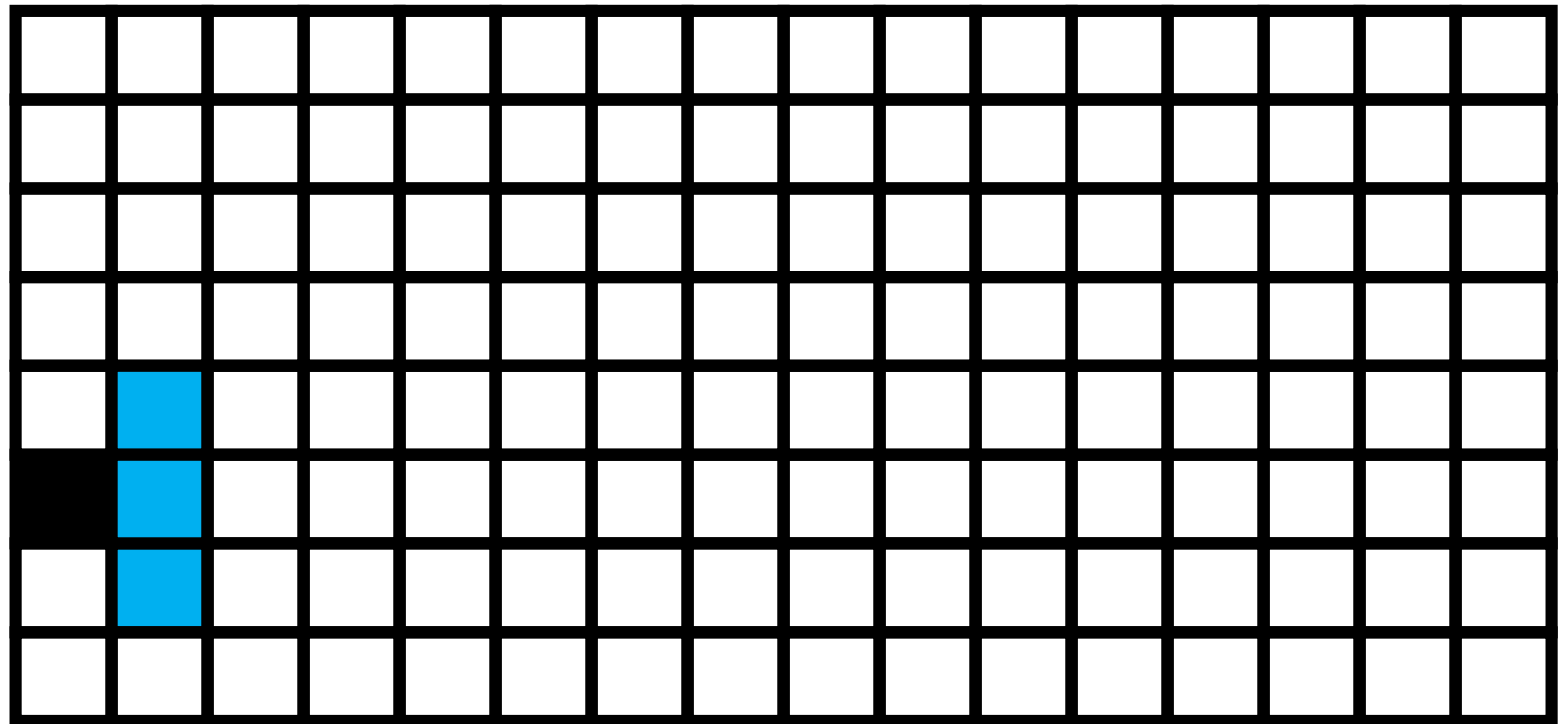
- Model:
  - Simple grammar model (next slides)
  - Factor graph contains  $\sim 50\text{M}$  edges
- Training:
  - Model parameters estimated using approximate EM algorithm
  - 200 train, 200 test

# Generating a curve

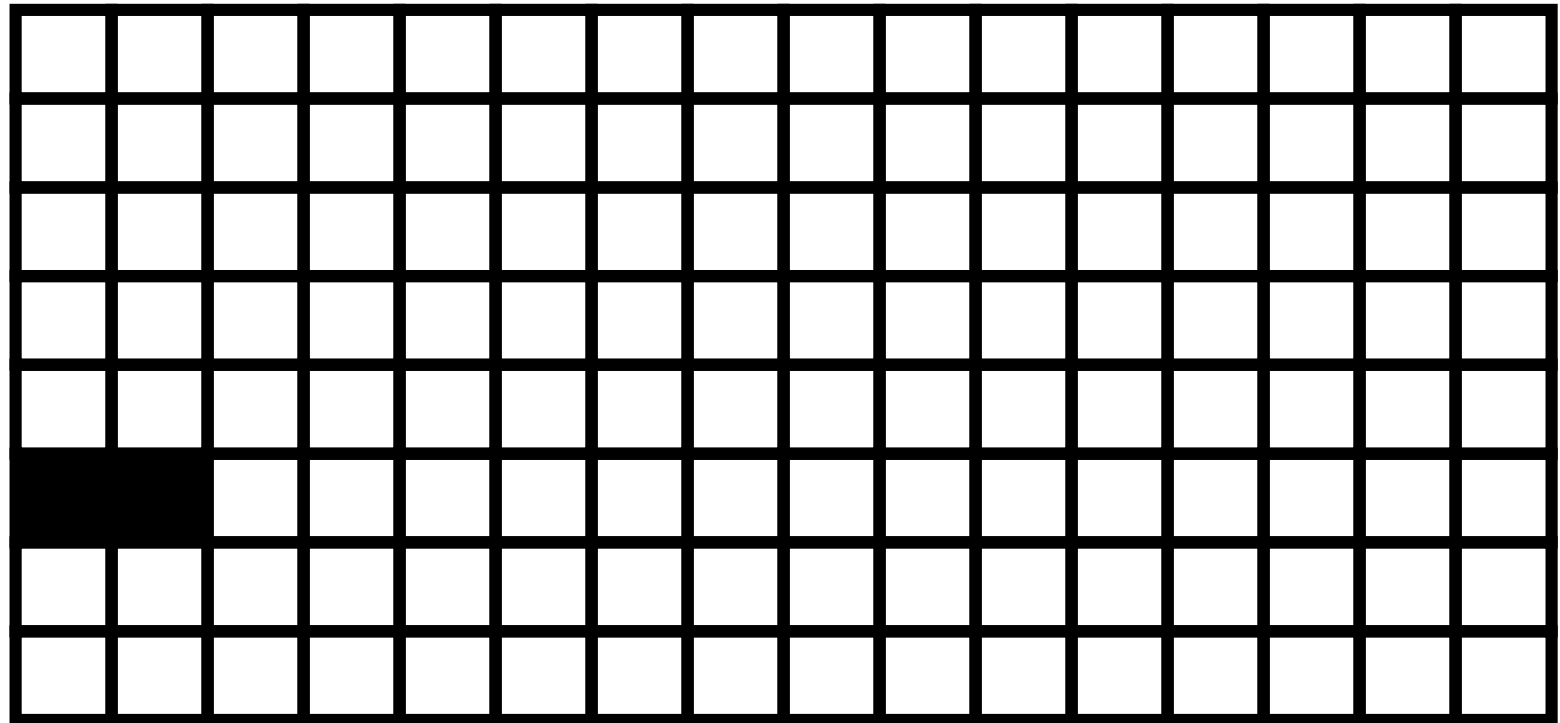


# Generating a curve

Choose: continue contour, change orientation, or STOP



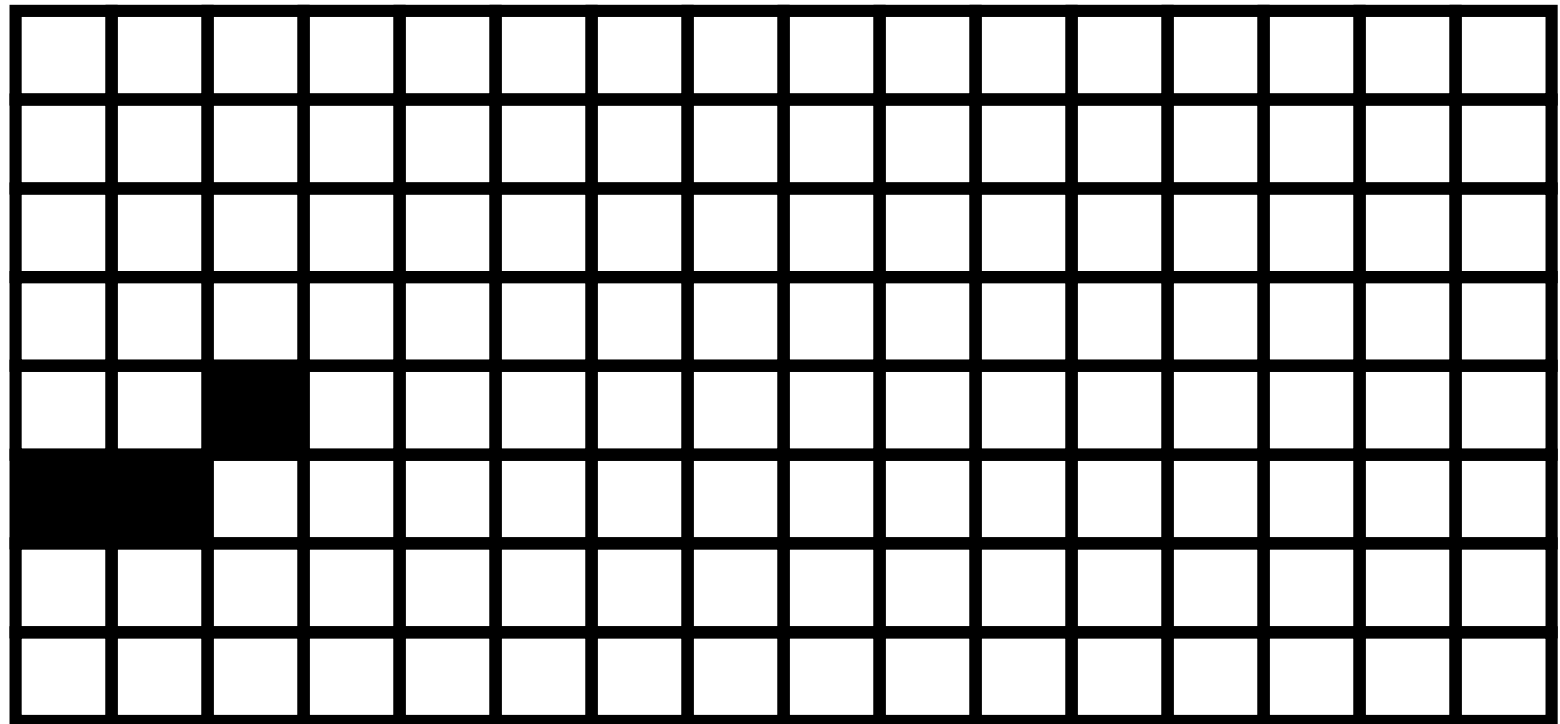
# Generating a curve





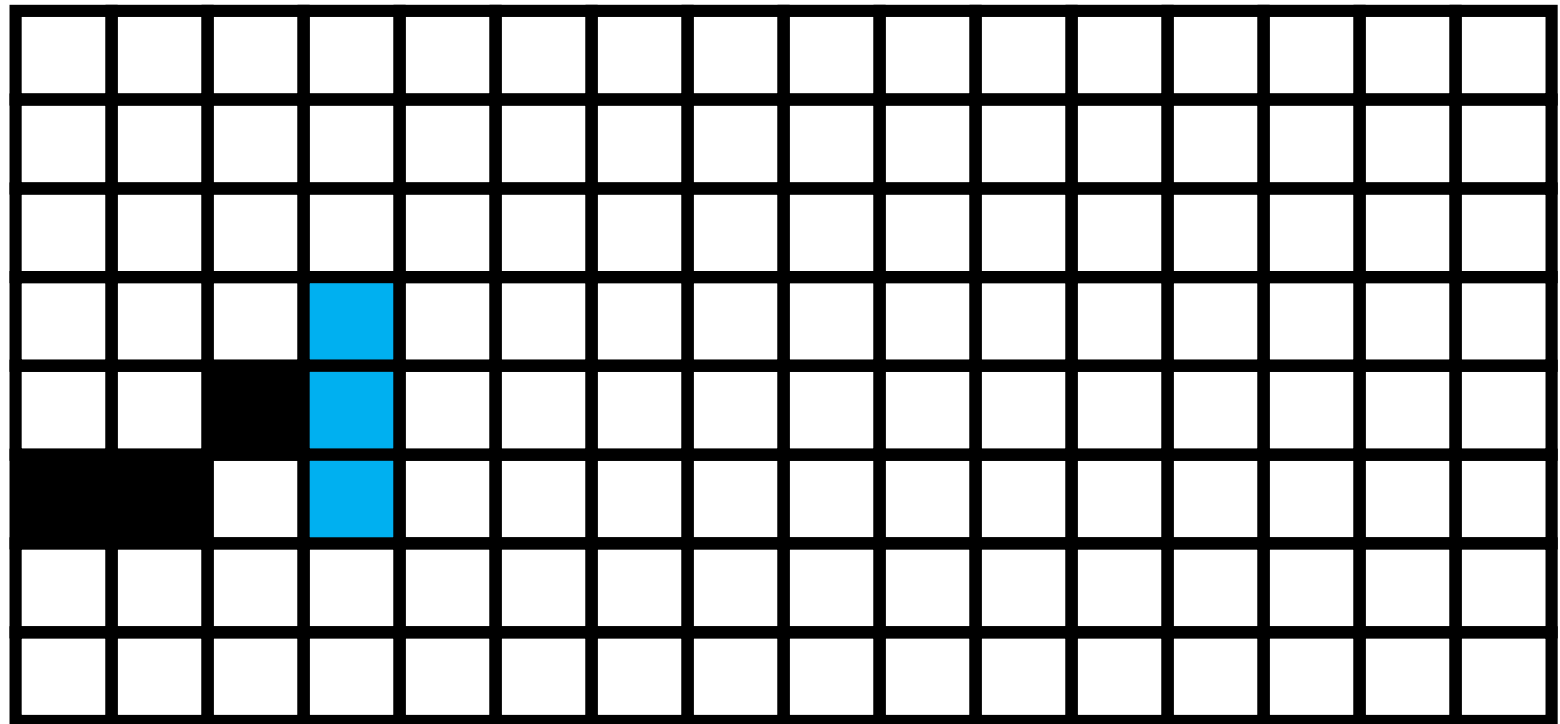


# Generating a curve



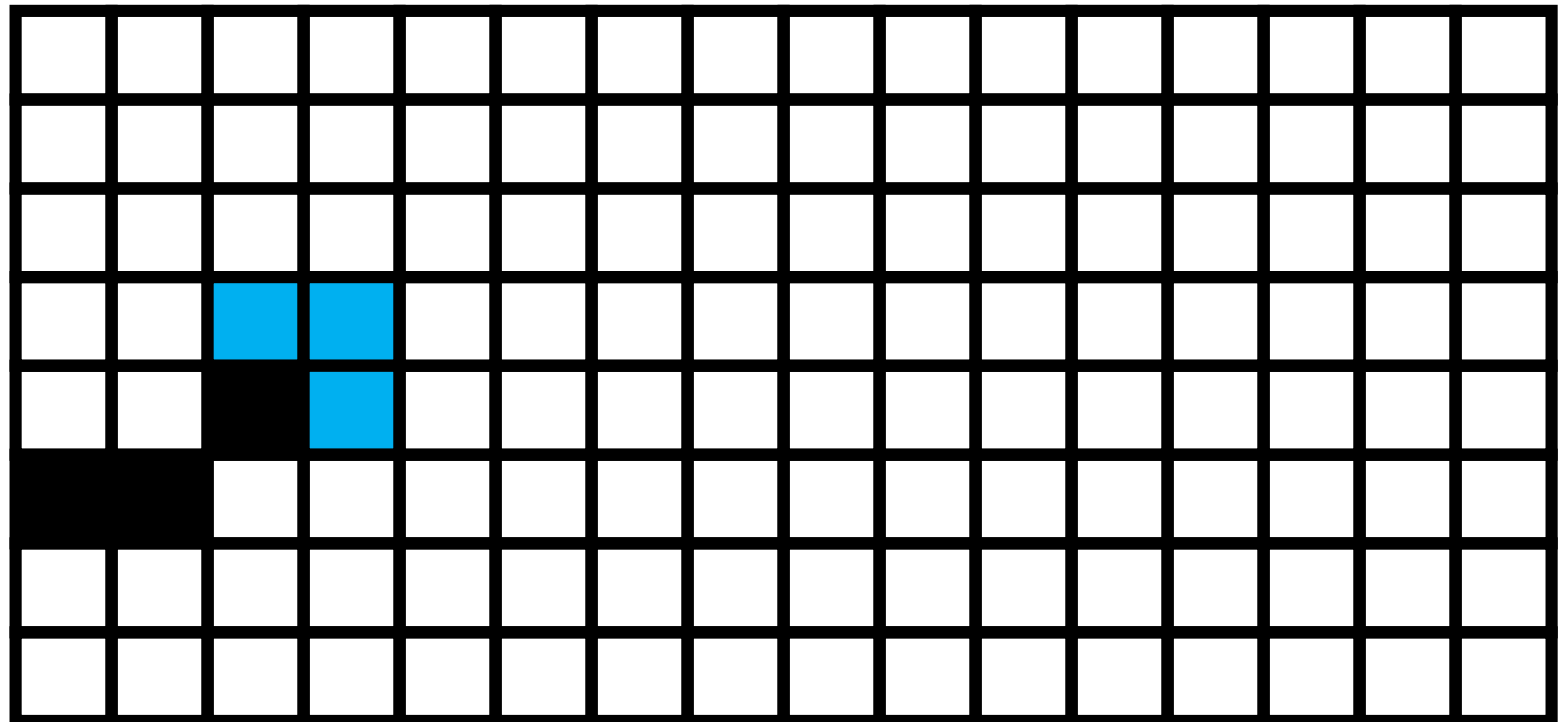
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Choose: continue contour, change orientation, or STOP



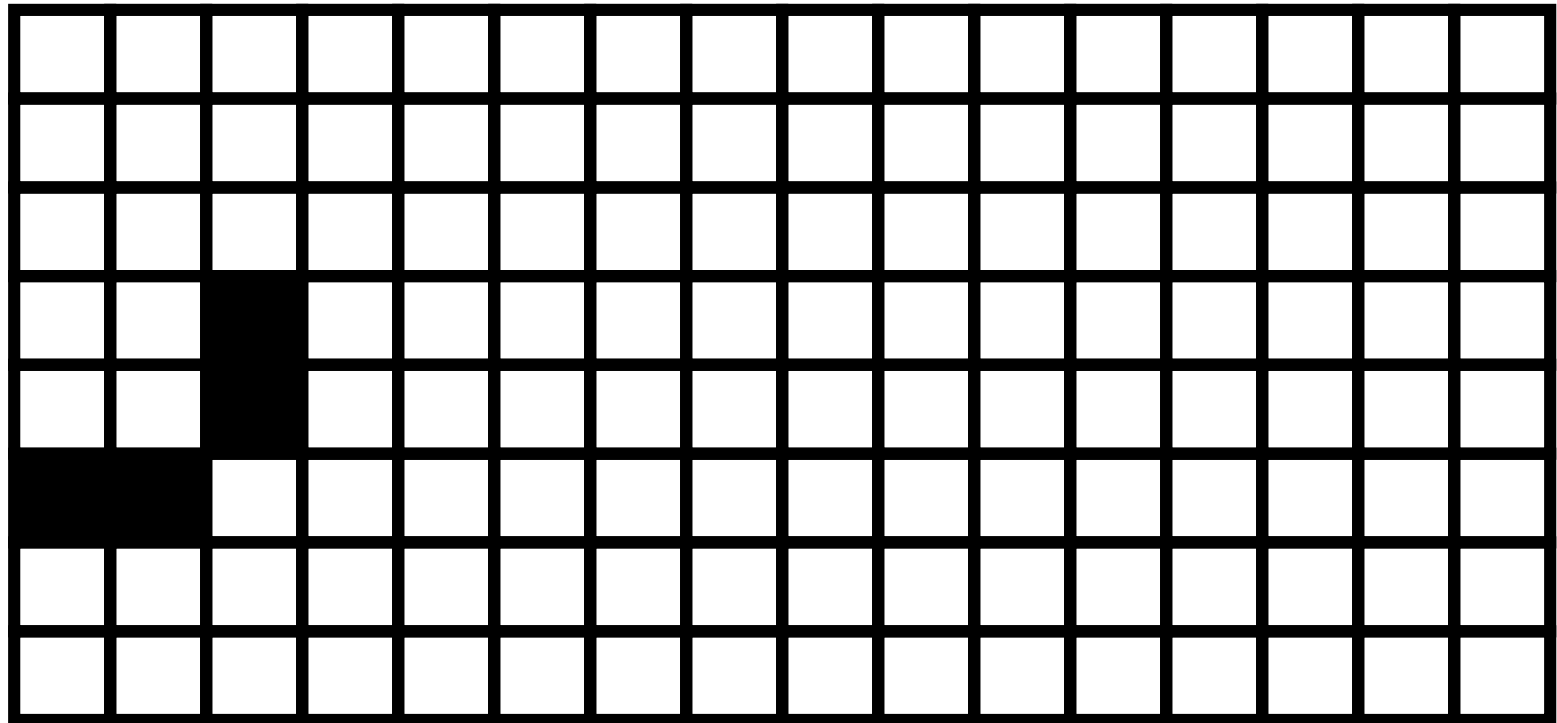
# Generating a curve

Choose: continue contour, change orientation, or STOP



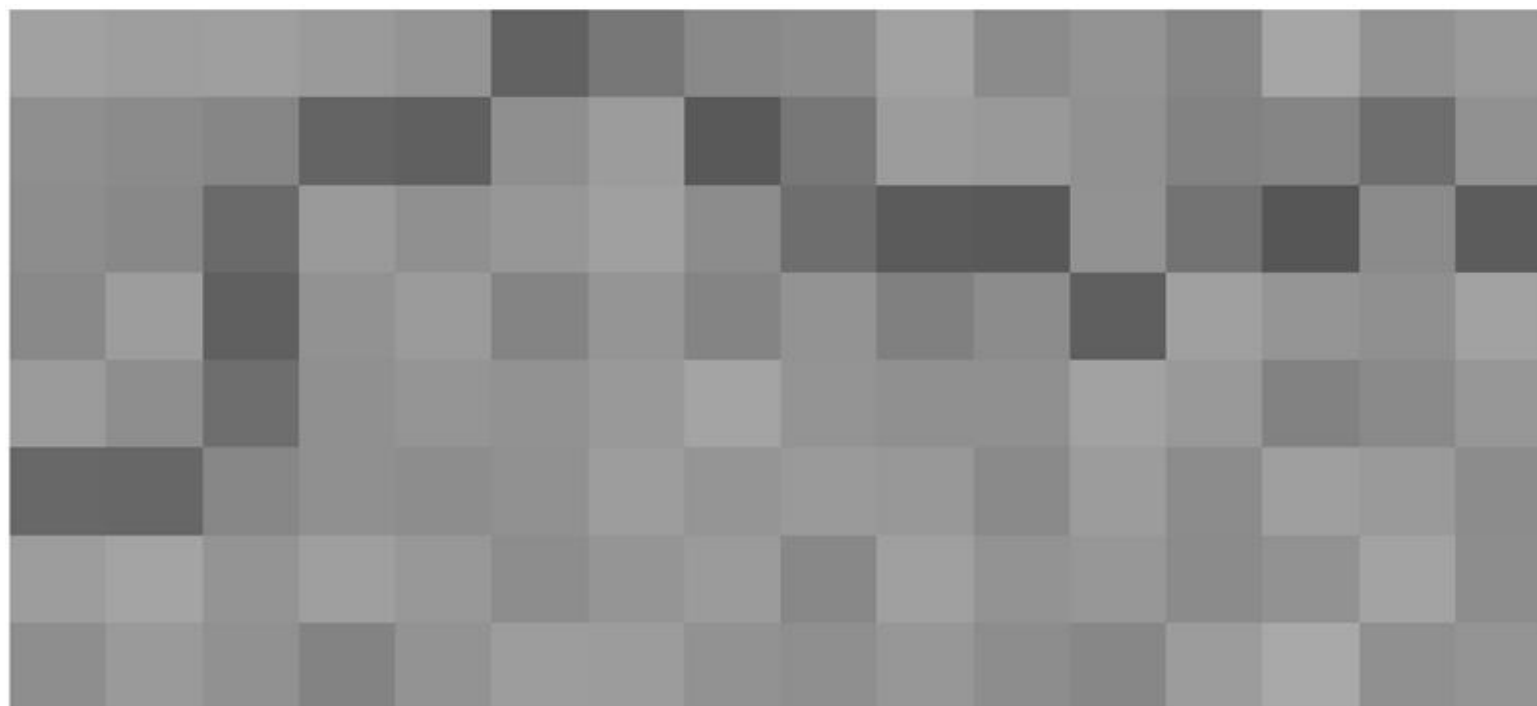


# Generating a curve





# Generating a curve





# Inferred contours

Ground truth

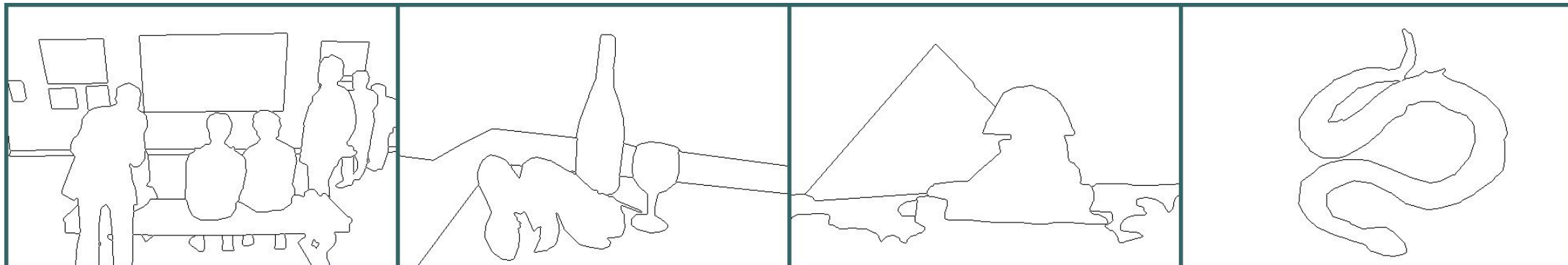
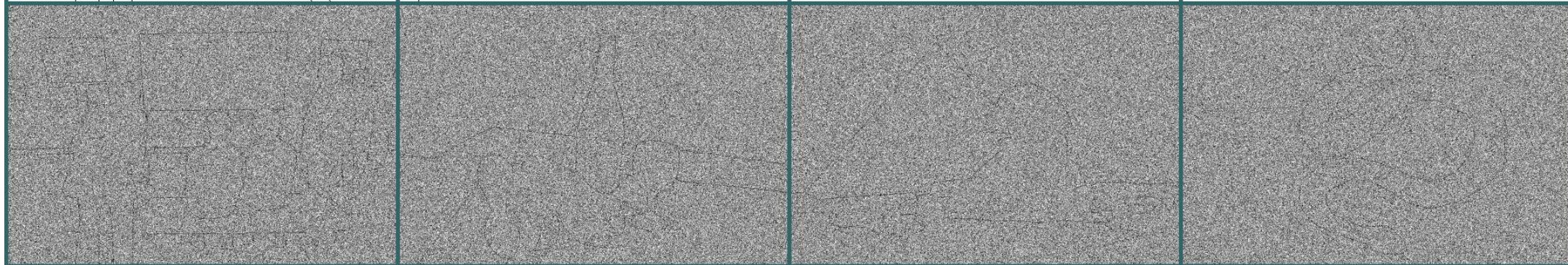
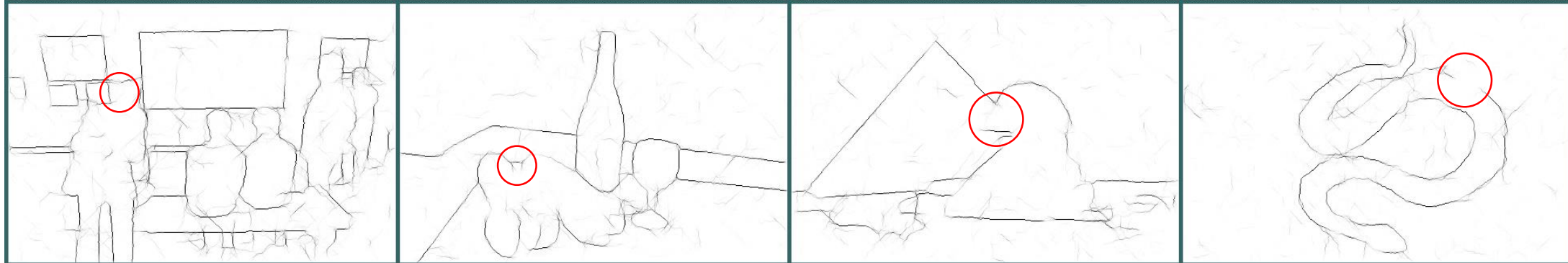


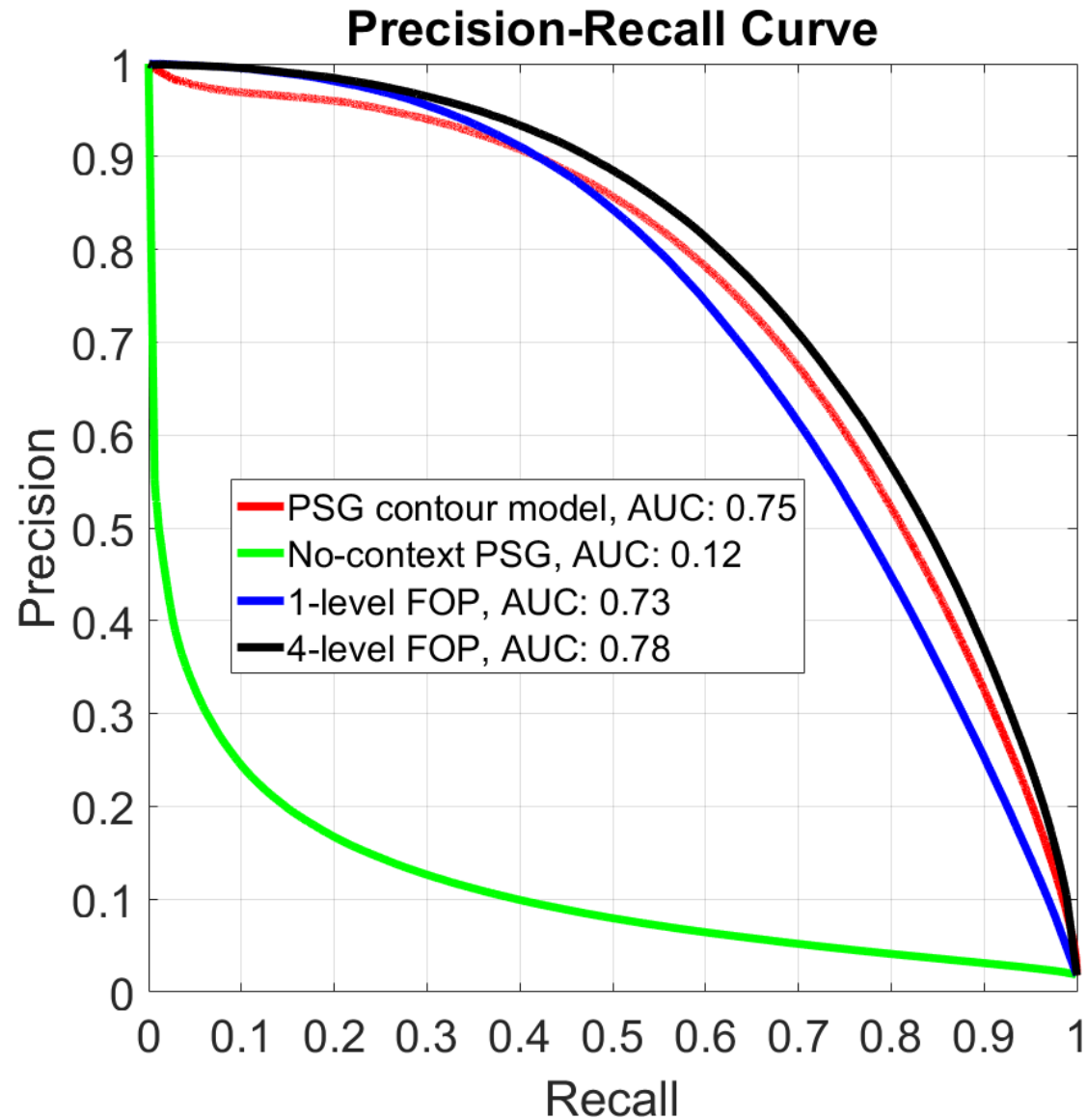
Image data



$P(B = 1 | \text{Image})$



# Contour detection: Comparison

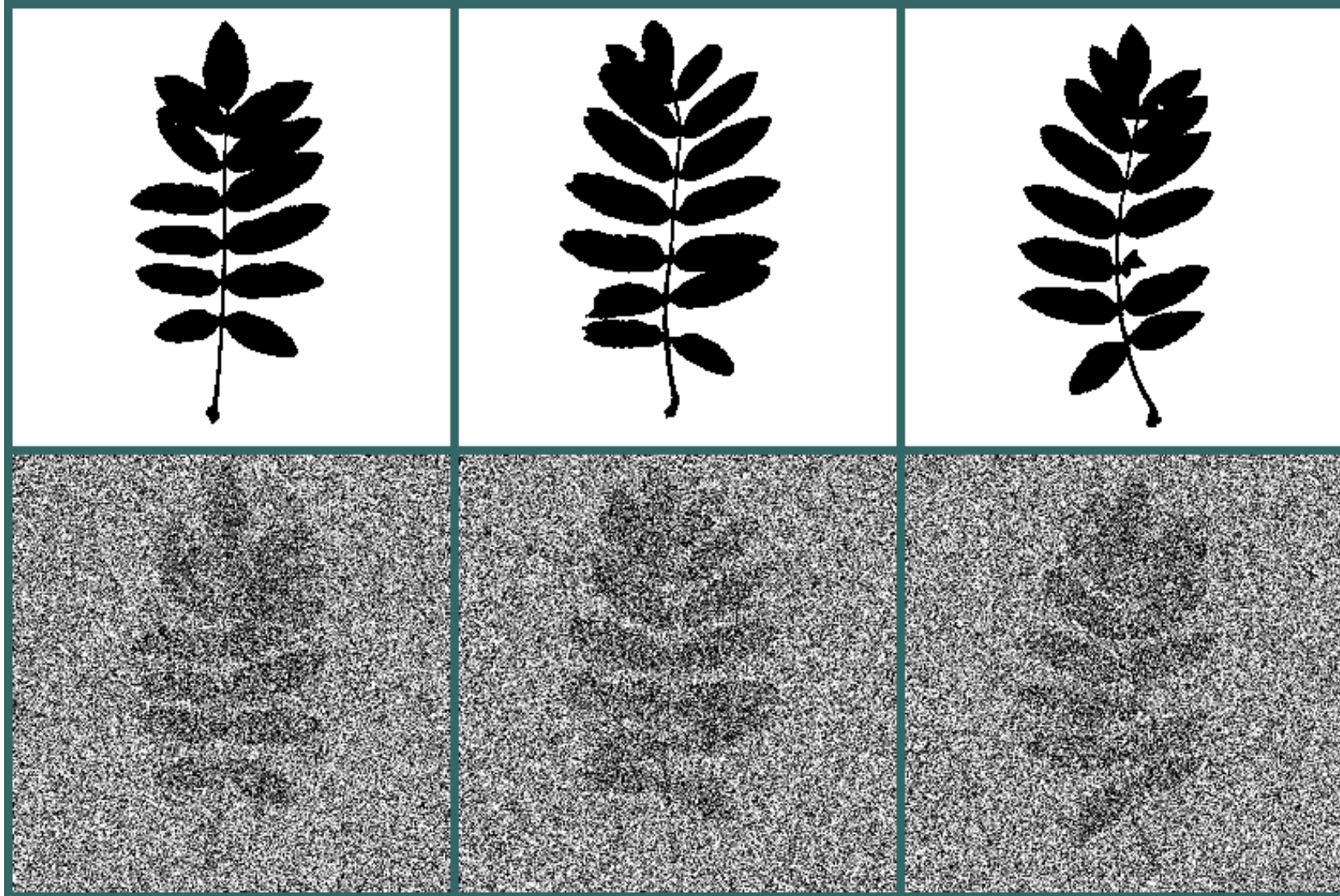


Context is important!

PSG framework competitive with Field-of-Patterns (FOP)

1-level FOP and 4-level FOP from: "Multiscale Field of Patterns", Felzenszwalb, Oberlin. NIPS 2014.

# Application: binary image segmentation



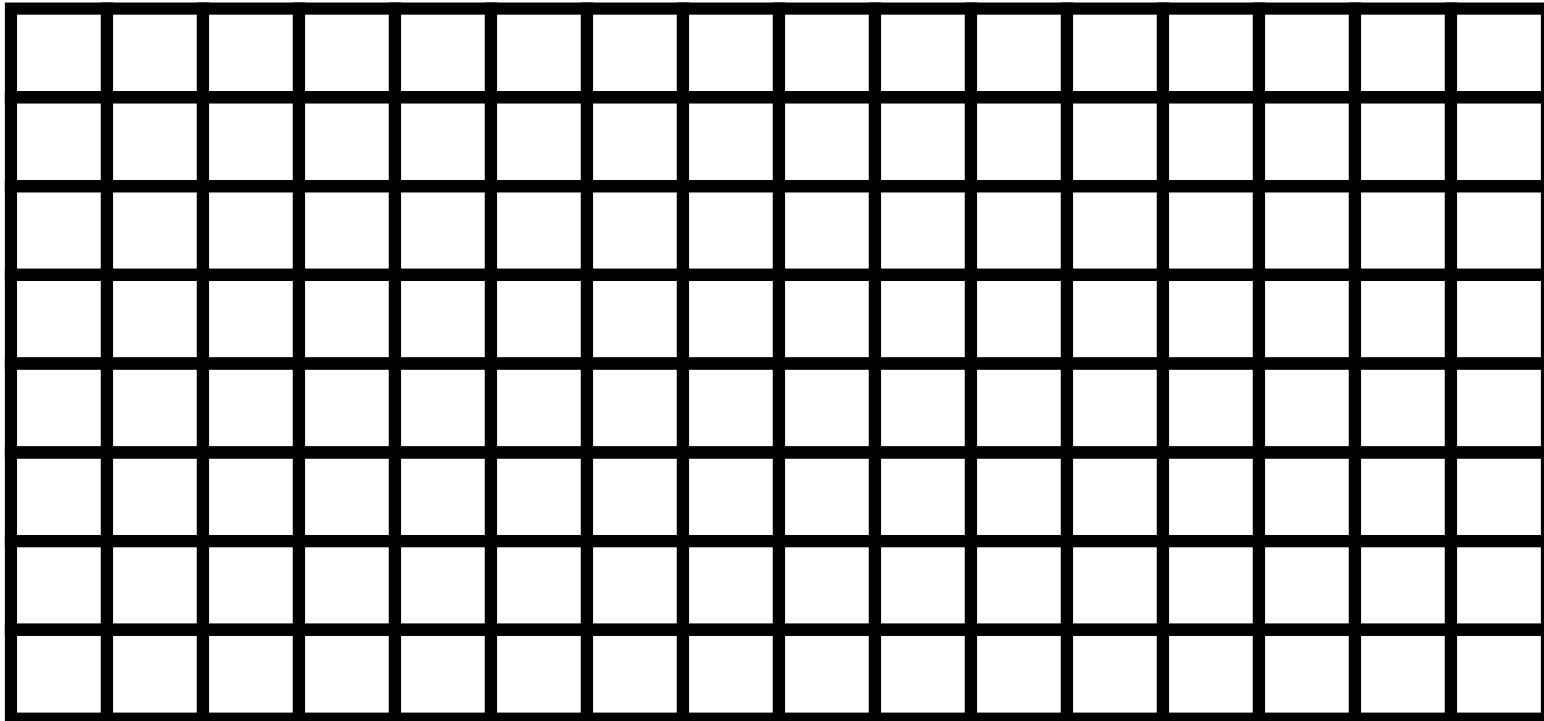
# Application: binary image segmentation

- Dataset:
  - Ground truth: binary leaf masks [1]
  - $B(x,y)$ : Binary value of whether this pixel belongs to a leaf
  - $D(x,y)$ : Pixel intensity
  - Data-model:  $D(x,y) \sim N(\mu_{B(x,y)}, \sigma)$

[1] Soderkvist. "Computer vision classification of leaves from Swedish trees", Master's thesis 2011.

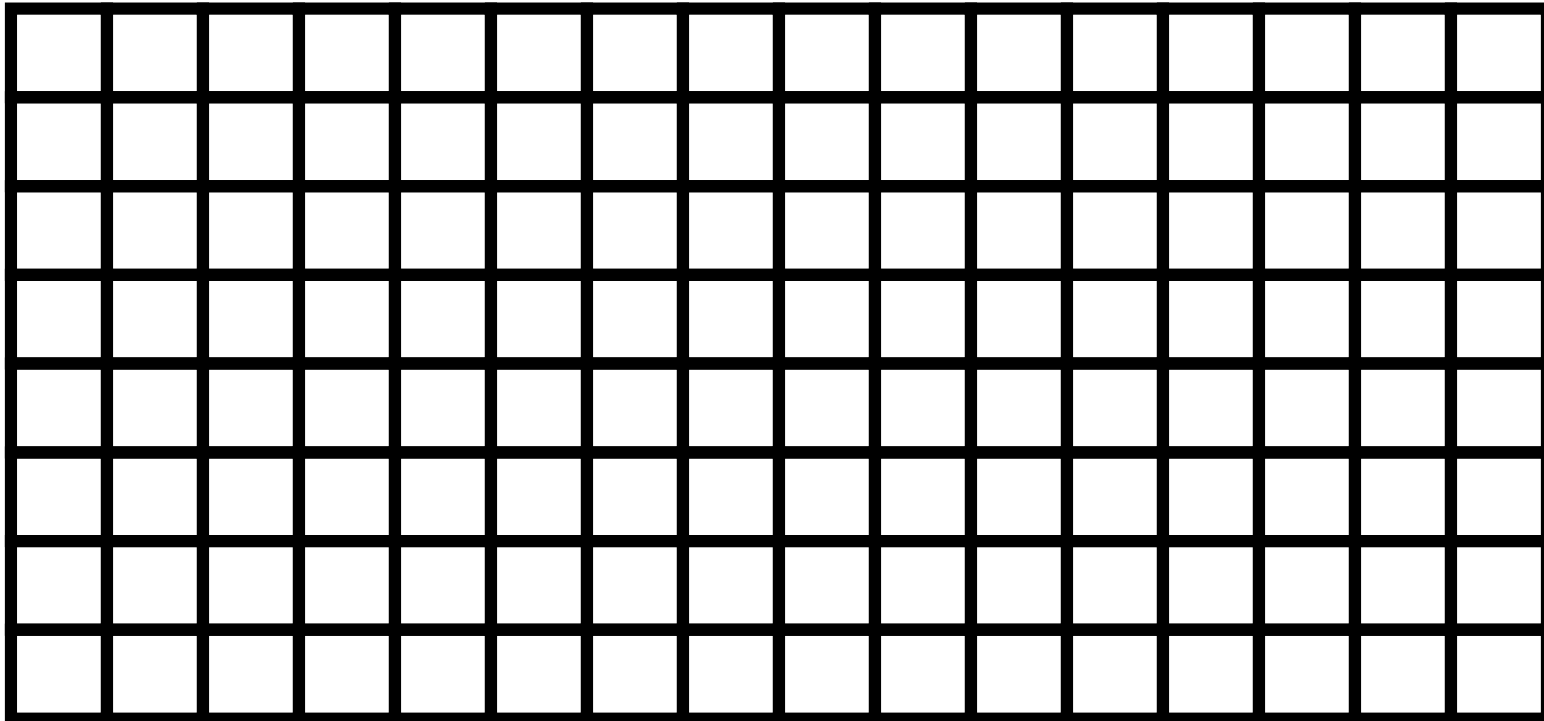
# Simple process to generate a binary mask

“Grow” a foreground. Red/black pixels are part of foreground.



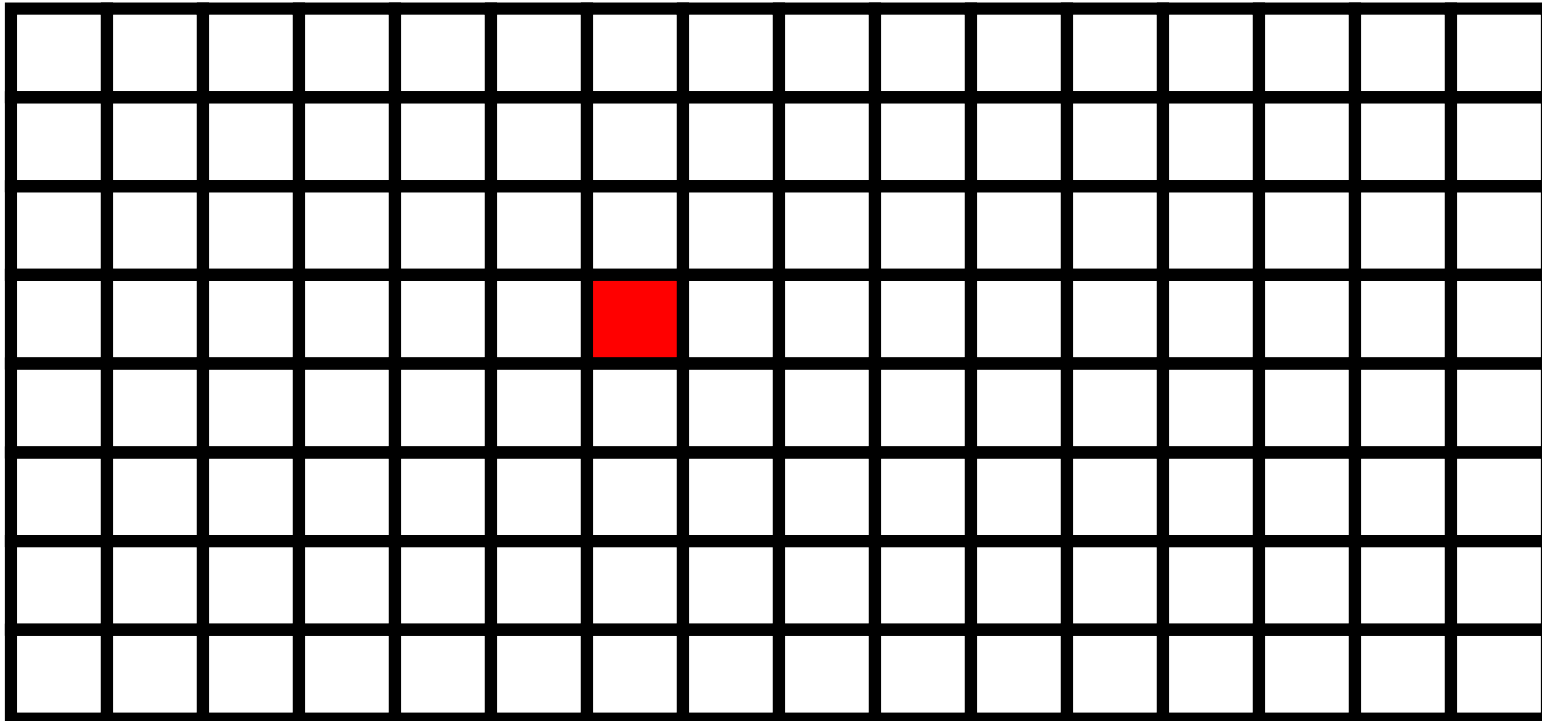
# Simple process to generate a binary mask

Choose a pixel to be part of the foreground. Colour it red.



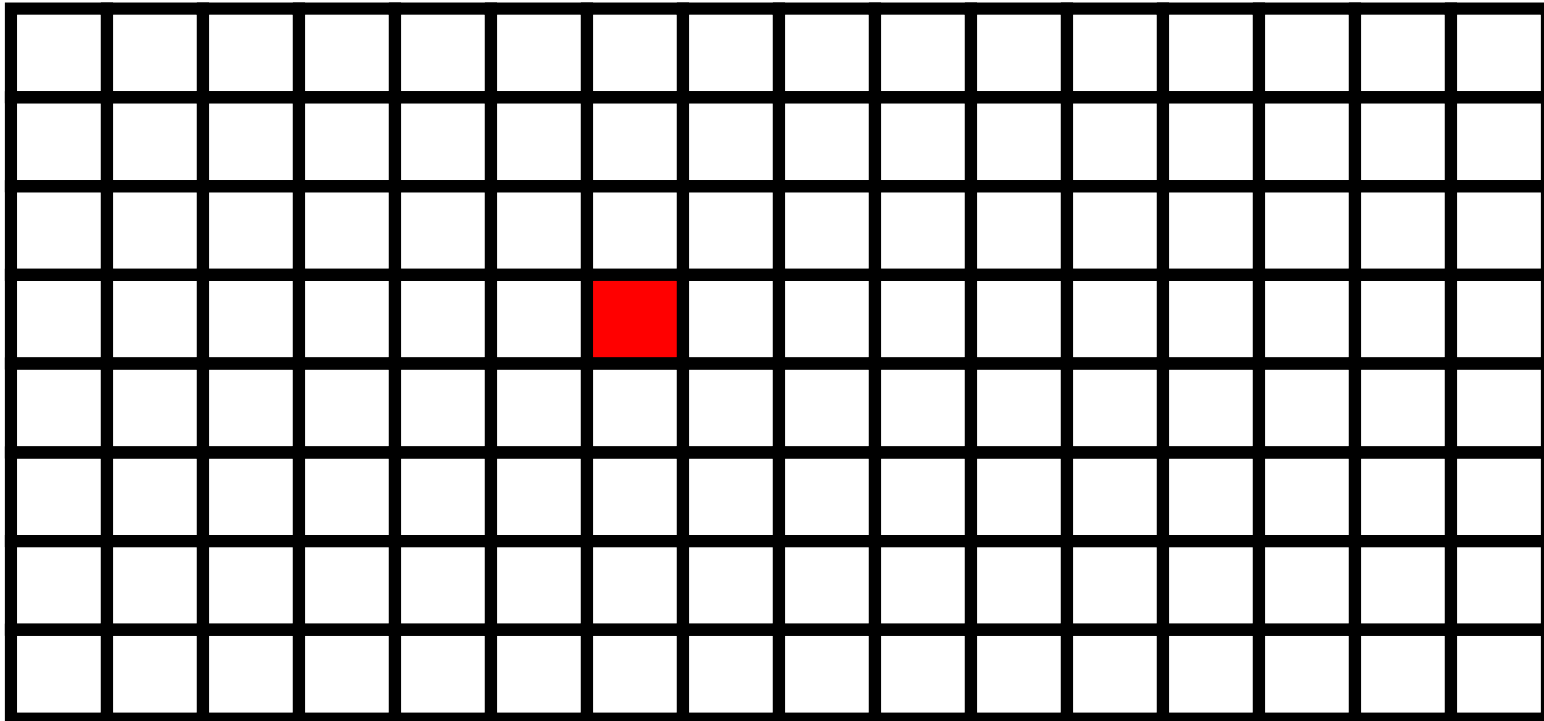
# Simple process to generate a binary mask

Choose a pixel to be part of the foreground. Colour it red.



# Simple process to generate a binary mask

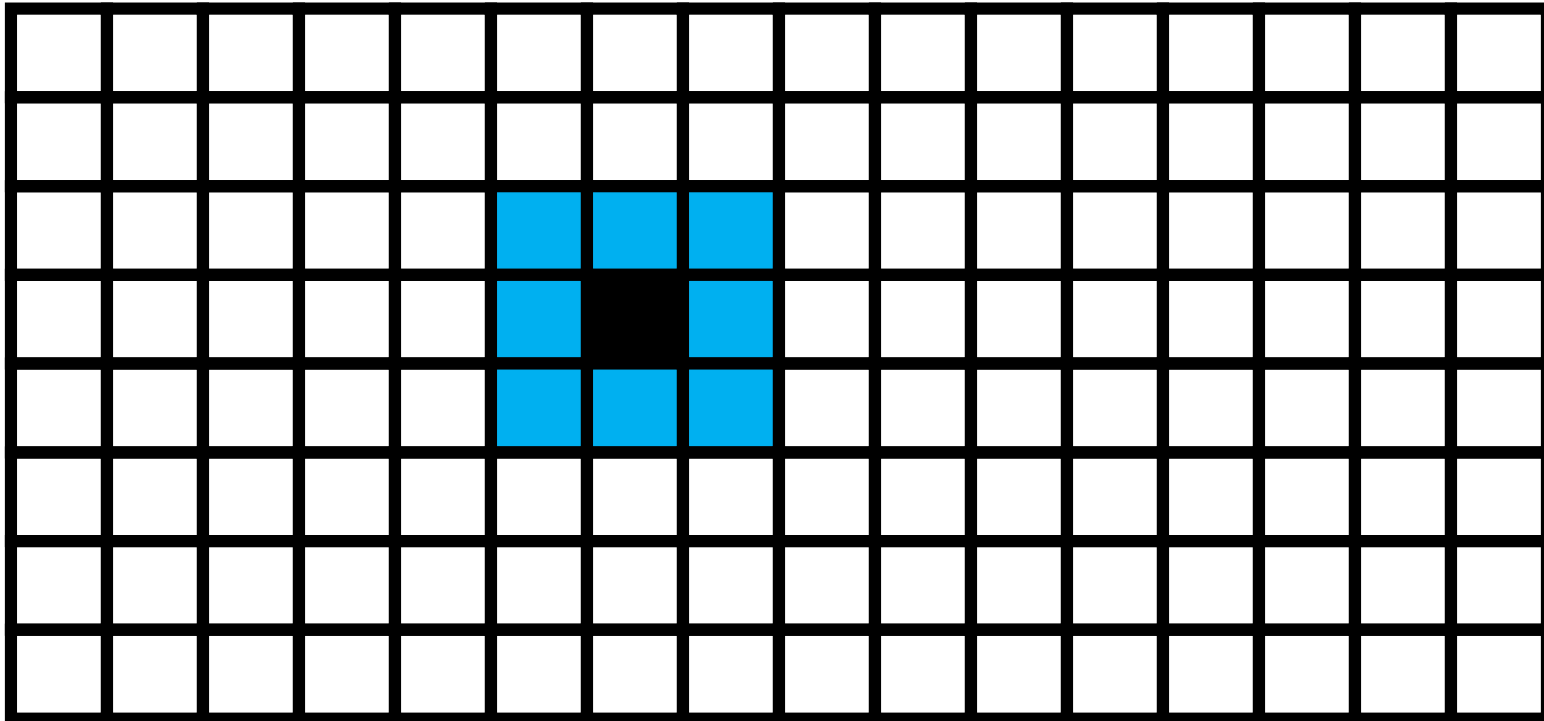
Pick a red pixel and change its colour to black. Select some neighbours to be part of the foreground, if they are not already, and colour them red.





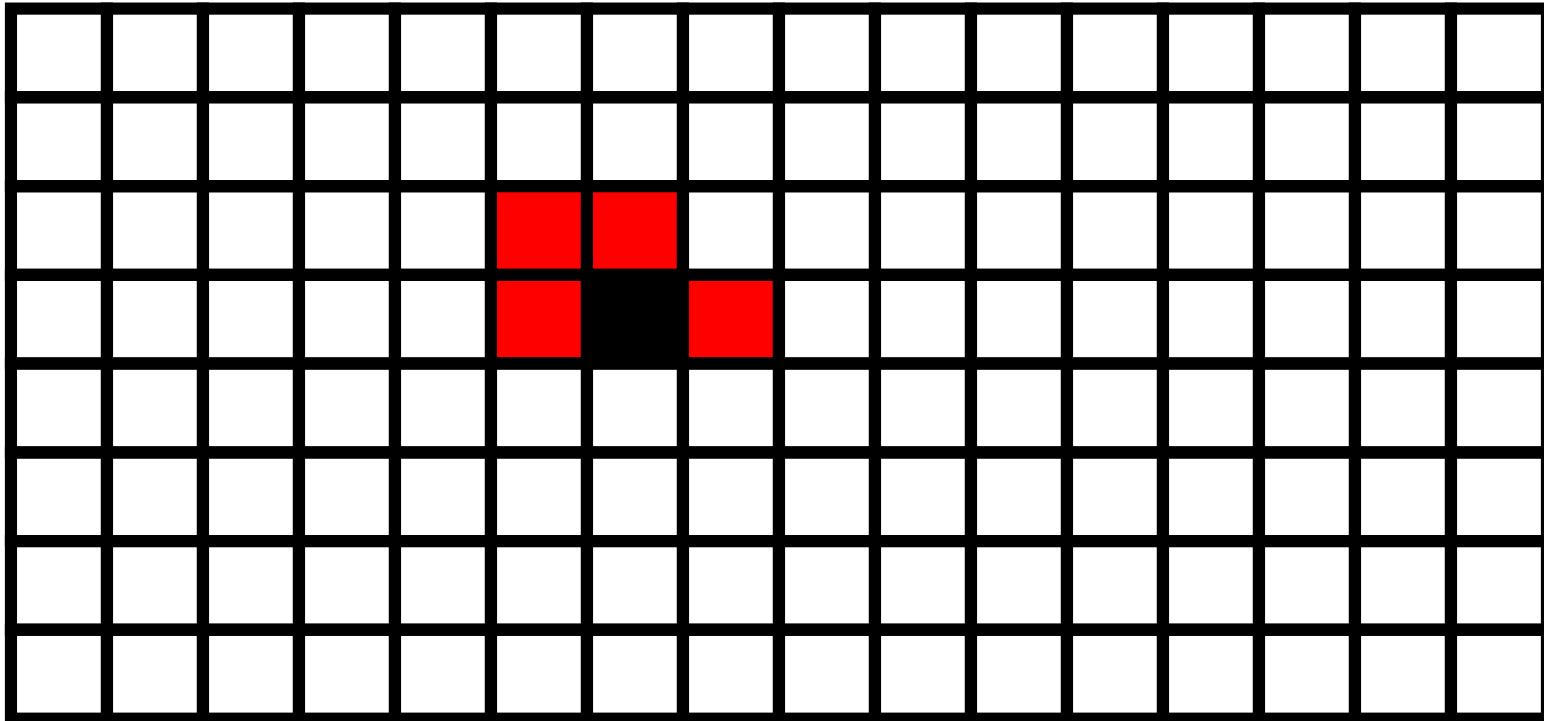
# Simple process to generate a binary mask

Pick a red pixel and change its colour to black. Select some neighbours to be part of the foreground, if they are not already, and colour them red.



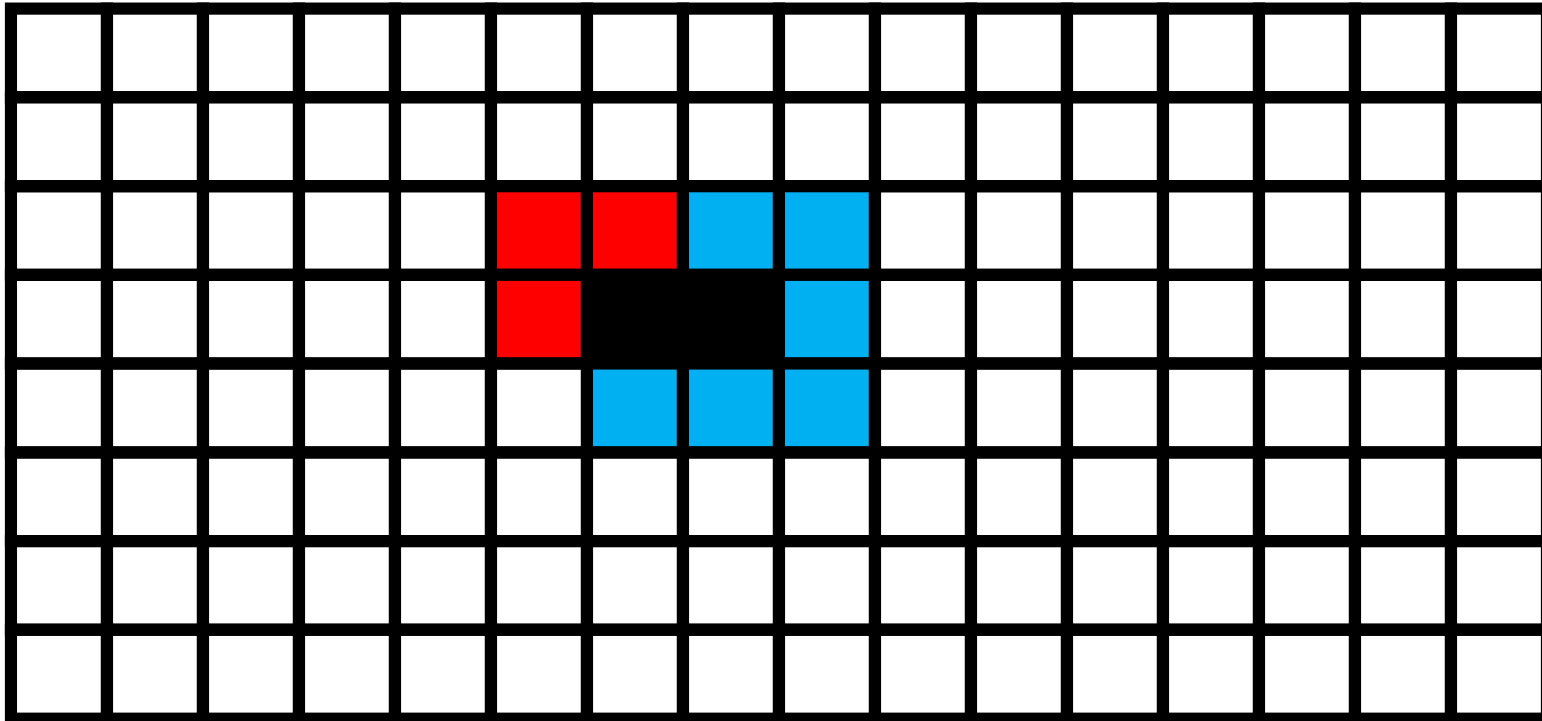
# Simple process to generate a binary mask

Pick a red pixel and change its colour to black. Select some neighbours to be part of the foreground, if they are not already, and colour them red.



# Simple process to generate a binary mask

Pick a red pixel and change its colour to black. Select some neighbours to be part of the foreground, if they are not already, and colour them red.







Simple process to generate a binary mask



# Application: binary image segmentation

- Models:
  - Simple segmentation grammar (previous slides)
  - More complex segmentation grammar
- Training:
  - Model parameters estimated using approximate EM algorithm
  - 50 train, 25 test

Ground truth

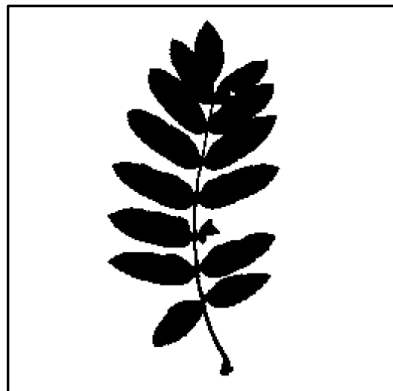
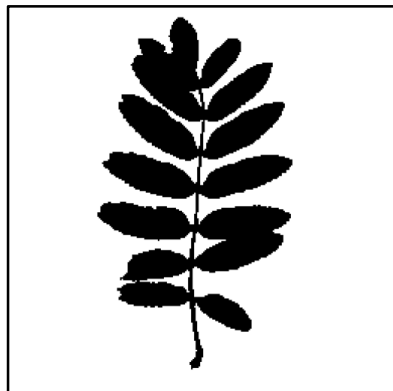
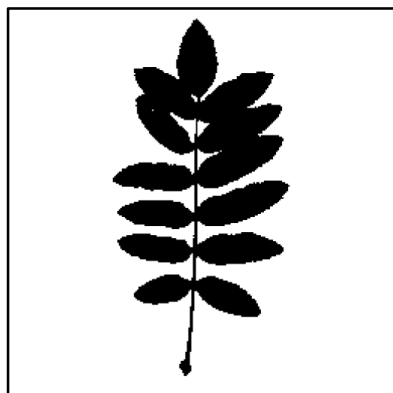
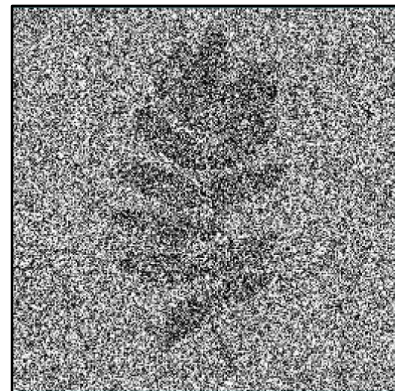
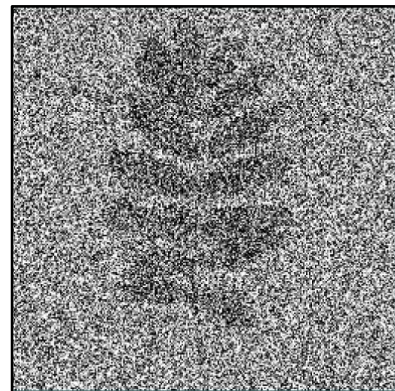
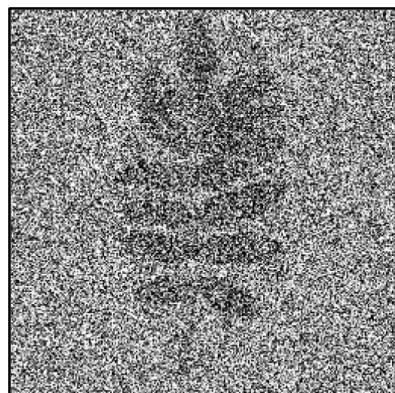
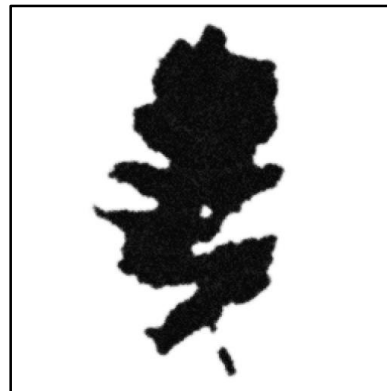
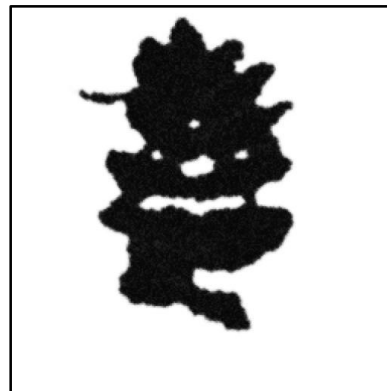


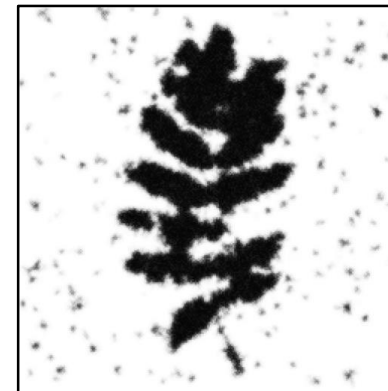
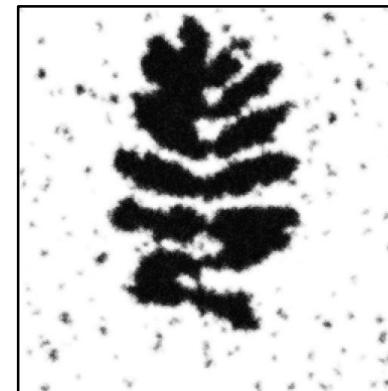
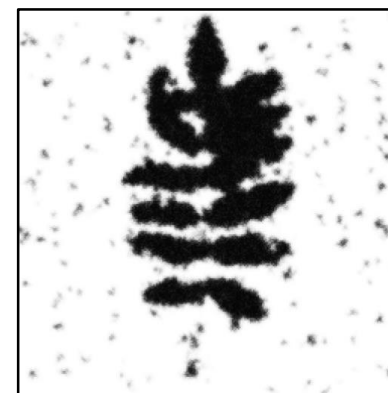
Image data



Simple grammar

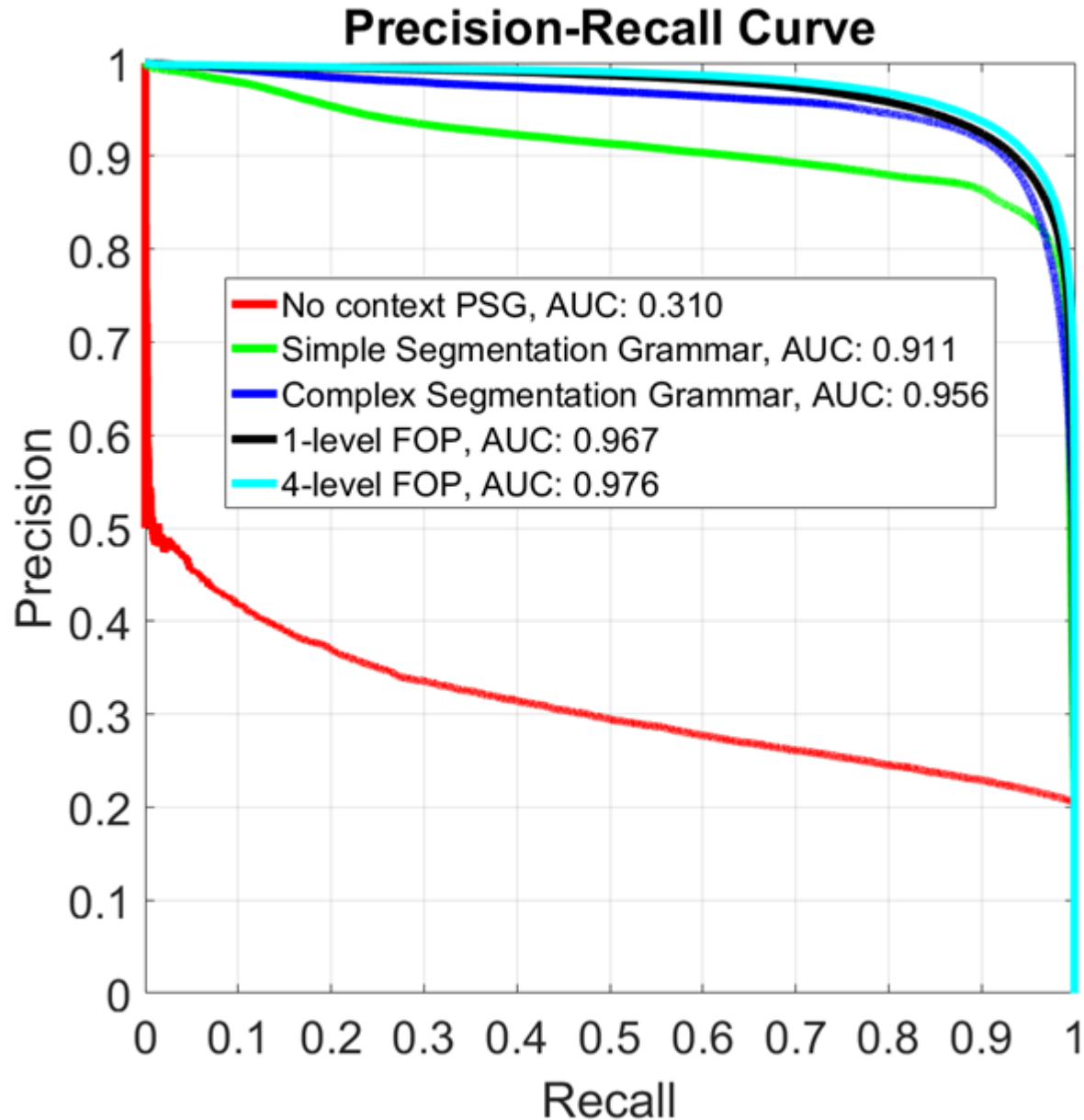


Complex grammar





# Binary image segmentation: Comparison



Context is important!

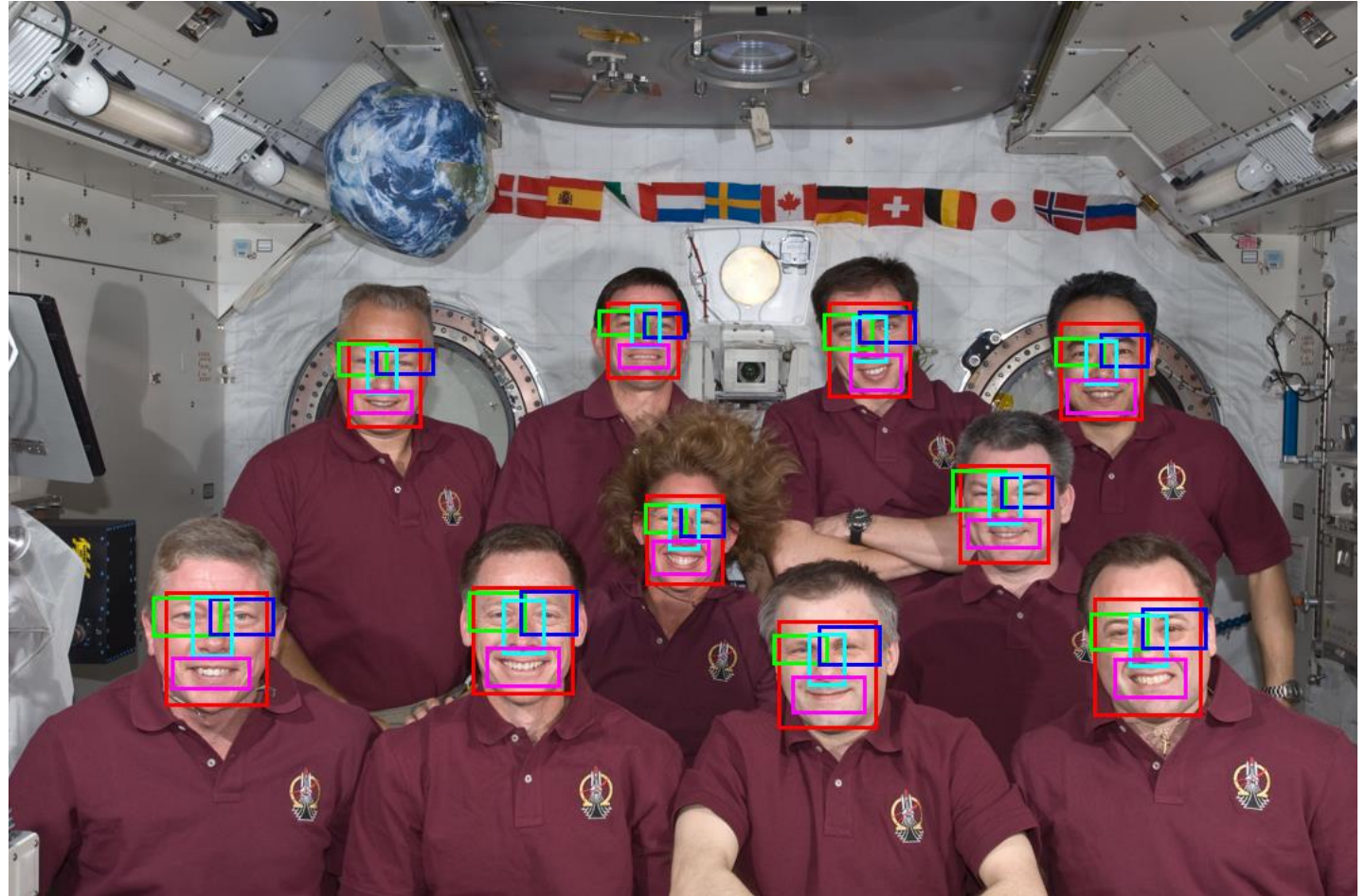
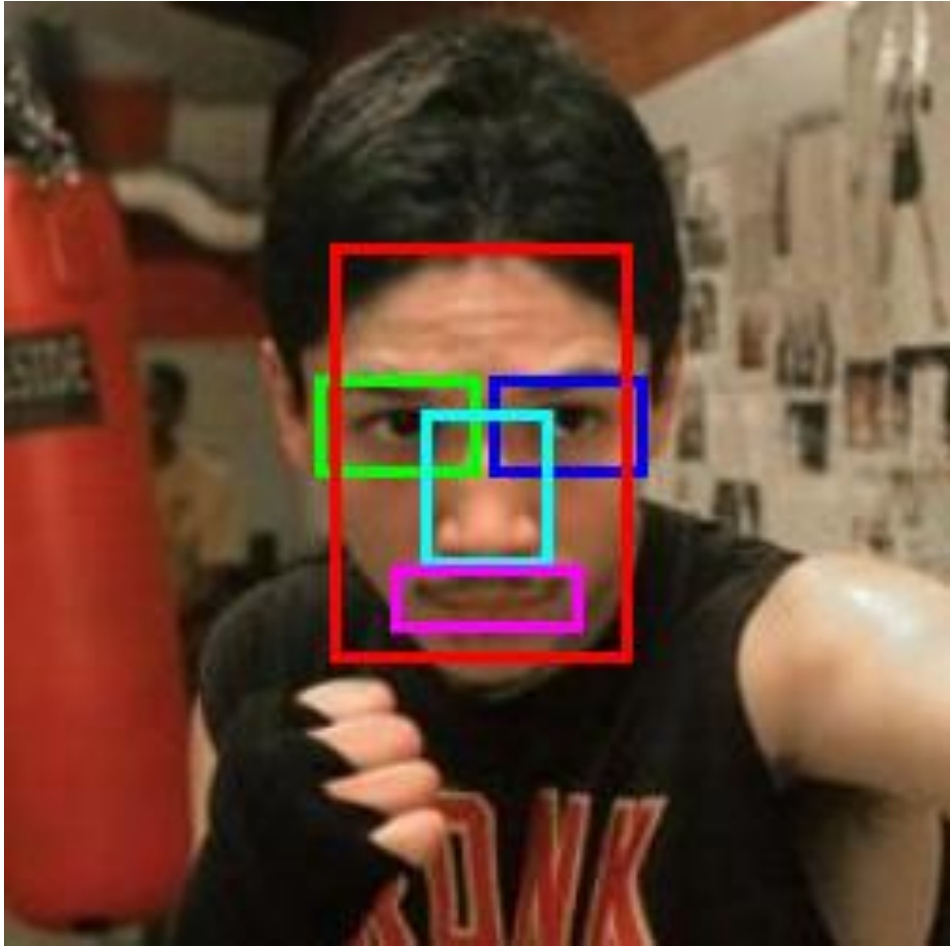
Complex segmentation grammar competitive with Field-of-Patterns (FOP)

1-level FOP and 4-level FOP from: "Multiscale Field of Patterns", Felzenszwalb, Oberlin. NIPS 2014.

# Application: Face localization

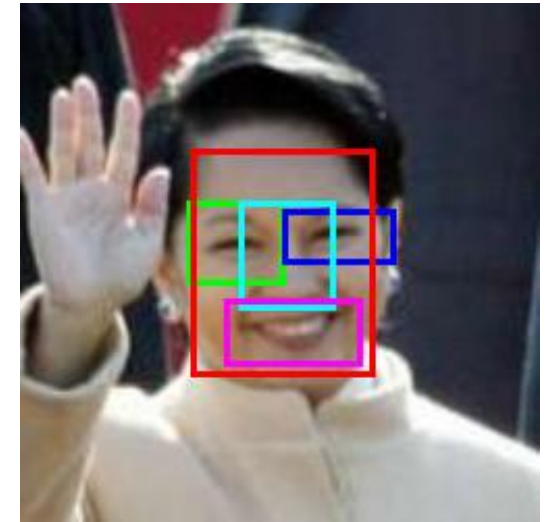
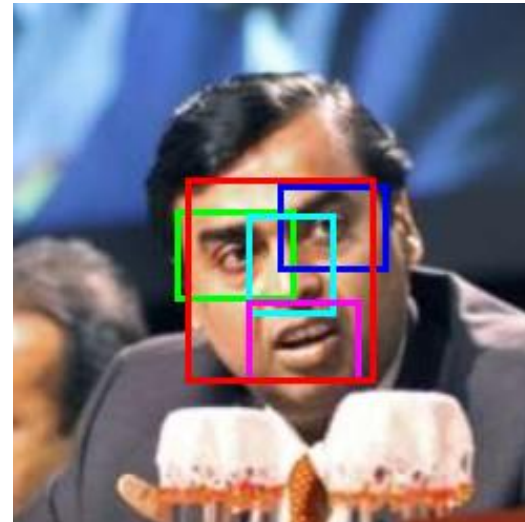
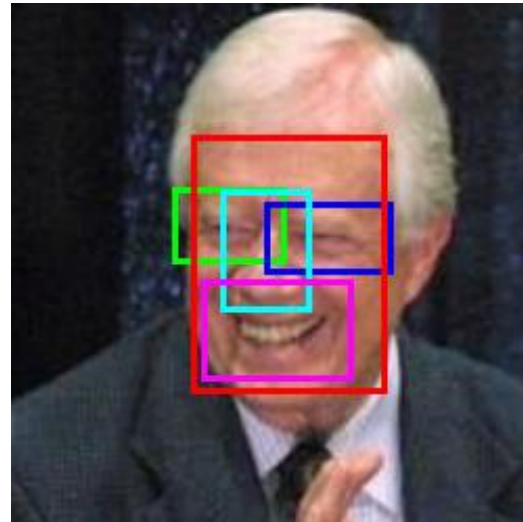
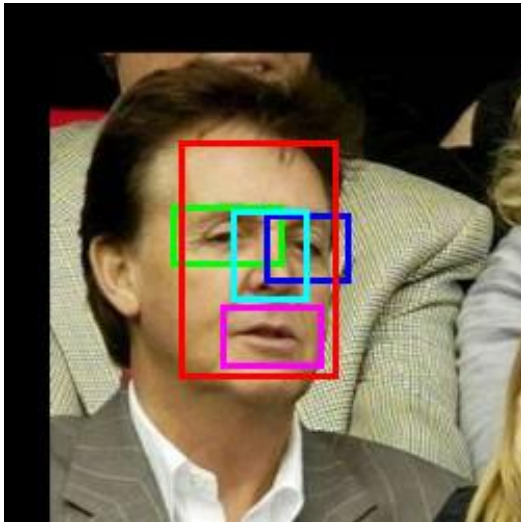


# Application: Face localization



# Face localization: Single-face Dataset

- Labelled Faces in the Wild [1]
- Manually annotated 300 images with bounding box information for face, left eye, right eye, nose, mouth
- 200 training, 100 test



[1] Huang et al., "Labeled faces in the wild: A database for studying face recognition in unconstrained environments.", Technical Report 07-49, University of Massachusetts, Amherst, October 2007.

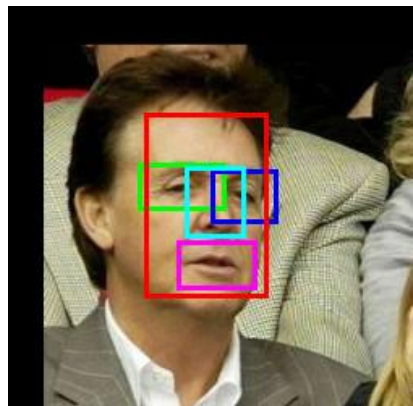
# PSG Face Grammar

- Symbols: Face (F), Left eye (L), Right eye (R), Nose (N), Mouth (M)
- Pose space: (x,y,scale)
- Mechanism to handle help suppress false positives
- Geometric model learned from labelled data
- Data-model: calibrated HOG filter scores.
- Factor graph has  $\sim 3M$  edges

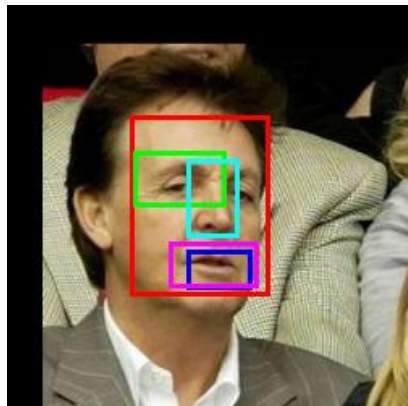
# Face localization: Baselines

- HOG Filter scores: calibrated HOG filter scores only
- “Pictorial Structures for object recognition”, IJCV 2005
  - Fast, exact inference
  - Assumes 1 object of each type per scene

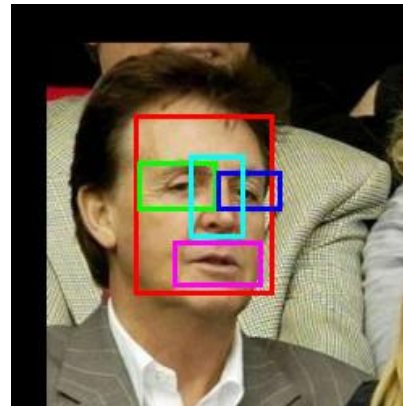
Ground truth



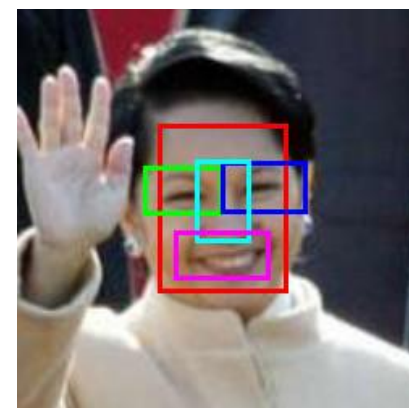
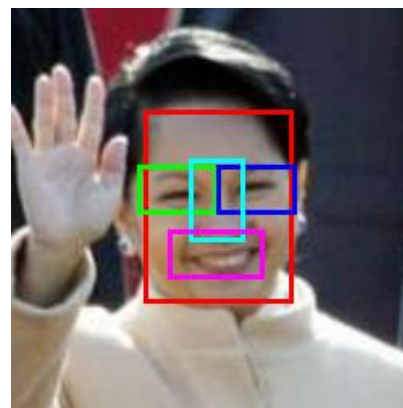
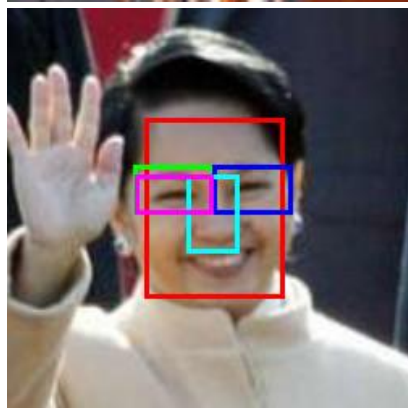
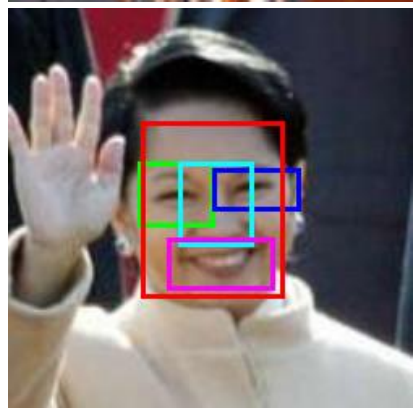
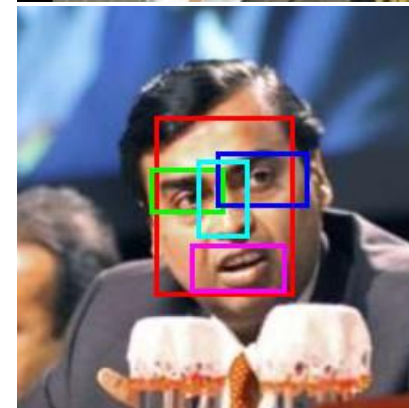
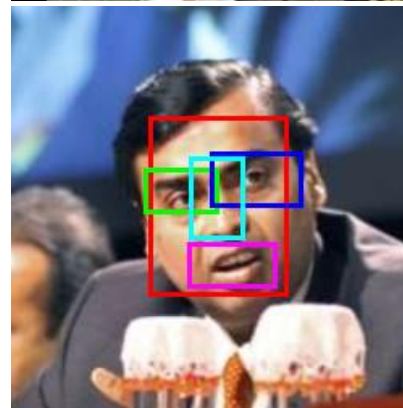
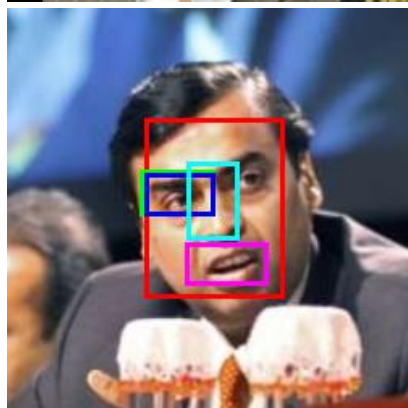
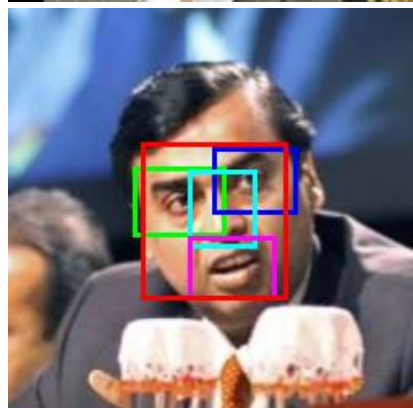
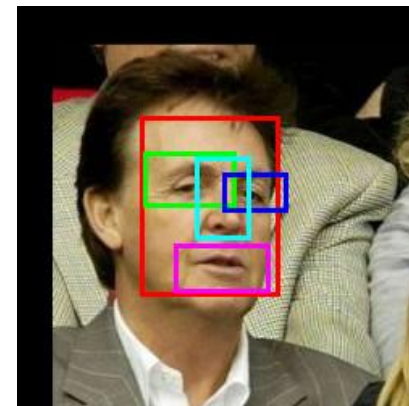
HOG Filters



Pictorial Structures



PSG Face Grammar



# Face Localization: Performance comparison

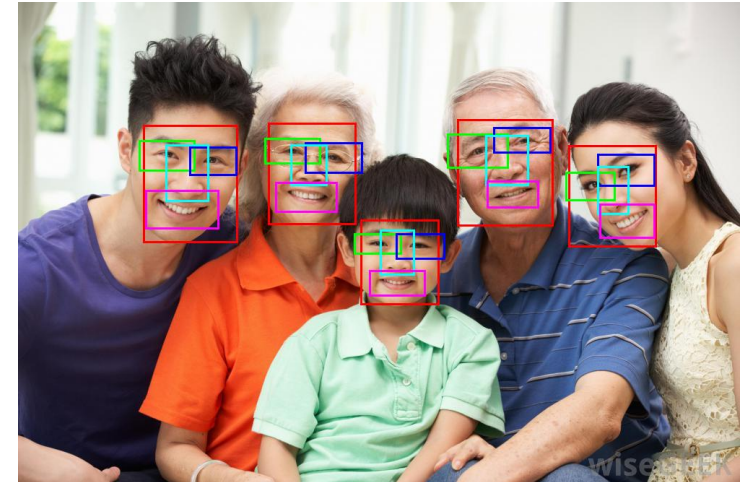
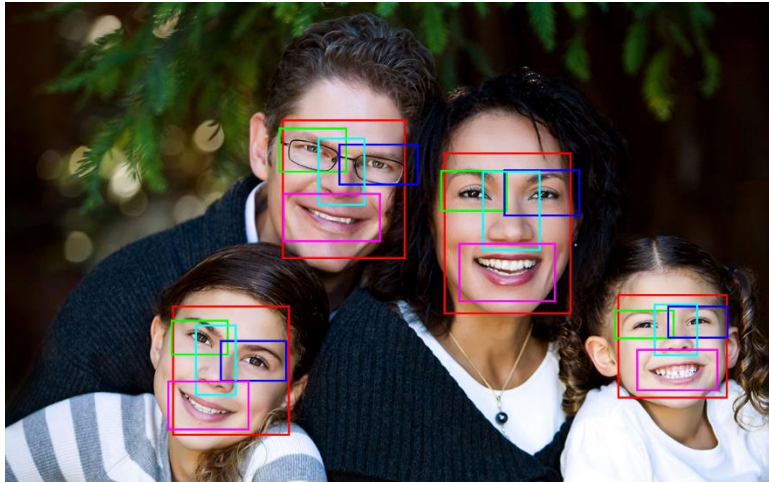
<b>Model</b>	FACE	LEFT-EYE	RIGHT-EYE	NOSE	MOUTH	<b>Average</b>
HOG Filters	1.00	0.76	0.65	0.96	0.60	0.80
Pictorial Structures	1.00	0.97	0.93	0.98	0.90	0.96
PSG Face Grammar	1.00	0.98	0.92	0.98	0.92	0.96

Area under the precision-recall curve

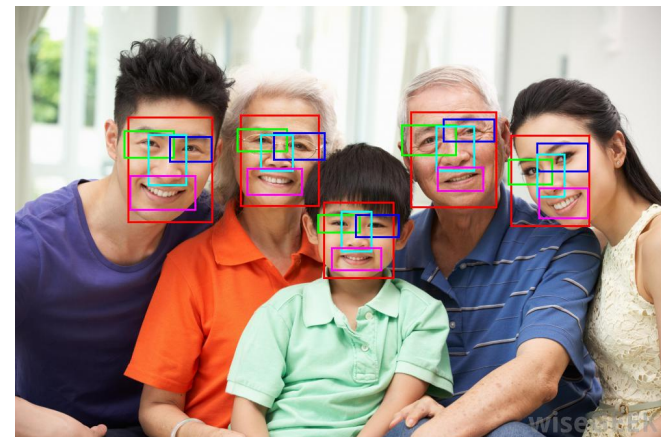
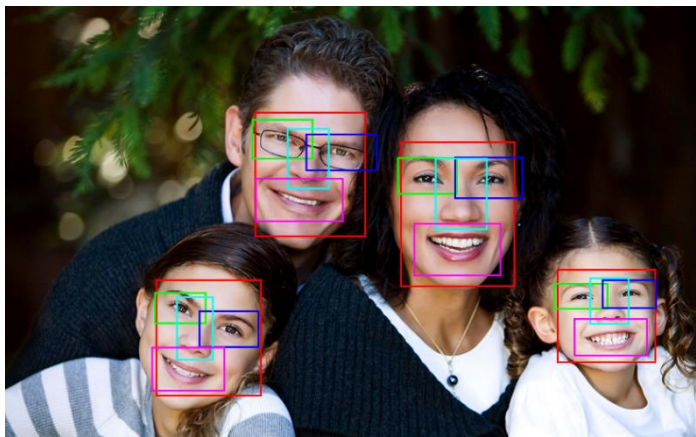


# Face localization: Family Portraits Dataset

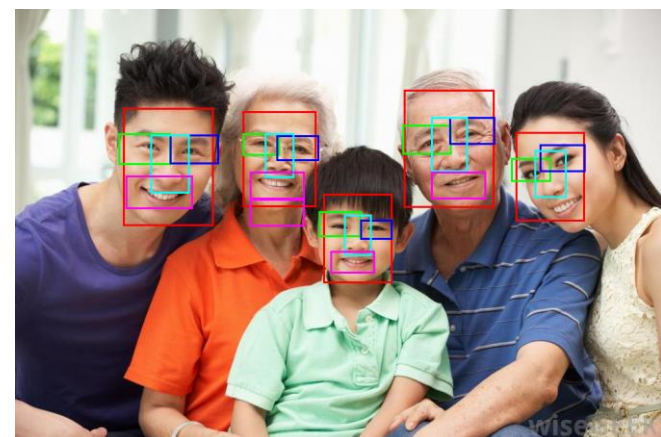
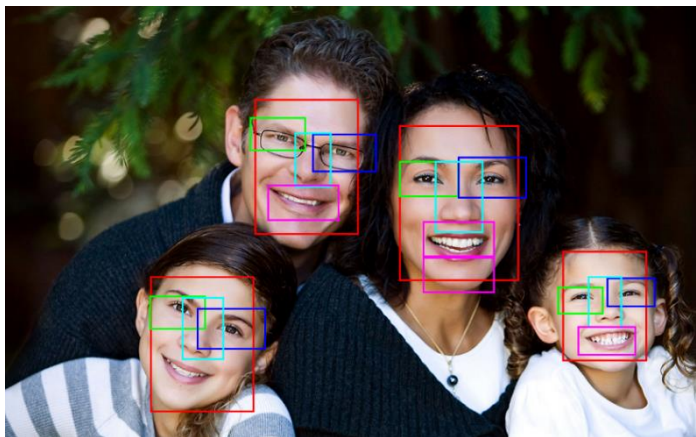
- Dataset collected from the Internet
- Manually annotated 40 images with bounding box information
- Average of 5.9 faces per image
- Similar as trained model from LFW, but with more scales
- Use all 40 images for testing



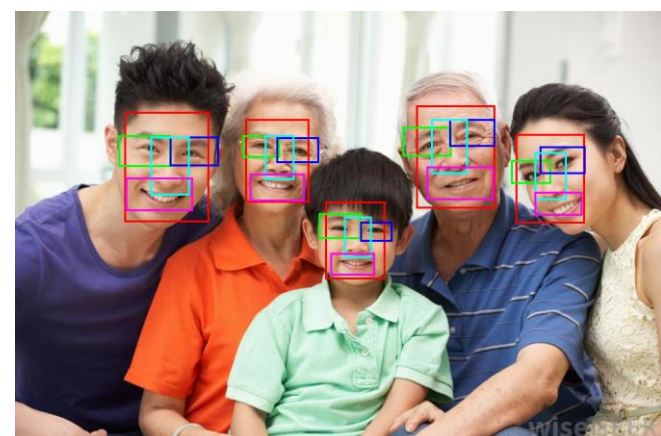
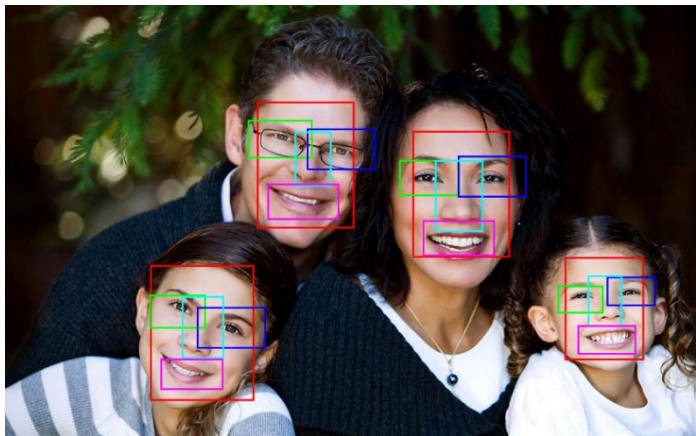
Ground truth



Pictorial Structures



PSG Face Grammar



# Face Localization: Performance Comparison

<b>Model</b>	FACE	LEFT-EYE	RIGHT-EYE	NOSE	MOUTH	<b>Average</b>
HOG Filters	0.95	0.50	0.48	0.90	0.32	0.63
Pictorial Structures	0.97	0.78	0.69	0.96	0.73	0.82
PSG Face Grammar	0.97	0.81	0.81	0.96	0.80	0.87

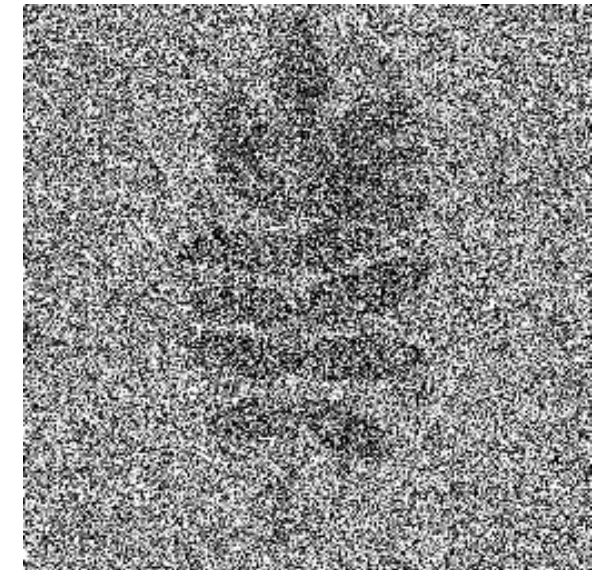
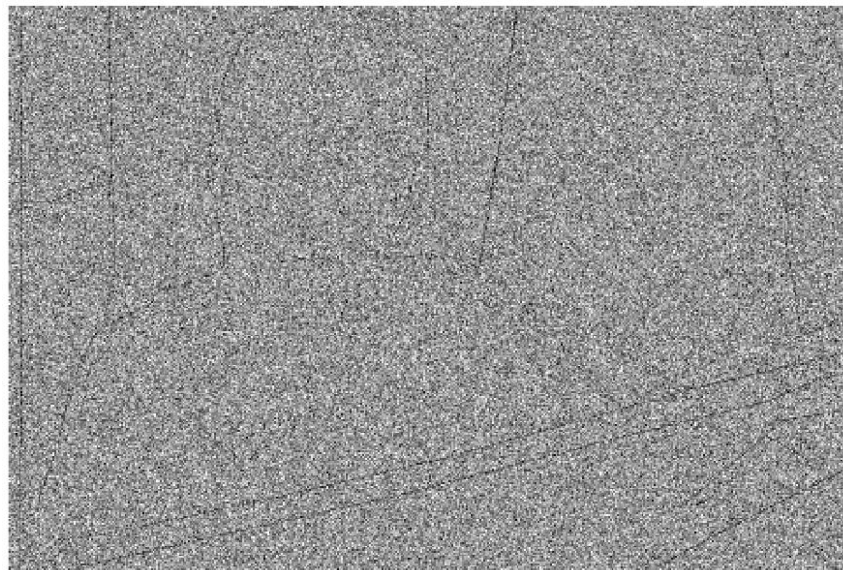
Area under the precision-recall curve

# This talk

- **Motivation** for a general scene understanding framework
- **Background/related work**
- **Representation** for general scene understanding tasks
- Efficient **approximate inference algorithm**
- **Learning algorithm** to estimate model parameters
- • **Experimental evaluation**
- **Extensions** for larger/more complex tasks
- **Directions** for future research

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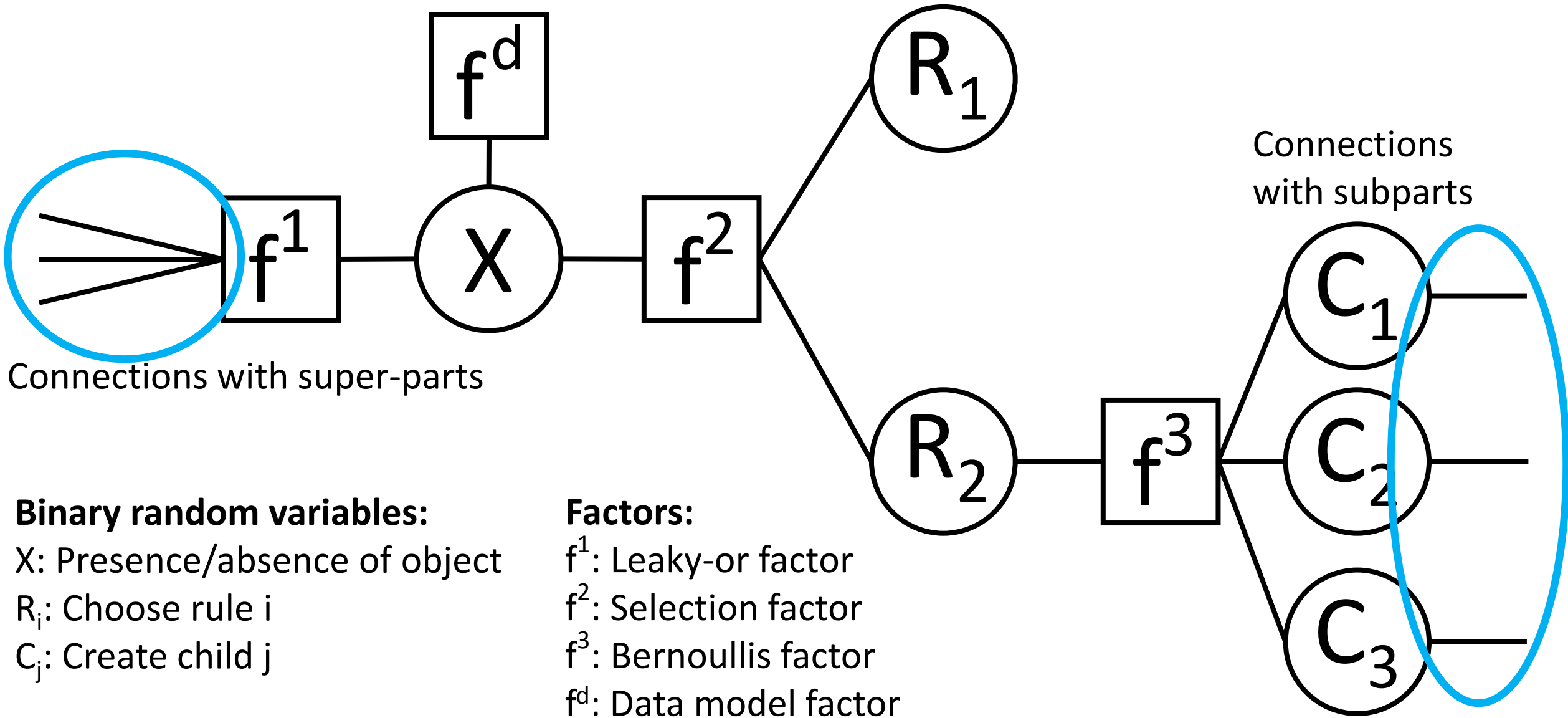


# Scaling up

- Bigger images! More objects! Larger grammars!



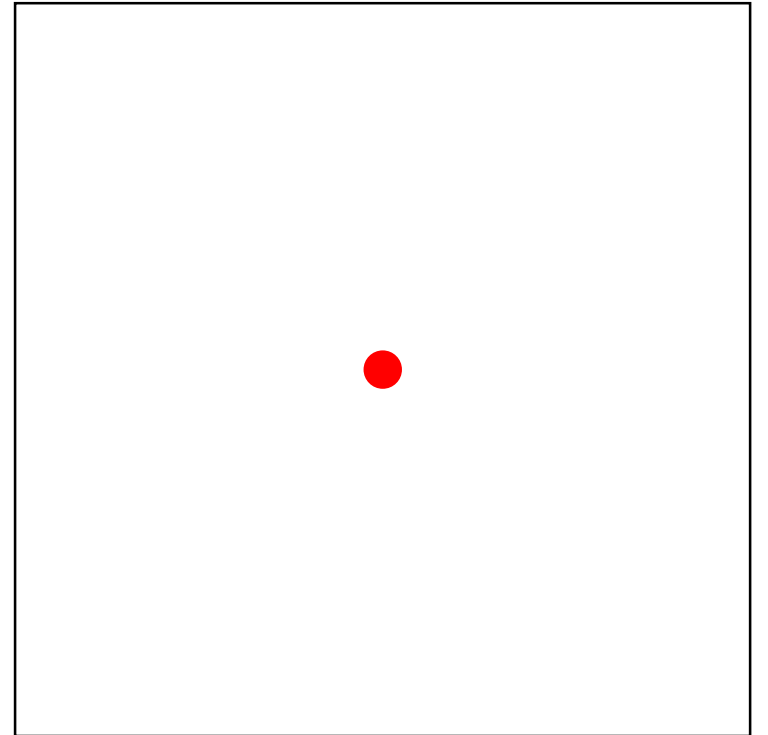
# Not so fast ...





# Graph has too many edges!

- Most edges are inter-object
- Example: Eye of a **particular** face

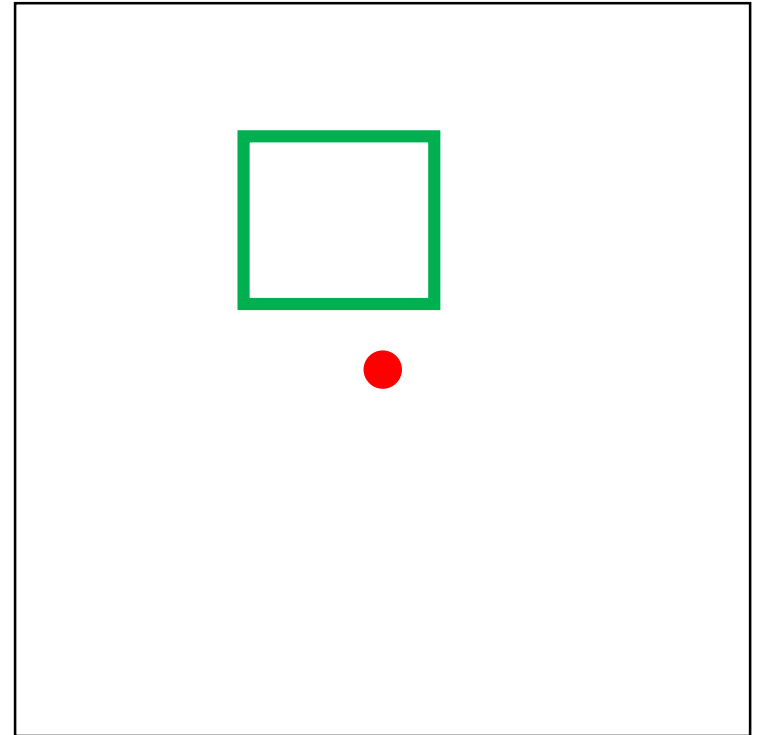


# Graph has too many edges!

- Most edges are inter-object
- Example: Eye of a **particular** face

- (15 x 15)

Size of  
image  
region

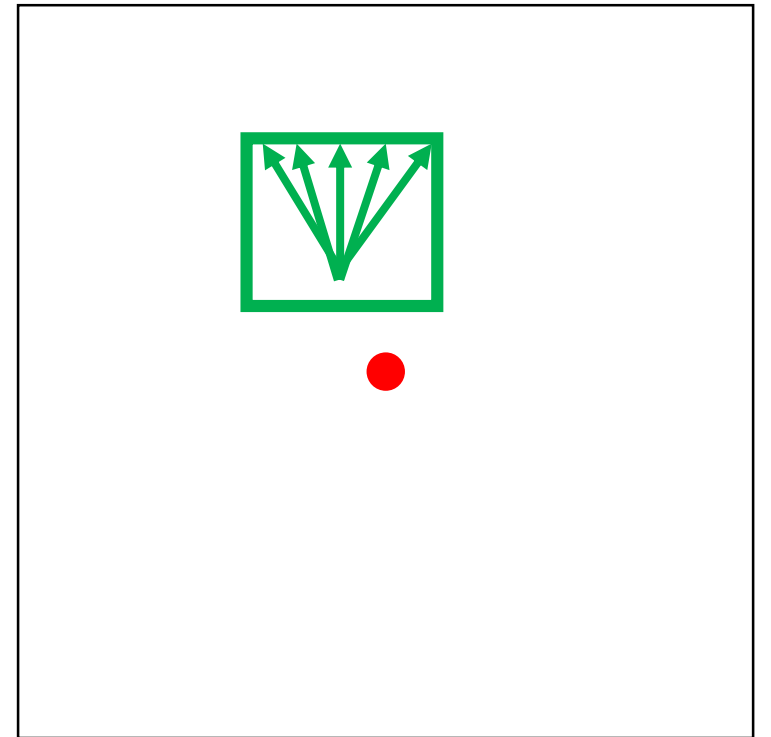


# Graph has too many edges!

- Most edges are inter-object
- Example: Eye of a **particular** face

- $(15 \times 15) \times 5$

Size of image region      # orientations

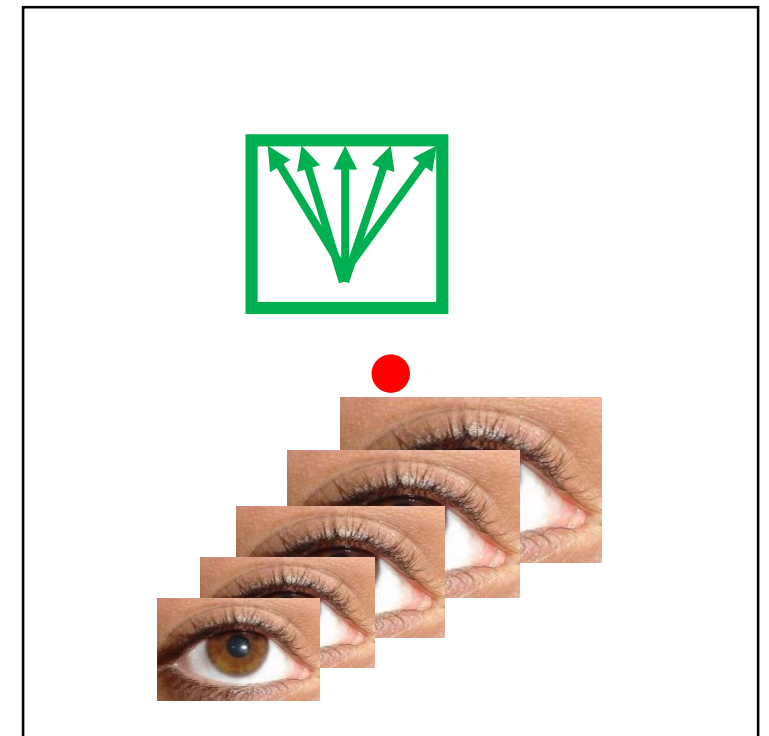


# Graph has too many edges!

- Most edges are inter-object
- Example: Eye of a **particular** face

- $(15 \times 15) \times 5 \times 5$

Size of image region      # orientations      # scales

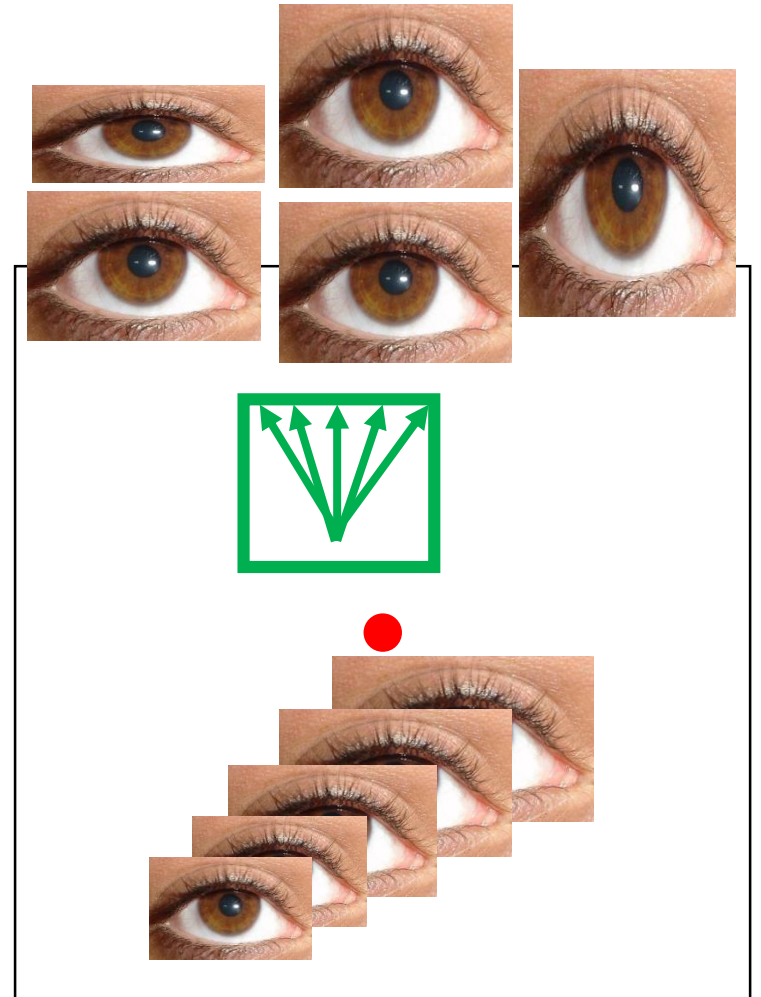


# Graph has too many edges!

- Most edges are inter-object
- Example: Eye of a **particular** face

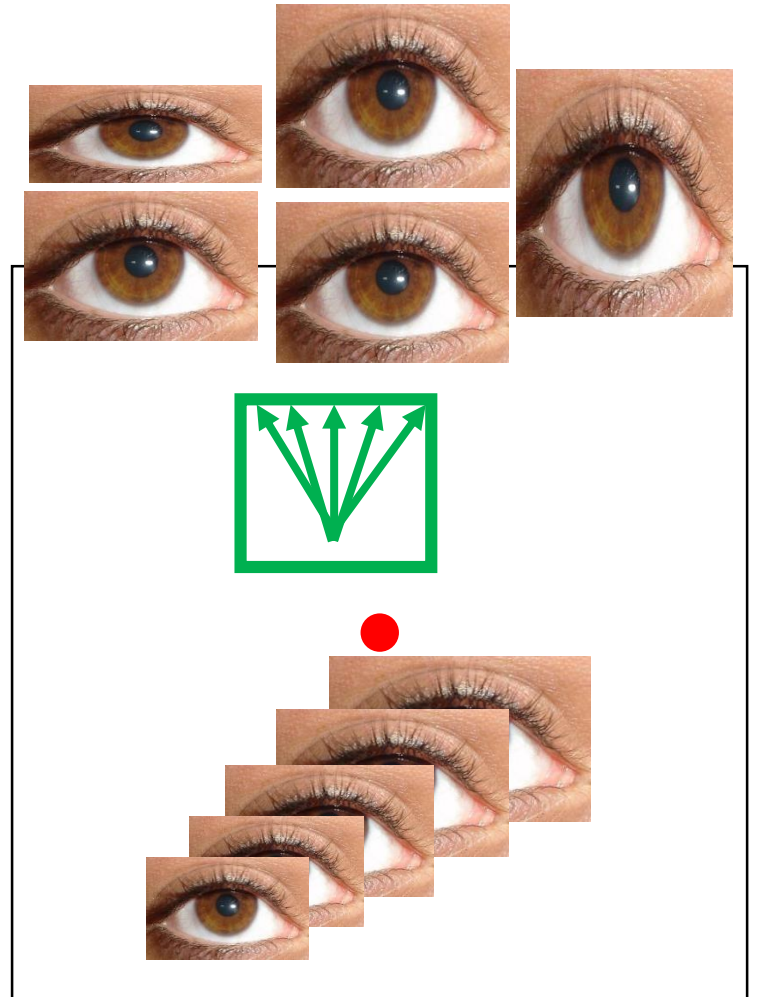
•  $(15 \times 15) \times 5 \times 5 \times 5$

Size of image region      # orientations      # scales      # aspect ratios



# Graph has too many edges!

- Most edges are inter-object
  - Example: Eye of a **particular** face
  - $(15 \times 15) \times 5 \times 5 \times 5 = 28125$  edges
- Size of image region      # orientations      # scales      # aspect ratios

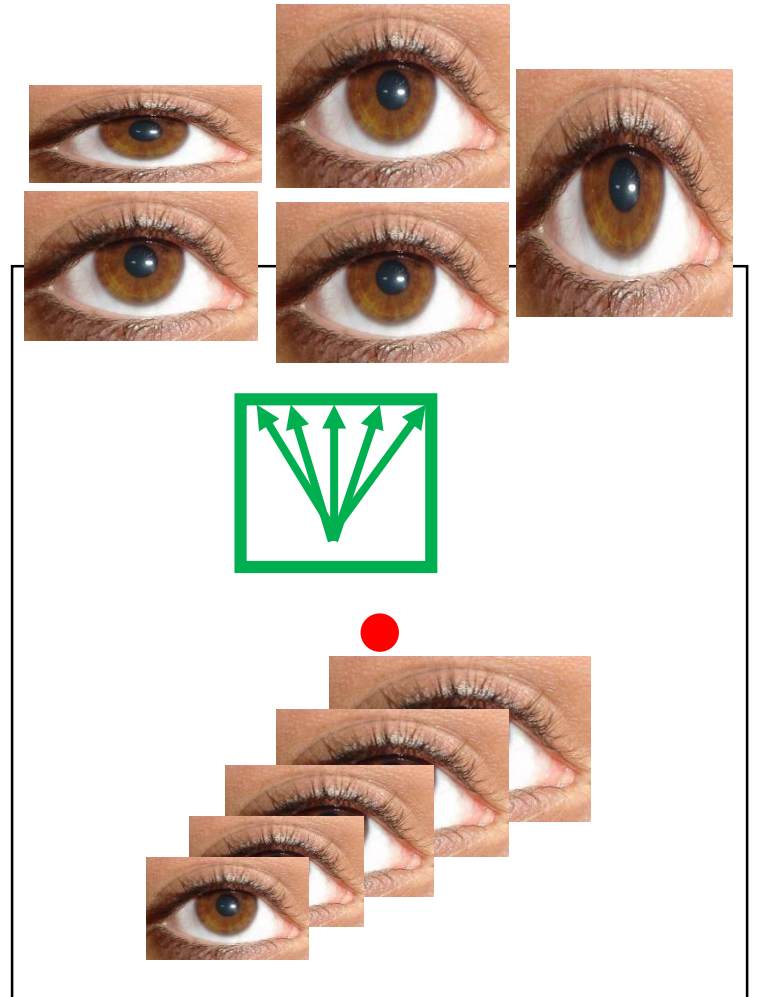


# Graph has too many edges!

- Most edges are inter-object
- Example: Eye of a **particular** face
- $(15 \times 15) \times 5 \times 5 \times 5 = 28125$  edges

Size of image region      # orientations      # scales      # aspect ratios

This is for a **single** face, and a **single** eye!  
Key issue: Size of distribution's support



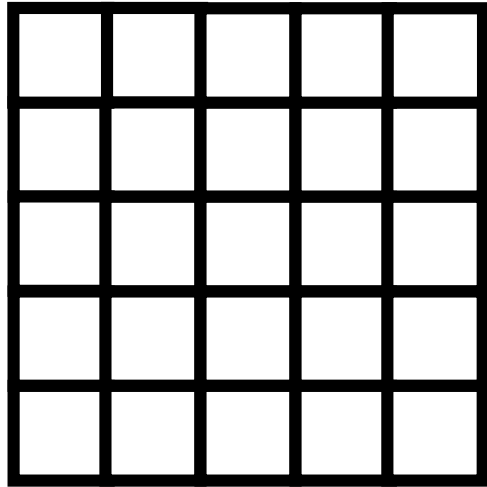
# Reducing the number of factor graph edges

- Reduce total support of probability distributions → Reduce # of factor graph edges
- **Approximate** N-D distribution as N one-dimensional distributions
- **Decompose** 1-D Uniform distribution into a set of Categorical distributions



# Approximating an N-D distribution

Where to put eye? 1 of 25 choice



Cost: 25 edges

x-coordinate of eye? 1 of 5 choice



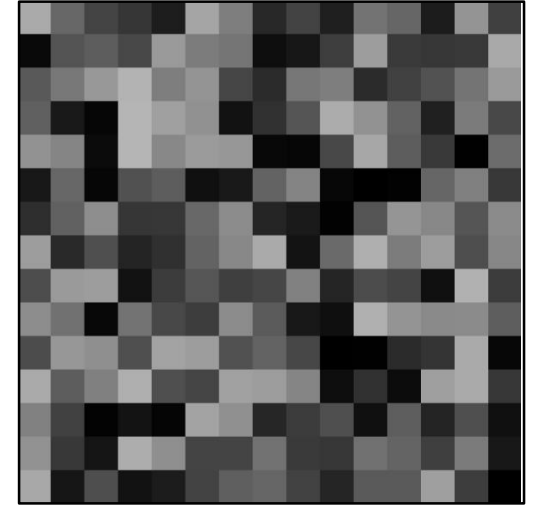
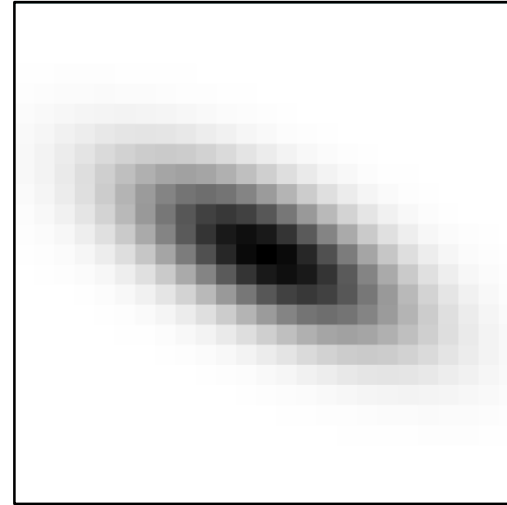
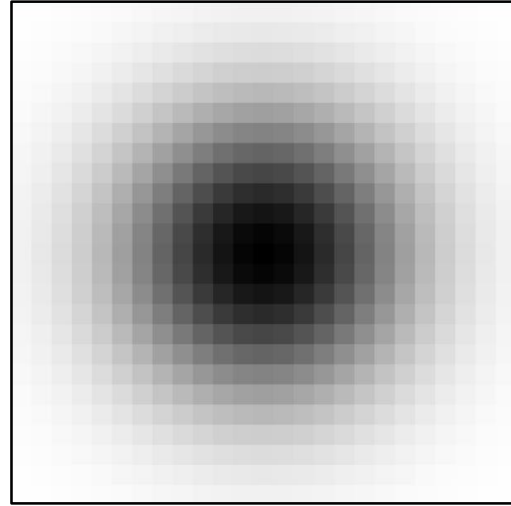
y-coordinate of eye? 1 of 5 choice



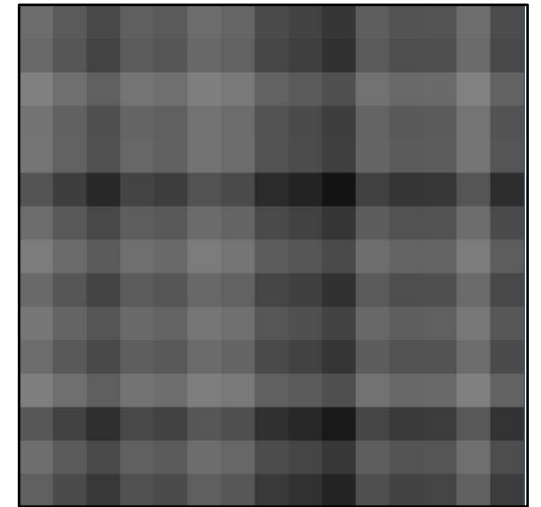
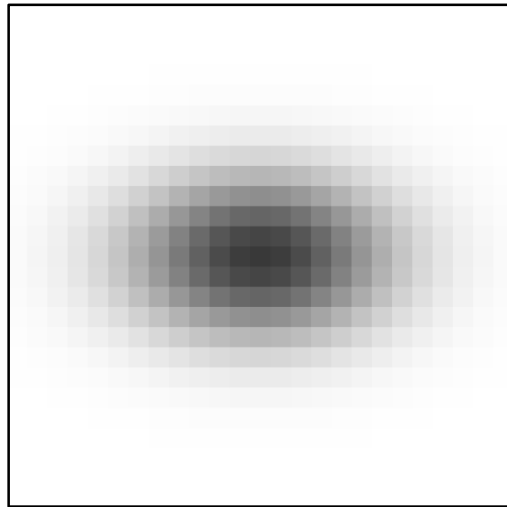
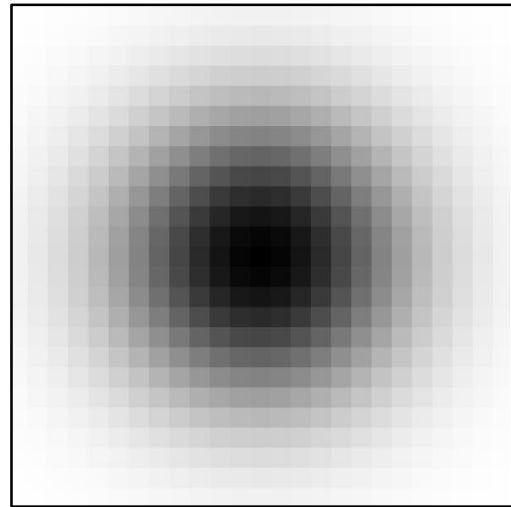
Cost: 10 edges

# Approximating an N-D distribution

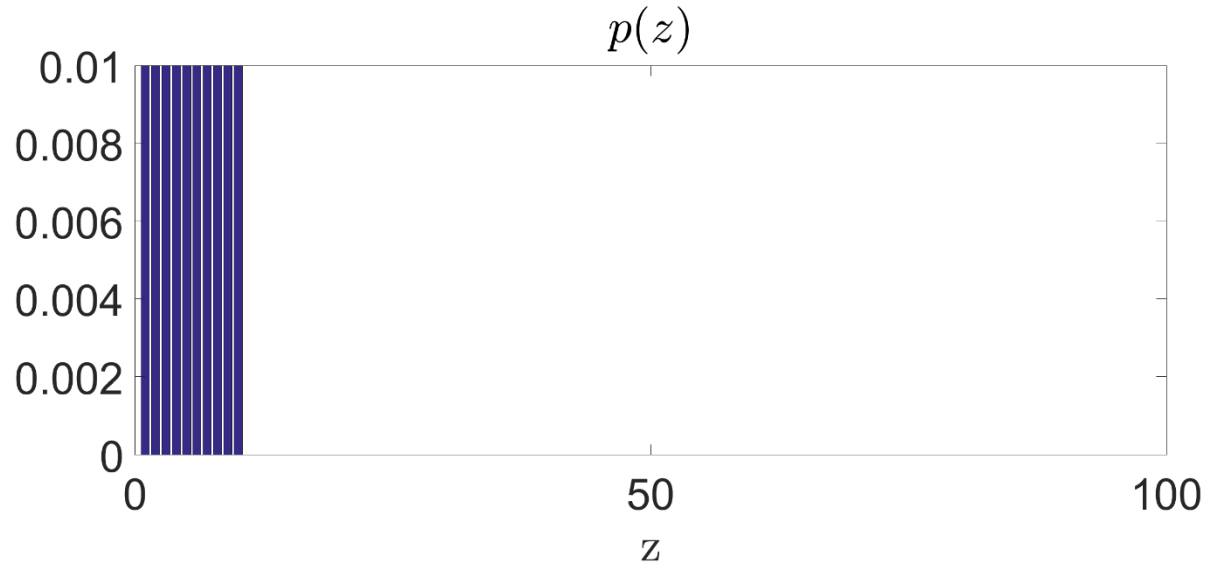
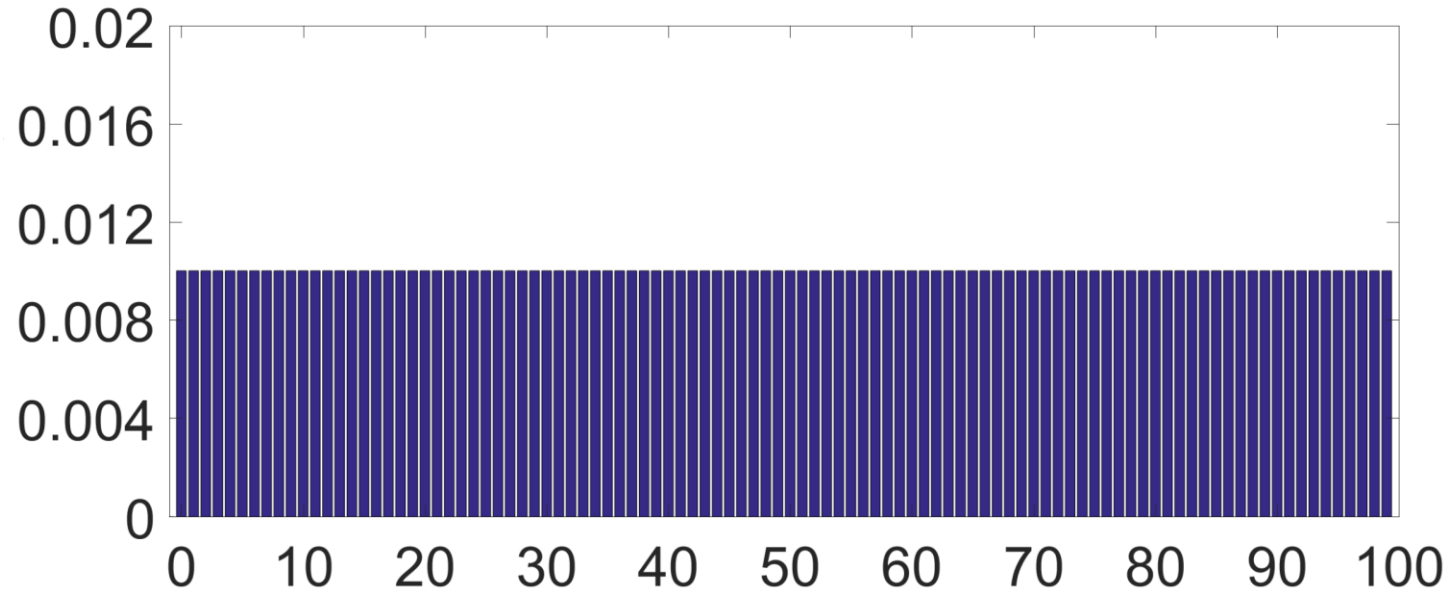
Original  
distribution



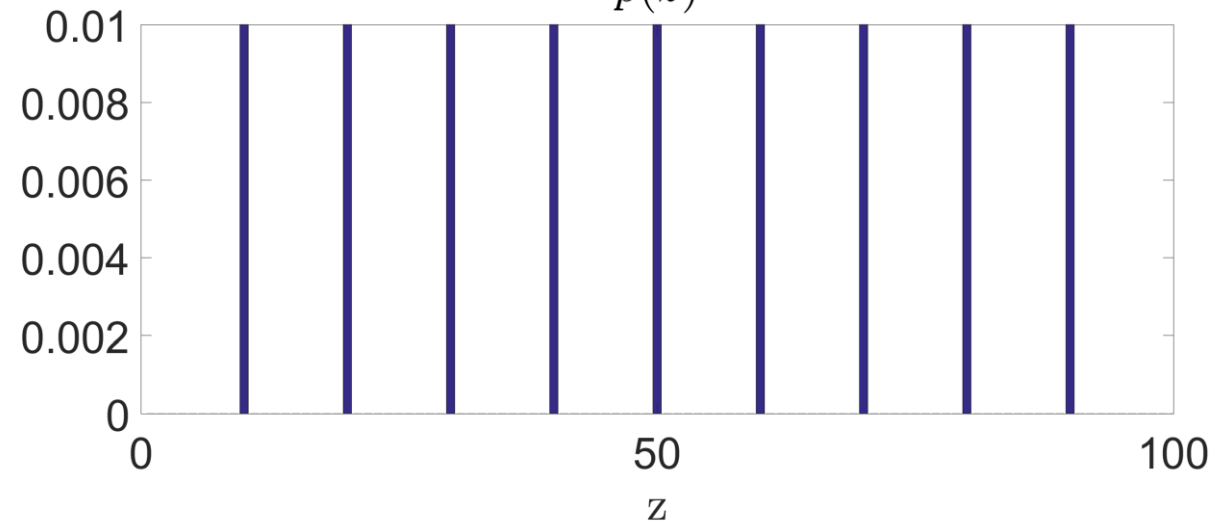
Approximated  
distribution



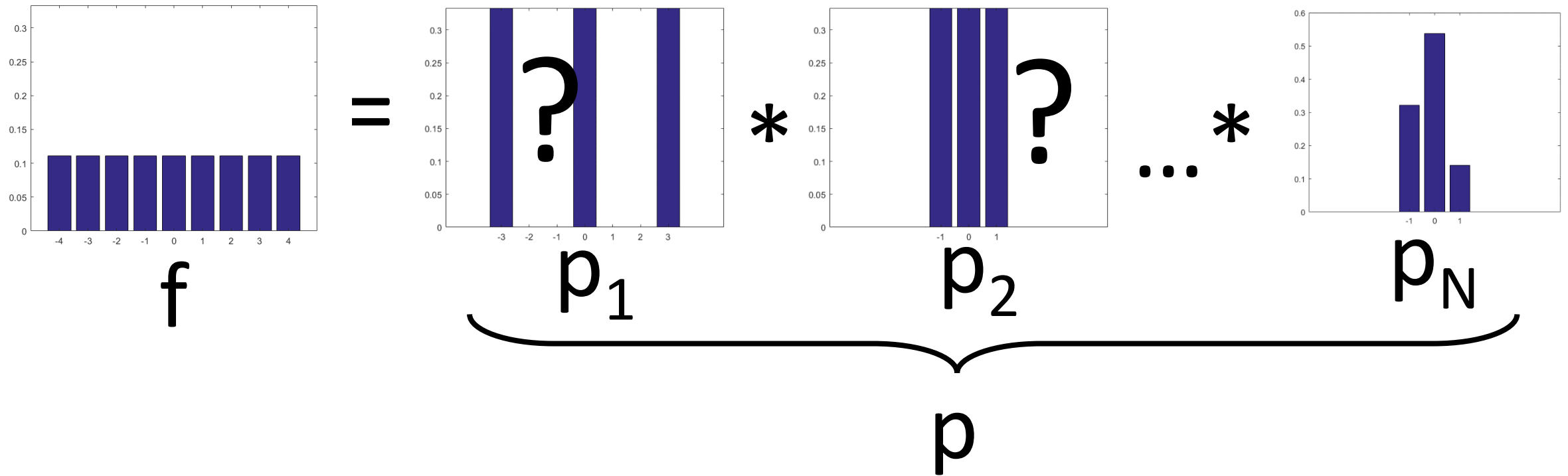
# Decomposing a Uniform distribution



\*

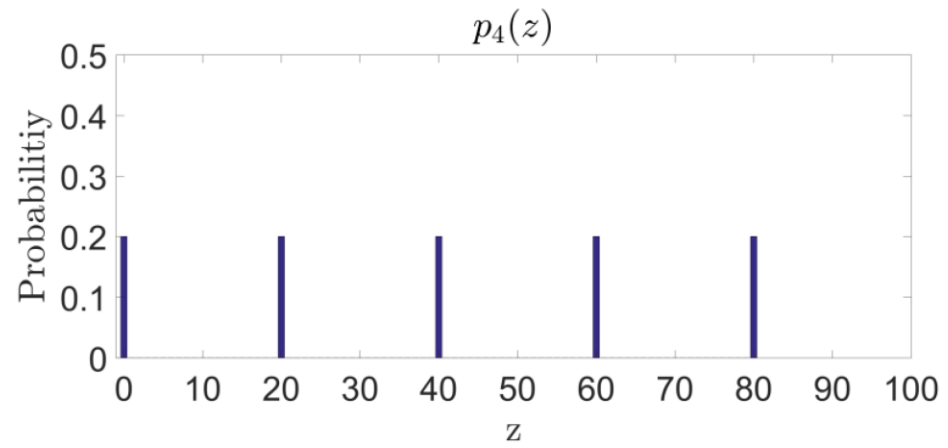
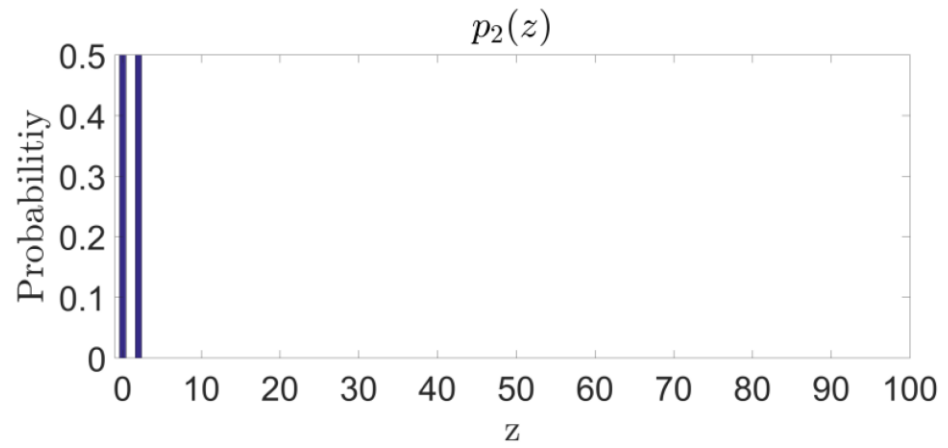
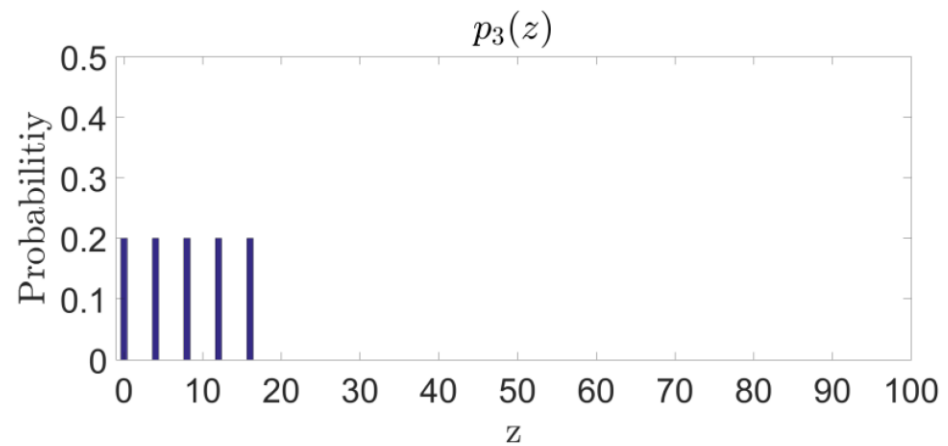
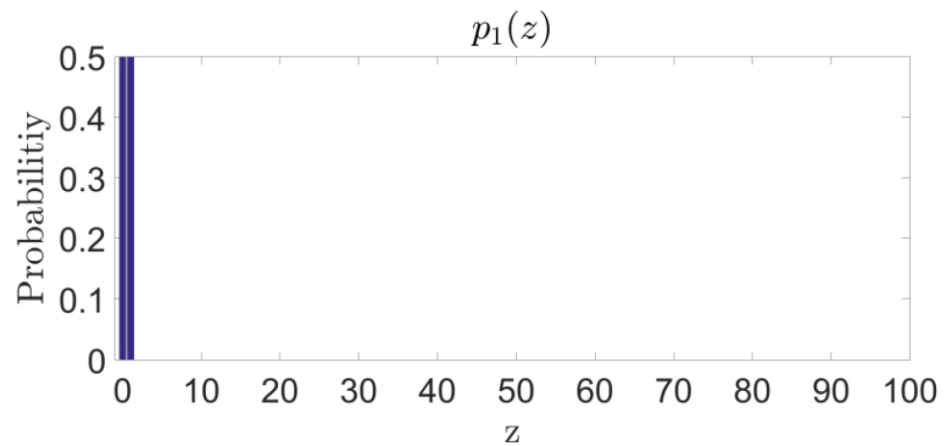


# Decomposing a Uniform distribution



- Decomposition can be phrased as a series of convolutions
- Find  $N$  and  $p_i$ 's such that  $f=p$  and  $\sum |p_i|_0$  is minimized.
- Minimum value of  $\sum |p_i|_0 =$  sum of prime factorization of  $|f|_0$
- Construction algorithm for  $p_i$ 's in thesis

# Decomposing a Uniform distribution on set $\{0, \dots, 99\}$



Total support size: 14

# Applying edge reductions

Rule	Spatial distribution	Size of region
Face → Nose	Uniform	[25,25]

625 edges



Rule	Spatial distribution	Size of region
Face → Nose-Y	Uniform	[1,25]
Nose-Y → Nose	Uniform	[25,1]

50 edges



Rule	Spatial distribution	Size of region
Face → Nose-Y1	Uniform	[1,5]
Nose-Y1 → Nose-Y	Uniform	[1,5]
Nose-Y → Nose-Y2	Uniform	[5,1]
Nose-Y2 → Nose	Uniform	[5,1]

20 edges

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# Directions for Future Research

- More scene understanding tasks
- Integration with Deep Learning
- Grammar learning

# This talk

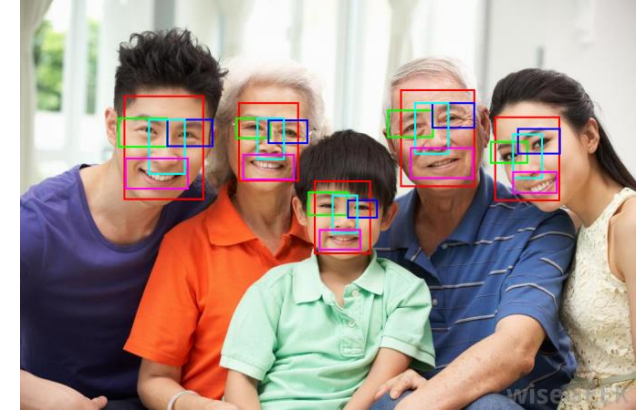
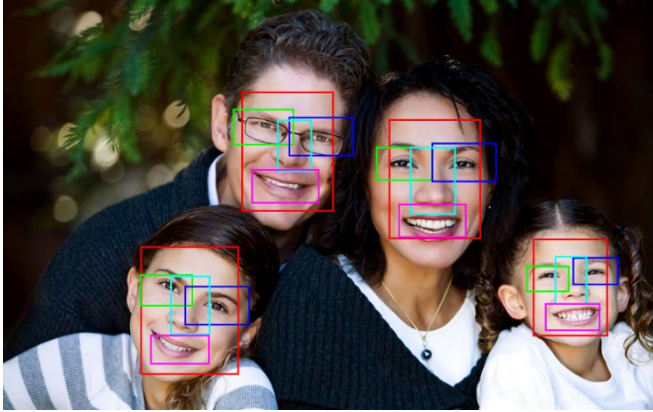
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# Thanks!

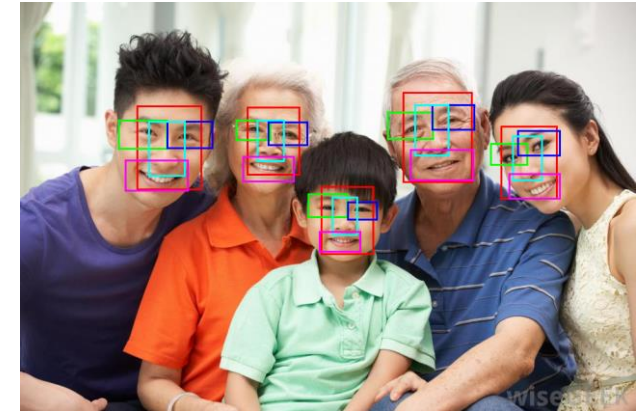
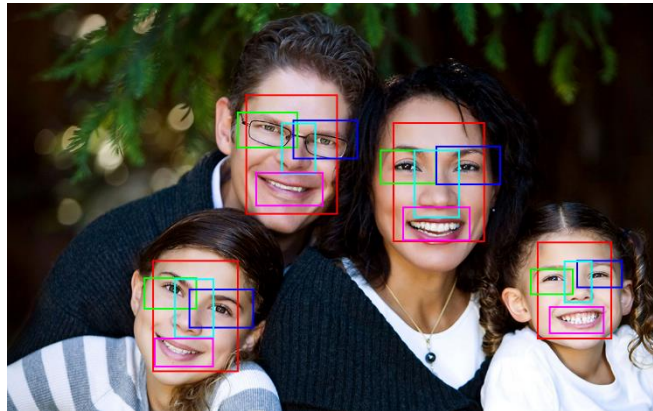
Backup slides start

# Face localization **without** a face data model

PSG Face Grammar



Faceless Grammar

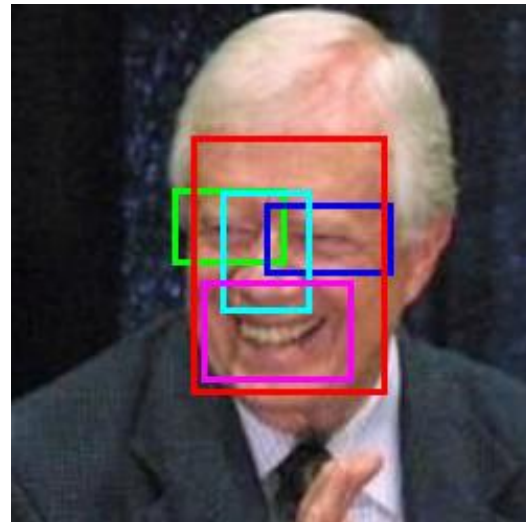
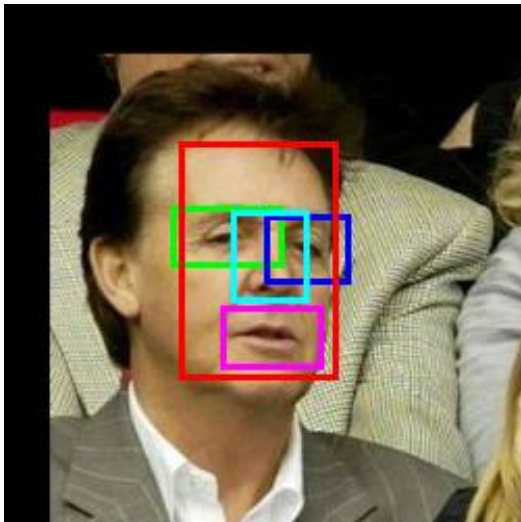


<b>Model</b>	<b>FACE</b>	<b>LEFT-EYE</b>	<b>RIGHT-EYE</b>	<b>NOSE</b>	<b>MOUTH</b>	<b>Average</b>
PSG Face Grammar	0.97	0.81	0.81	0.96	0.80	0.87
Faceless Grammar	0.93	0.78	0.80	0.95	0.76	0.84

Family Portraits: Area under the precision-recall curve

# Face localization: 0-1 Face Dataset

- Labelled Faces in the Wild [1] + images from VOC2012[2] without faces
- 200 training, 200 test
- 100 test image have one face, 100 images have no faces.



[1] Huang et al., "Labeled faces in the wild: A database for studying face recognition in unconstrained environments.", Technical Report 07-49, University of Massachusetts, Amherst, October 2007.

[2] Everingham, et al., "The PASCAL Visual Object Classes Challenge 2012 {(VOC2012)} Results", 2012.

# Face localization: 0-1 Face Dataset

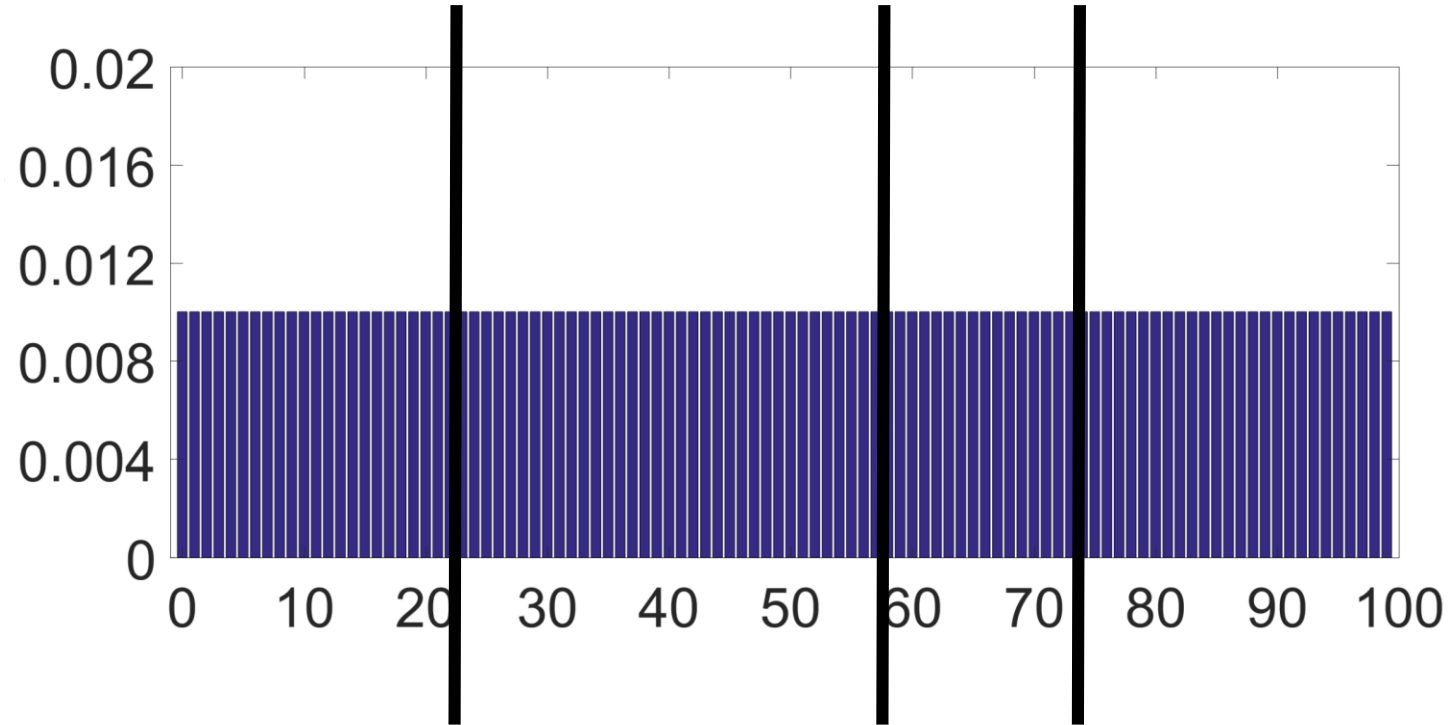
Model	Face	Left eye	Right eye	Nose	Mouth	Average
Pictorial Structures	0.86	0.94	0.86	0.81	0.84	0.86
PSG Face Grammar	1.00	0.98	0.95	0.99	0.93	0.97

Area under the precision-recall curve for the 0-1 Face Dataset

Model	Face	Left eye	Right eye	Nose	Mouth	Average
Pictorial Structures	1.00	0.97	0.93	0.98	0.90	0.96
PSG Face Grammar	1.00	0.98	0.92	0.98	0.92	0.96

Area under the precision-recall curve for the Single-Face Dataset

# Decomposing a Uniform distribution with prime support



Search over partitions. Dynamic programming?